

# Transient Response Analysis and Design of Current-Controlled Grid-Tied Converters

Author: *Ana Vidal González*

Supervisors: *Jesús Doval Gando y & Francisco D. Freijedo Fernández*

Applied Power Electronics Research Group,  
University of Vigo

15th May 2015

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Dissertation submitted for the degree of Doctor of  
Philosophy at the University of Vigo  
“International Doctor Mention”

**APET** Applied Power  
Electronics Technology  
Research Group

Universidade de Vigo

# Outline

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1. Introduction
2. Equivalent Loss Resistance Estimation of Grid-Tied Converters for Current Control Analysis and Design
3. A Method for Identification of the Equivalent Inductance and Resistance in the Plant Model of Current-Controlled Grid-Tied Converters
4. Assessment and Optimization of the Transient Response of Proportional-Resonant Current Controllers for Distributed Power Generation Systems
5. Transient Response Evaluation of Stationary-Frame Resonant Current Controllers for Grid-Connected Applications
6. Conclusions and Future Research

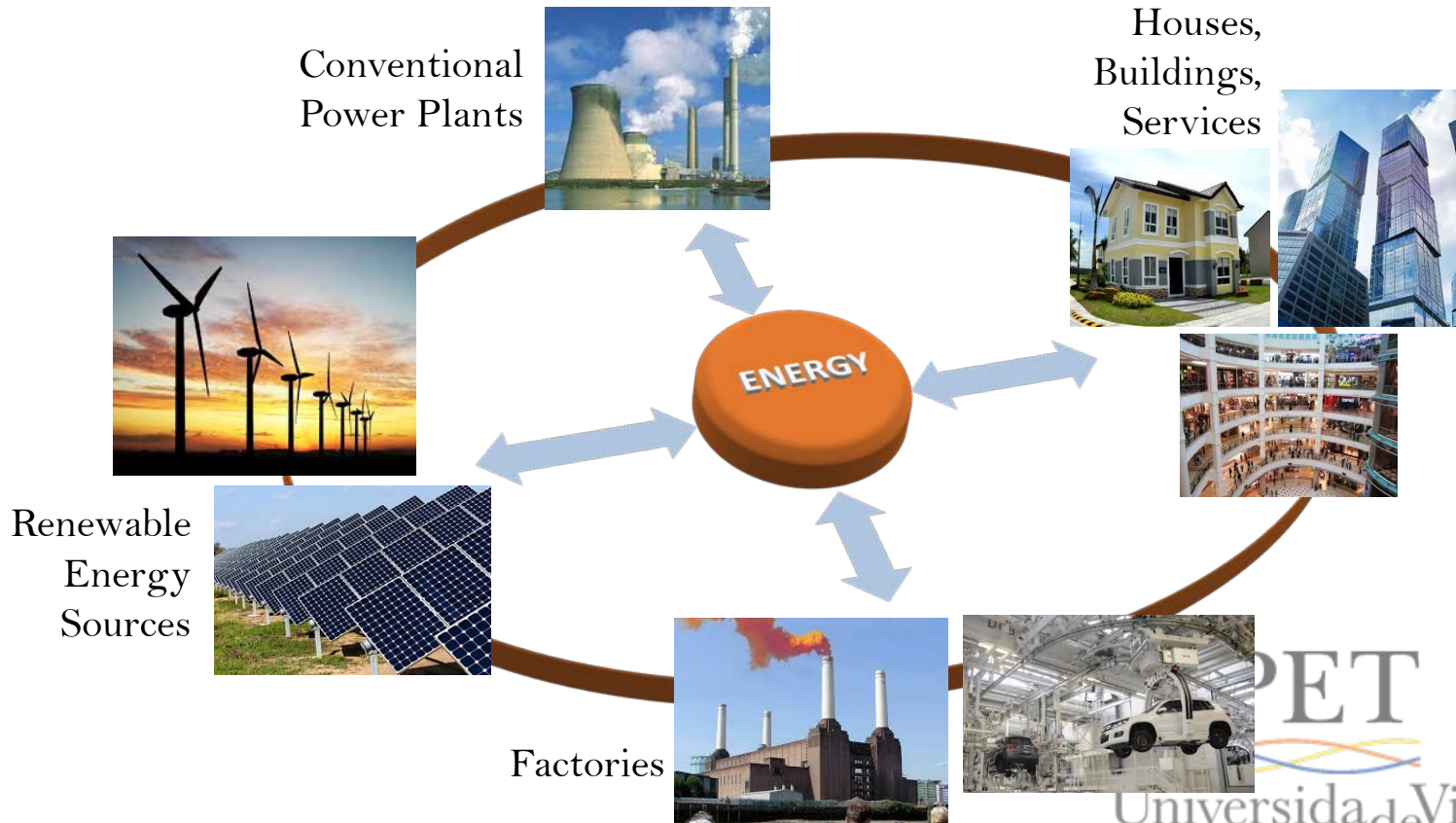
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  - Background
  - Objectives
  - Review of Previous Research
2. Equivalent Loss Resistance Estimation of Grid-Tied Converters for Current Control Analysis and Design
3. A Method for Identification of the Equivalent Inductance and Resistance in the Plant Model of Current-Controlled Grid-Tied Converters
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# Current Electric Grid

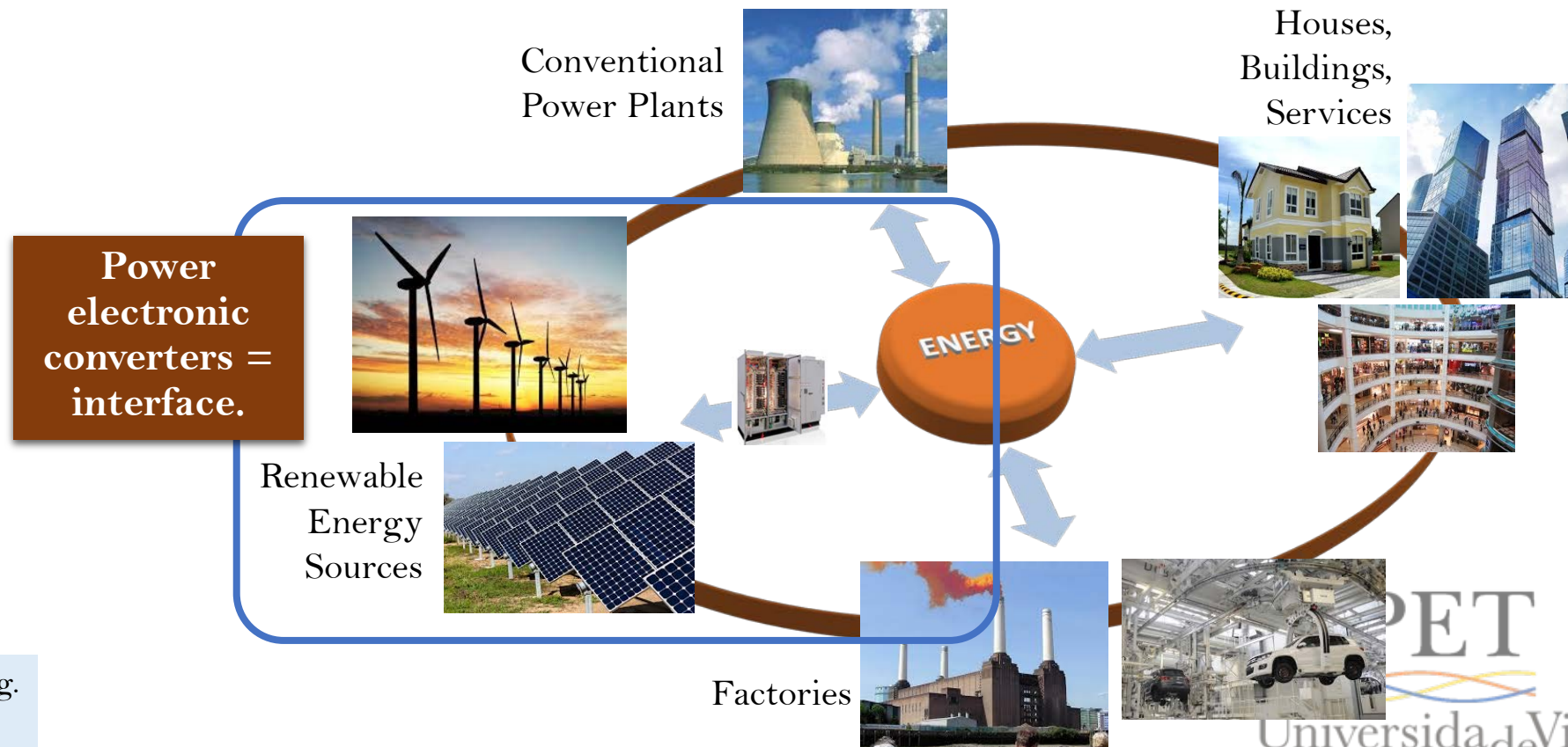
- ✓ Flexibility
- ✓ Bidirectionality
- ✗ Problems to guarantee stability → Grid codes





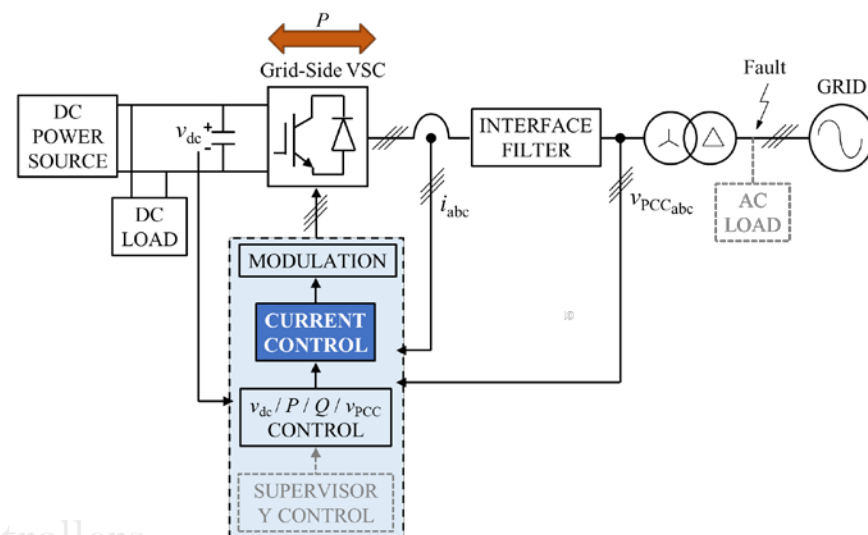
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# Grid-Side VSC

- Tasks
  - Maintaining the dc link constant
  - Interaction with the grid ( $P$  &  $Q$ )
- Implementation
  - Modulation stage
  - Multiple cascaded loops of linear controllers
    - Outer power/ dc-link voltage controllers
    - Inner current controllers
      - Appropriate power factor
      - Harmonic rejection
      - Disturbance rejection (faults)
      - Fast transient response



Accurate tuning  
of the  
regulators

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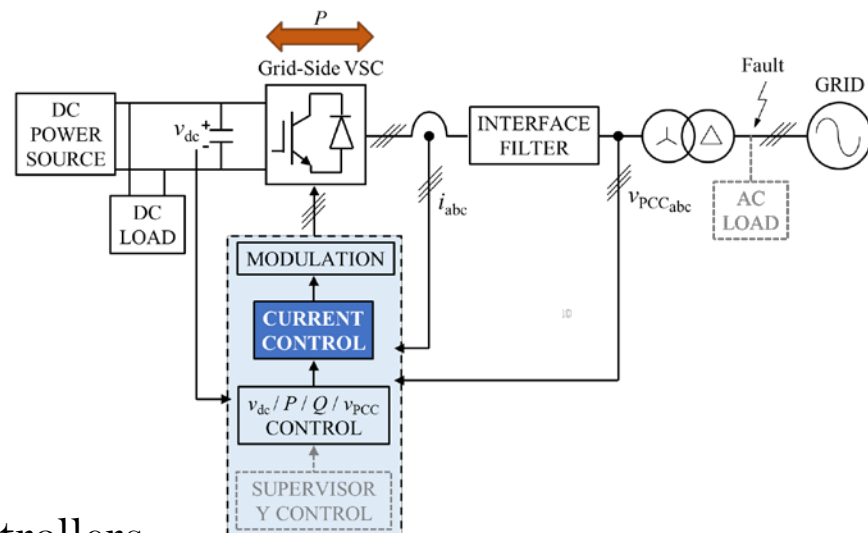
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## Main Objective of this Thesis

- A thorough analysis and design of the current control closed loop, oriented to an accurate tuning of the regulators is developed.

Precise plant model.

Accurate plant parameters.

Appropriate controller structure.

Rigorous regulator tuning.

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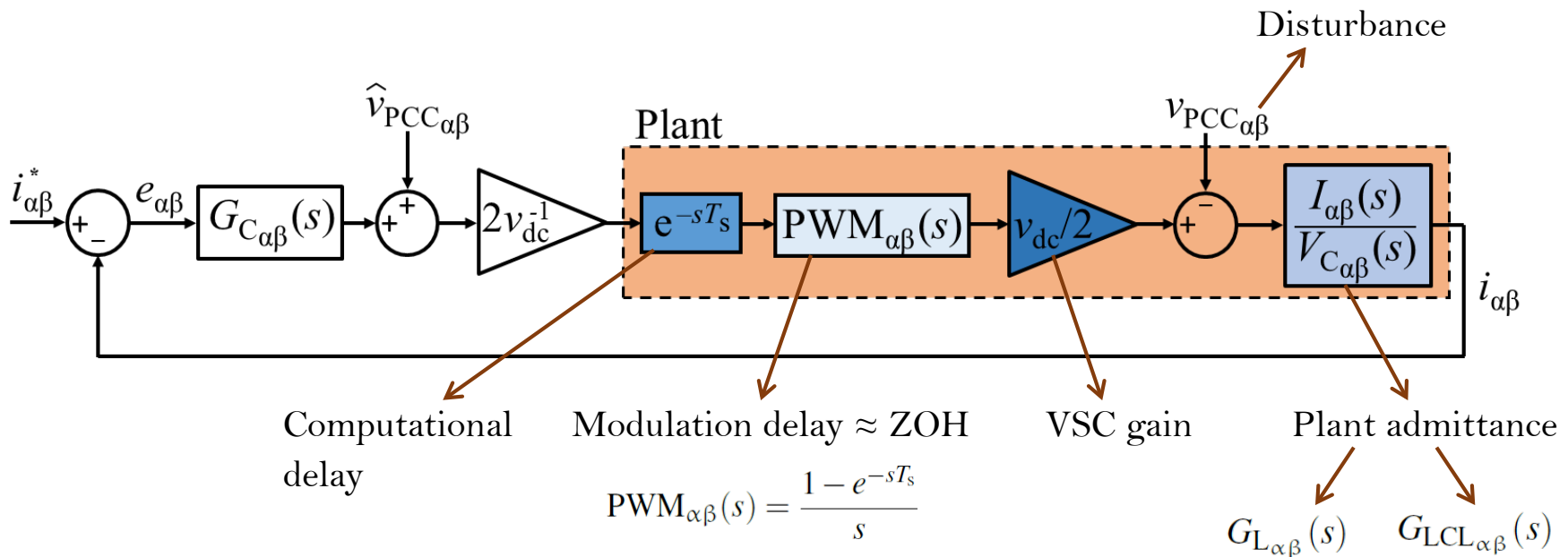
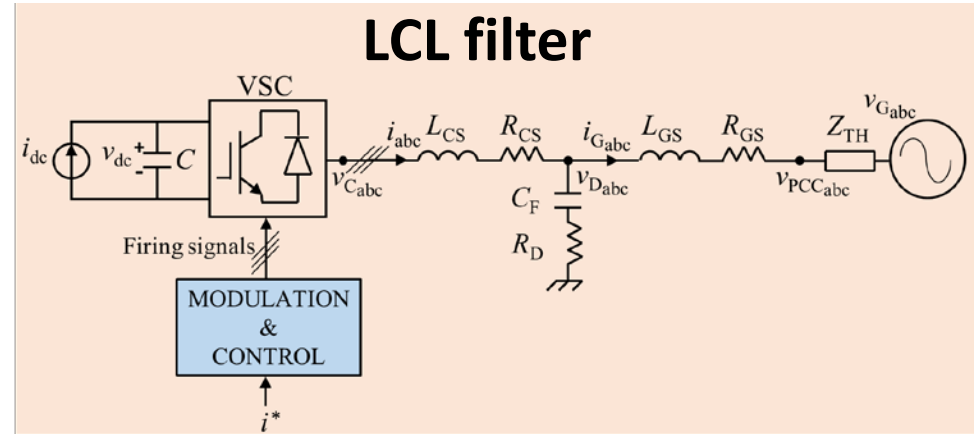
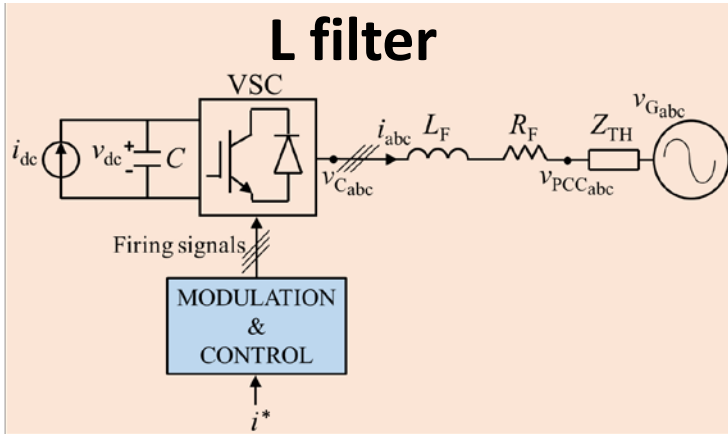
Appropriate controller structure.

Chapters 4 & 5

Rigorous regulator tuning.

Chapter 1: Introduction

# Plant Model for Current-Controlled Grid-Tied VSCs



# Plant Admittance

### L filter

Firing signals

MODULATION & CONTROL

$i^*$

$L = L_F + L_{TH}$

$R = R_F + R_{TH} + R_C$

$$G_{L\alpha\beta}(s) = \frac{I_{\alpha\beta}(s)}{V_{C\alpha\beta}(s)} = \frac{1}{sL + R}$$

$$\frac{I_{\alpha\beta}(s)}{V_{C\alpha\beta}(s)}$$

### LCL filter

Firing signals

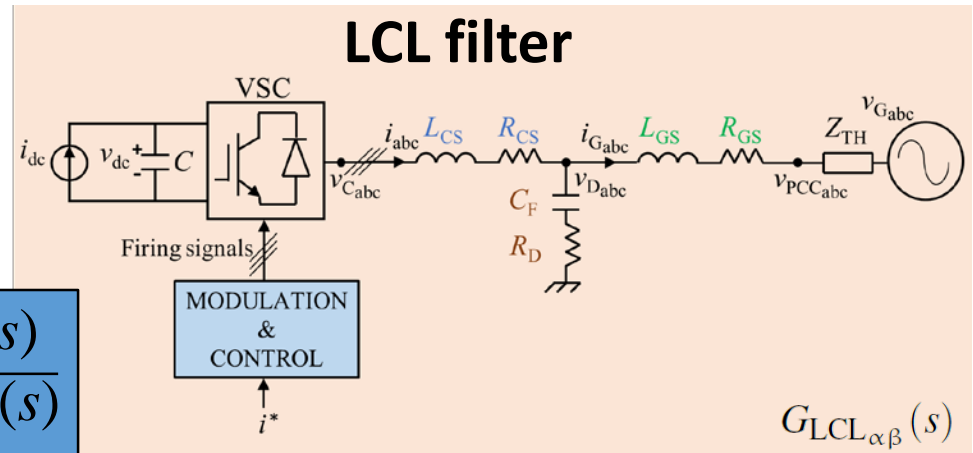
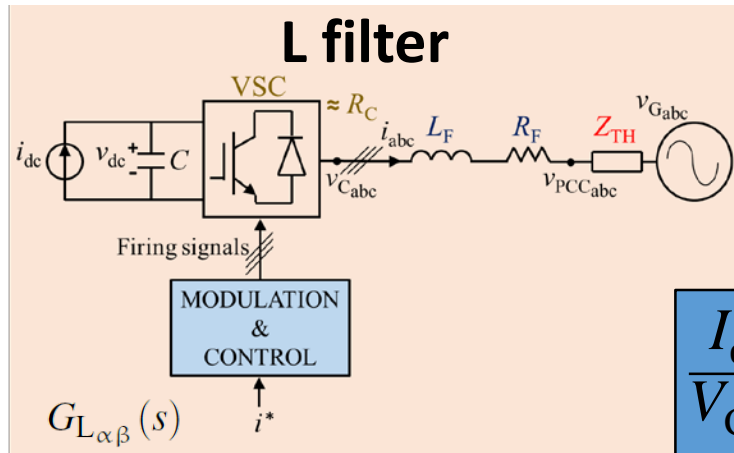
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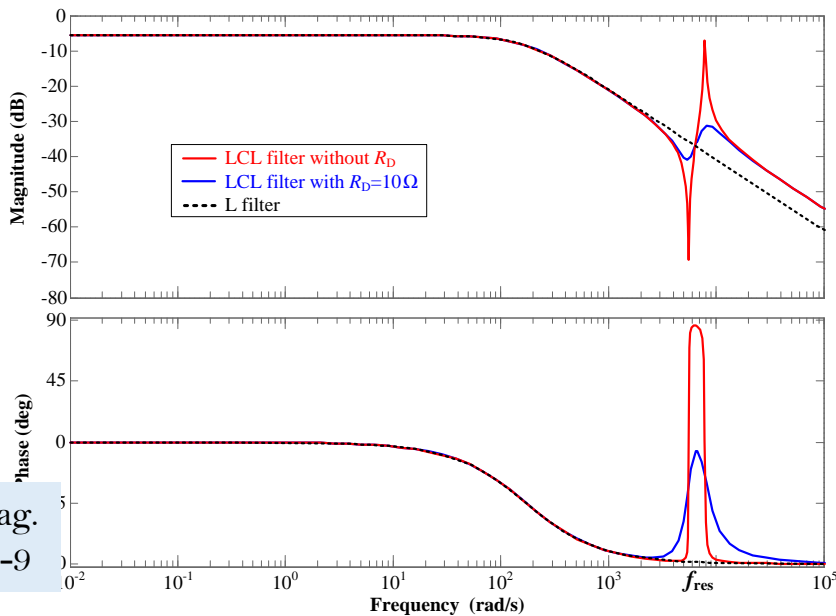
$$G_{LCL\alpha\beta}(s) = \frac{I_{\alpha\beta}(s)}{V_{C\alpha\beta}(s)} = \frac{Y_{CS}(s) [1 + Y_{GS}(s) Z_D(s)]}{1 + Y_{CS}(s) Z_D(s) + Y_{GS}(s) Z_D(s)}$$



# Equivalence Between L and LCL Filters



$$\frac{I_{\alpha\beta}(s)}{V_{C\alpha\beta}(s)}$$

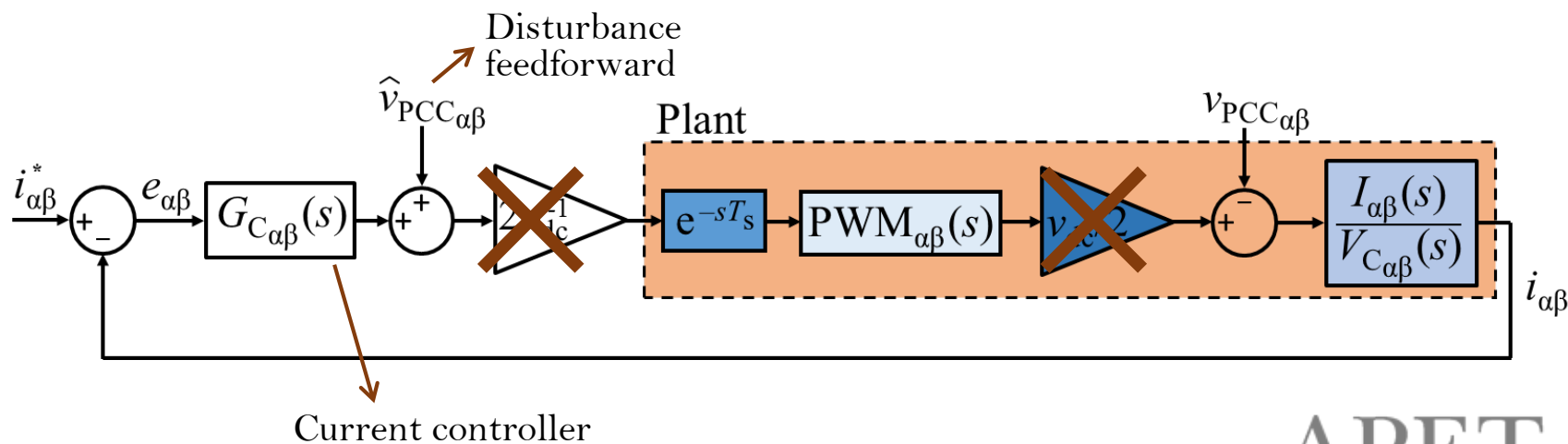
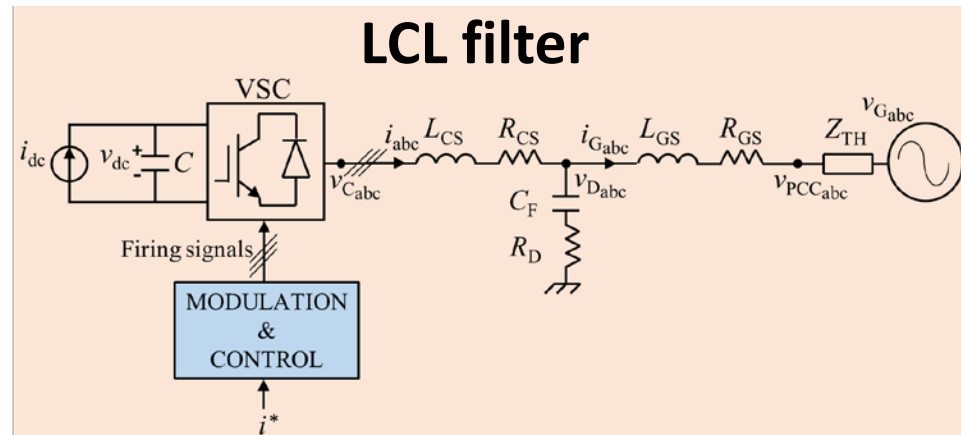
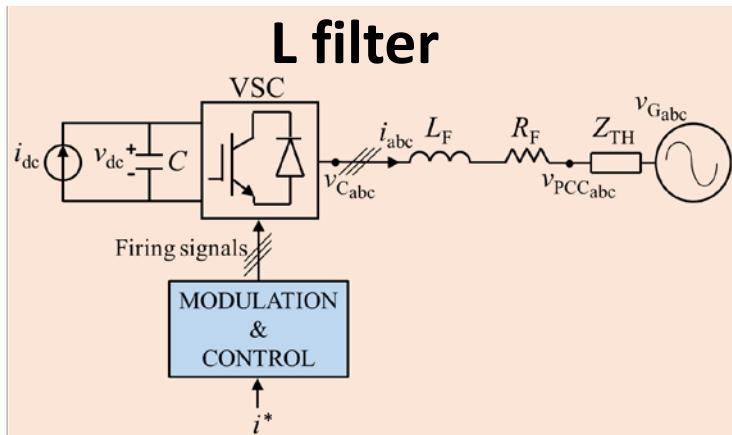


If  $L_F = L_{CS} + L_{GS}$  and  $R_F = R_{CS} + R_{GS}$

LCL filters behave as L ones at frequencies lower than approx.  $f_{res}$ .

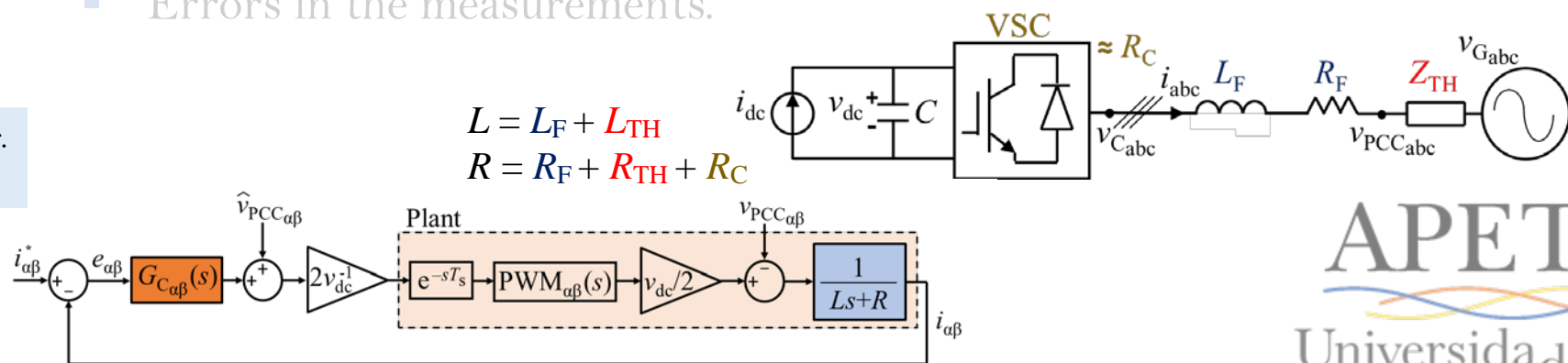
$$G_{L\alpha\beta}(s) \approx G_{LCL\alpha\beta}(s)$$

# Plant Model for Current-Controlled Grid-Tied VSCs



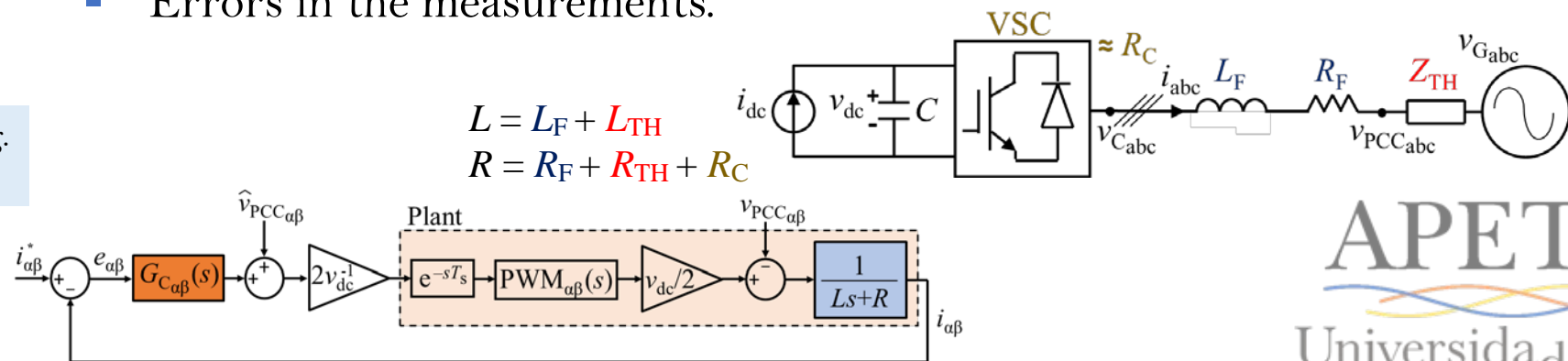
## Parameter Identification

- **Precise knowledge of  $L$  and  $R$  is essential to guarantee the performance of the current loop (particularly when specifications are established in terms of transient response).**
- **Parameter uncertainties.**
  - Non negligible impedance at the PCC.
  - Variation in the value of the different components with the working conditions.
    - Particularly significant in the parameters employed to model the losses (e.g.,  $R_C$ ).
  - Errors in the measurements.



# Parameter Identification

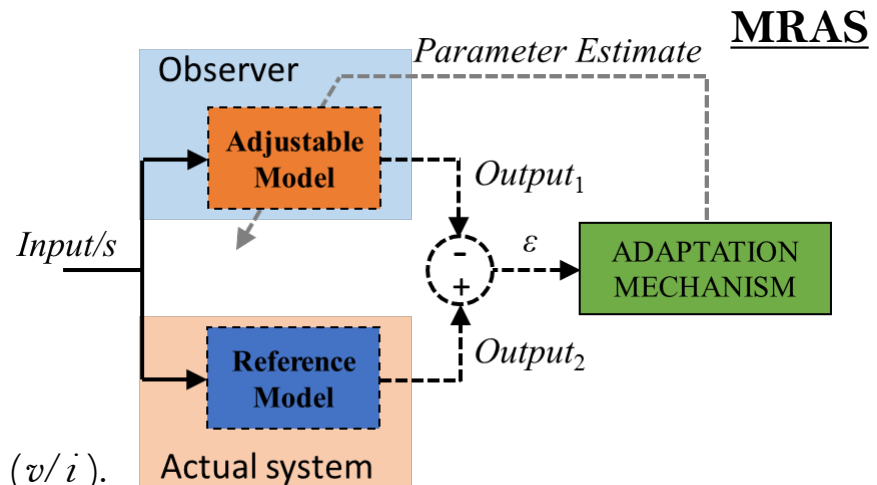
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# Parameter Identification Methods

They can be classified attending to different criteria.

- How they are executed:
  - **online**
  - **offline**
- How they calculate the impedance:
  - **directly** from the **measurements** ( $v/i$ ).
  - **iteratively**, by means of an **adaptive observer**.
    - Iterative minimization of the error (RLS, GPA, EKF, custom-made options....)
    - E.g., recursive closed-loop methods such as MRAS-based solutions.
- Whether they need a source of excitation:
  - NO → **passive**
  - YES → **active** (signal injection, change in the operating conditions...)



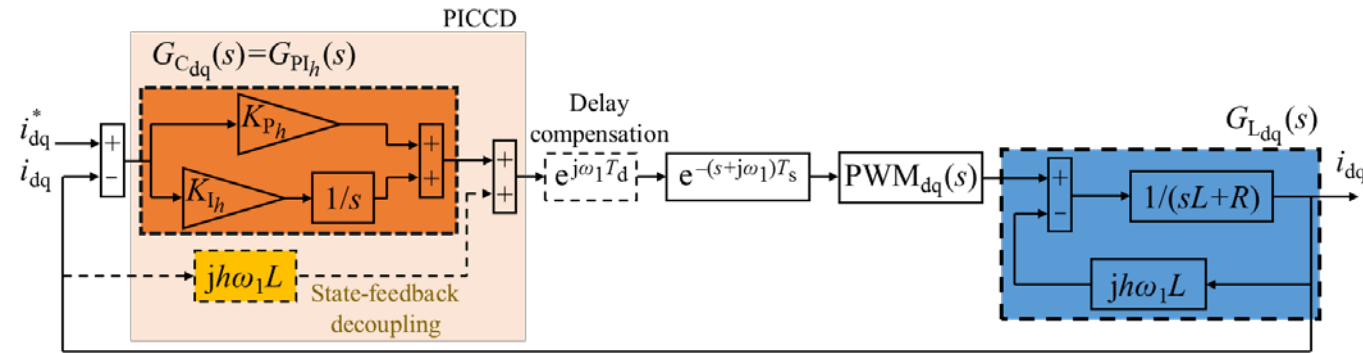
## Parameter Identification Methods

The following observations can be drawn from the available bibliography.

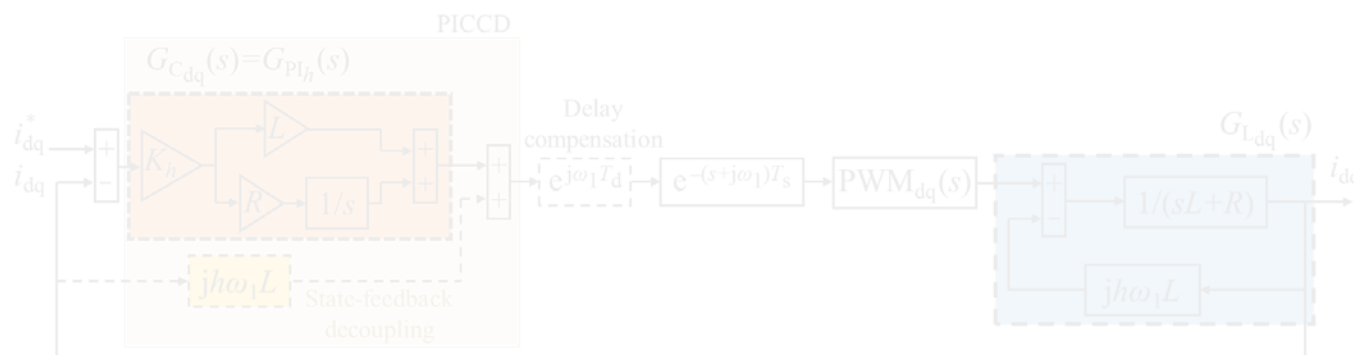
- There is **no previous technique aimed at the converter equivalent loss resistance estimation.**
- **None** of these methods is **oriented to** exactly the same objective as the one sought in this thesis: **an accurate analysis and design of current loop transient response in grid-tied VSCs.**

# PI Controllers in SRF

- One of the most extended solutions.



**Classical PI**  
controller with cross-coupling decoupling (PICCD)

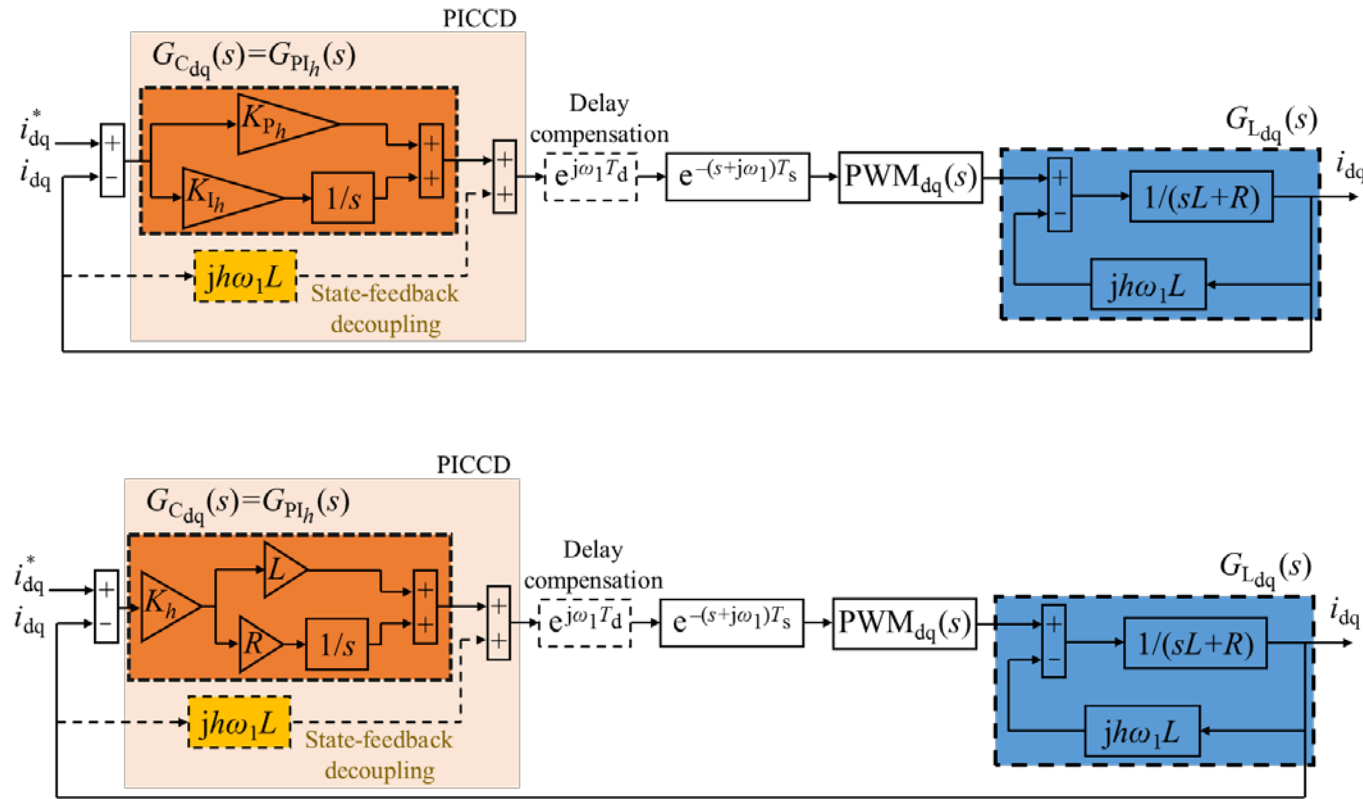


Tuned according to IMC



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## Resonant Controllers in Stationary Frame

(Vs PI Controllers in SRF)

- ✓ Open-loop **infinite gain** at the **resonant frequency** → ac currents can be regulated **in stationary frame** with **zero steady-state error**,
  - ✓ **reducing the computational burden** (Park transformations can be avoided),
  - ✓ showing **lower sensitiveness to errors and noise in synchronization**.
  
- ✓ Ability to regulate **positive- and negative-sequence components of the same harmonic order** ← equivalence to two identical PI regulators implemented in two SRF's simultaneously (one positive and one negative).
  
- ✗ **Complex schemes for distortion-free saturation**.
  
- ✗ **Great sensitiveness of their resonant frequency to the discretization technique**.

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# PR Controllers

## Proportional gain:

- Influences: phase margin and  $f_{\text{crossover}}$ .
- Selection: well-established rules.

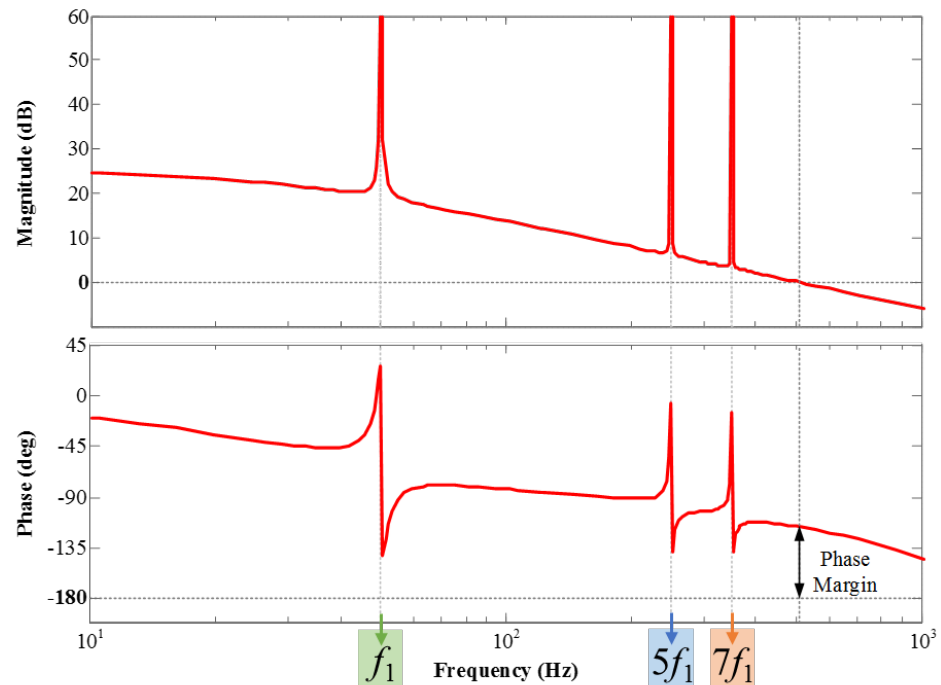
## Integral gain:

- Influences: bandwidth around  $hf_1$ .
- Selection: guidelines (selectivity Vs fast dynamics).



- × Qualitative guidelines.
- × Ignoring the delay.
- × Not aimed at the optimization of the disturbance rejection transient response.

$$G_{\text{PR}}(s) = K_{\text{PT}} + \sum_{h=1,5,7,\dots} K_{\text{I}h} \frac{s}{s^2 + h^2\omega_1^2}$$



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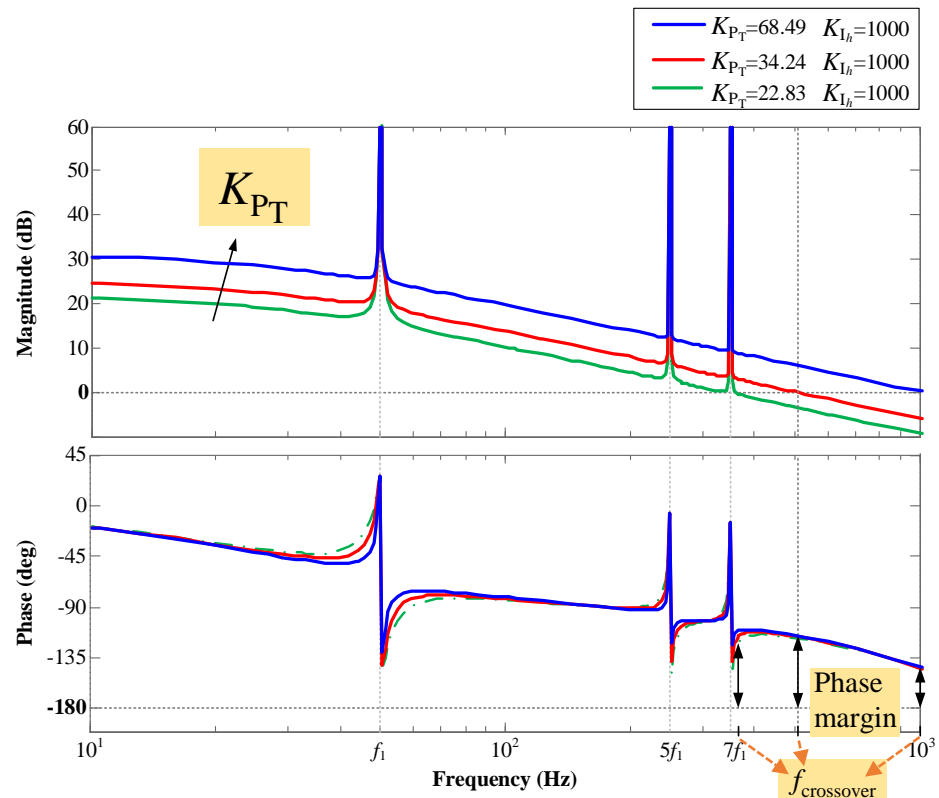
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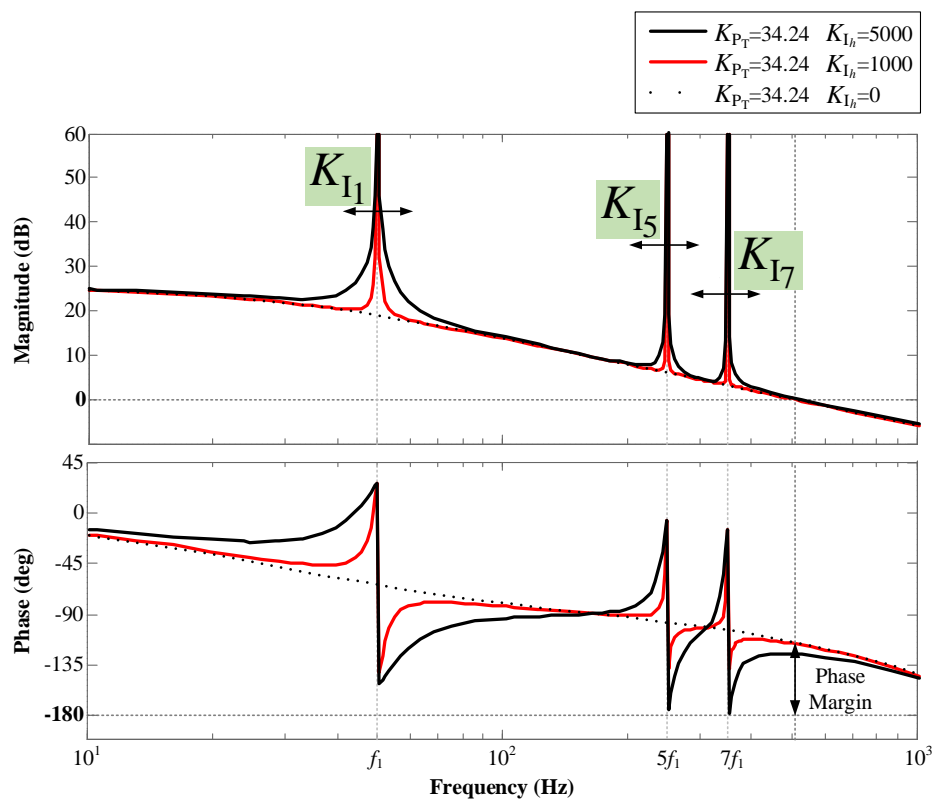
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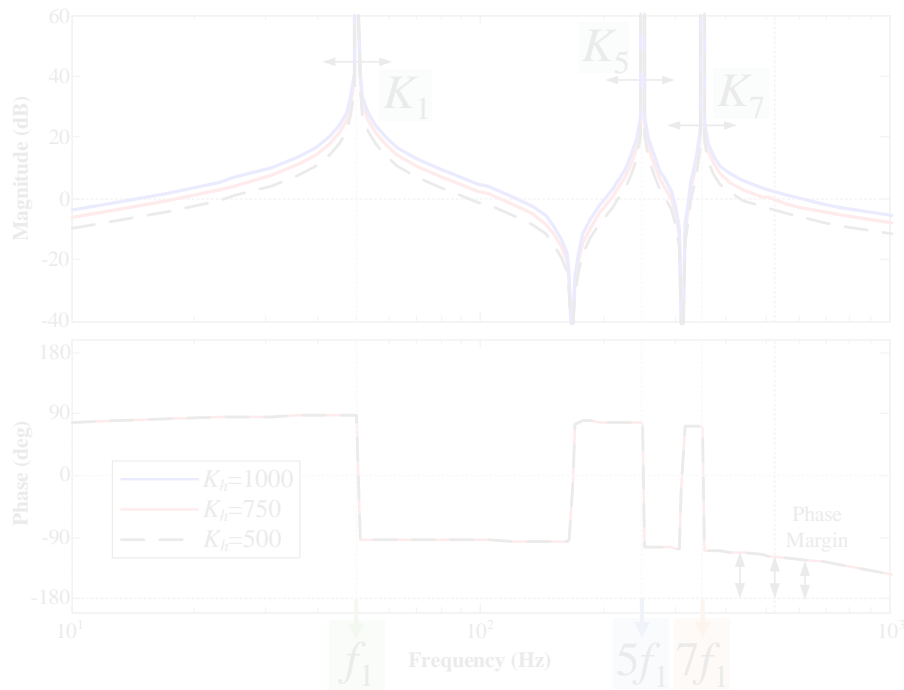
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# VPI Controllers

$$G_{VPI_h}(s) = \frac{s^2 K_{Ph} + s K_{Ih}}{s^2 + h^2 \omega_1^2} \xrightarrow{\text{IMC}} G_{VPI_h}(s) = K_h \frac{s(sL + R)}{s^2 + h^2 \omega_1^2}$$



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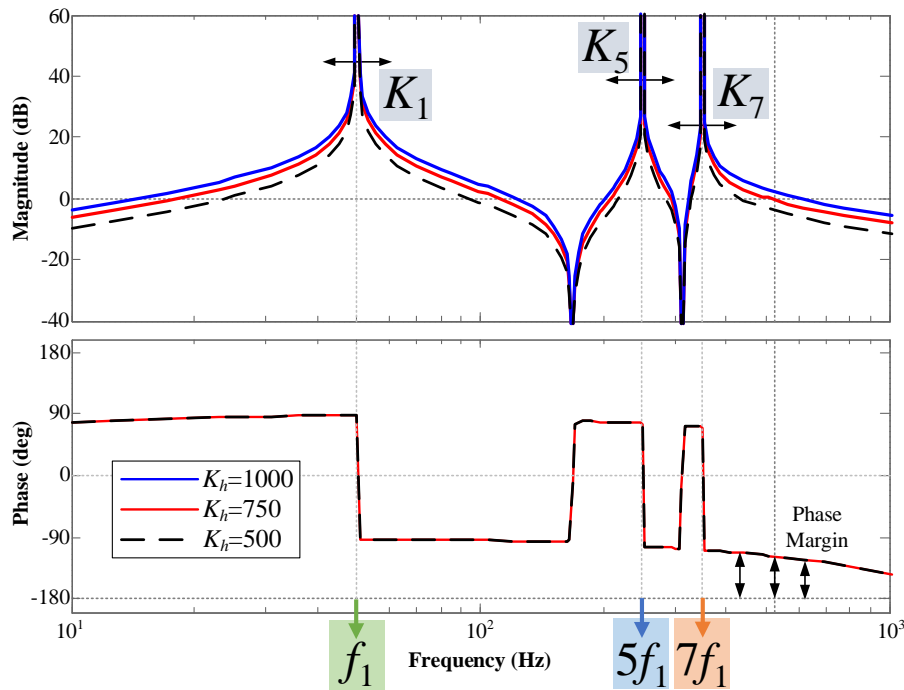


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### Chapters 2 & 3

- Plant **parameter identification methods** oriented to transient response optimization.

### Chapters 4 & 5

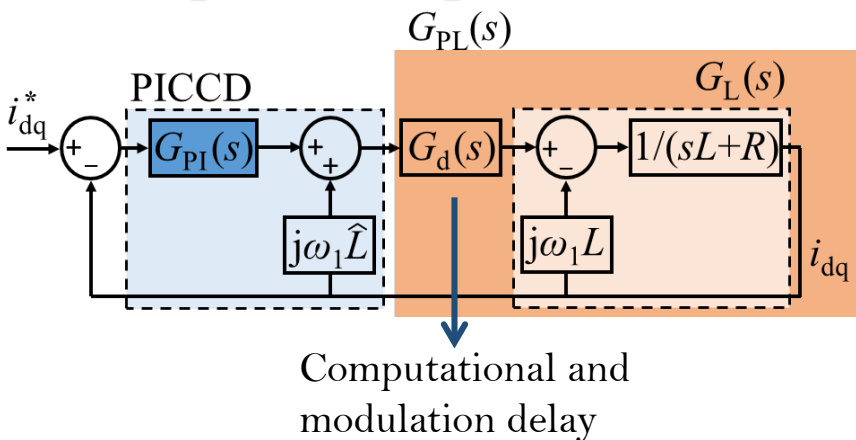
- Accurate **tuning methods** for resonant controllers oriented to transient response optimization (command tracking and disturbance rejection).
- **Comparison** between **PR** and **VPI** controllers (transient response and THD).

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2. Equivalent Loss Resistance Estimation of Grid-Tied Converters for Current Control Analysis and Design
  - Analysis of the Current Closed-Loop Step Response
  - Developed Identification Method of the VSC Equivalent Loss Resistance
  - Experimental Results
  - Conclusion
3. A Method for Identification of the Equivalent Inductance and Resistance in the Plant Model of Current-Controlled Grid-Tied Converters
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# Open-Loop Transfer Function



Neglecting  $G_d(s)$  & assuming  $\hat{L} = L$

$$G_{OL}(s) = G_{PI}(s) \frac{1}{sL+R} = \frac{sK_P + K_I}{s} \frac{1}{sL+R}$$

where  $\begin{cases} R = R_F + R_C \\ L = L_F \end{cases}$

**IMC**  
 $K_P/K_I = \hat{L}/\hat{R}$   
 $K_P = K\hat{L}$

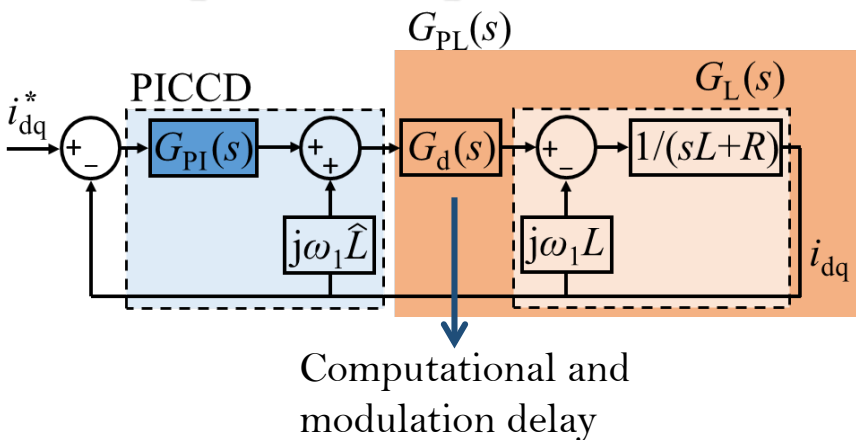
If  $\begin{cases} \hat{R} = R \\ \& \\ \hat{L} = L \end{cases} \Rightarrow G'_{OL}(s) = K \frac{1}{s}$

If  $\begin{cases} \hat{R} \neq R \\ \& \\ \hat{L} = L \end{cases} \Rightarrow G''_{OL}(s) = K \frac{sL + \hat{R}}{sL + R} \frac{1}{s}$

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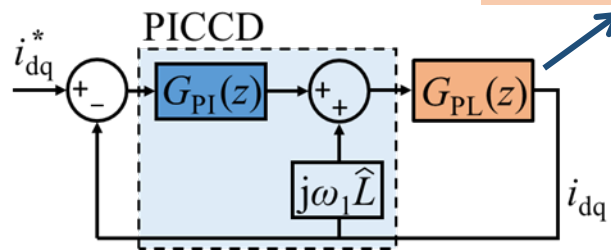
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Including  $G_d(s)$



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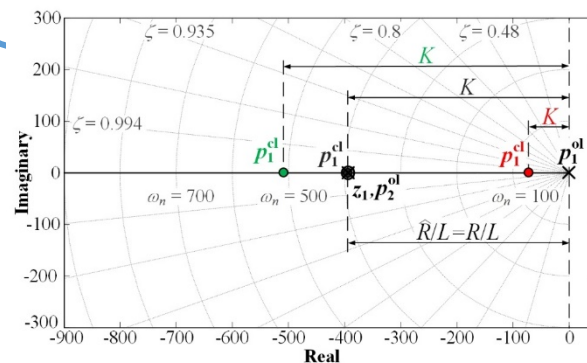
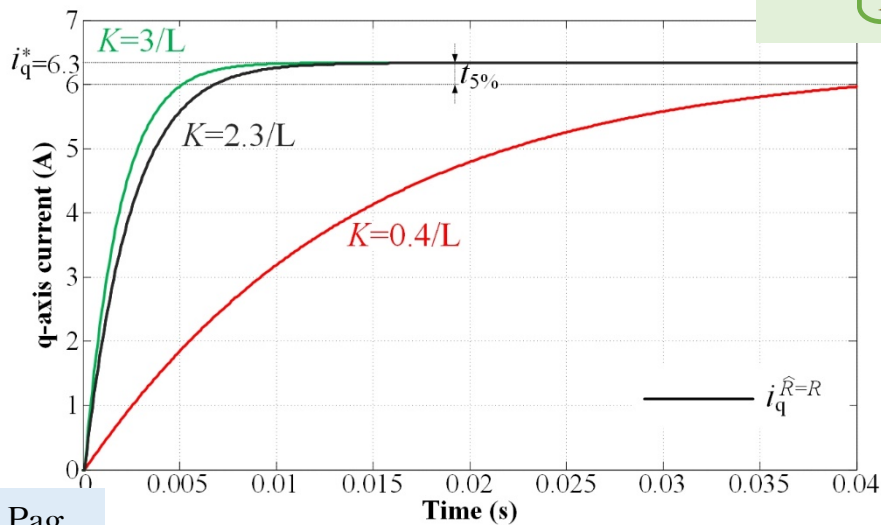
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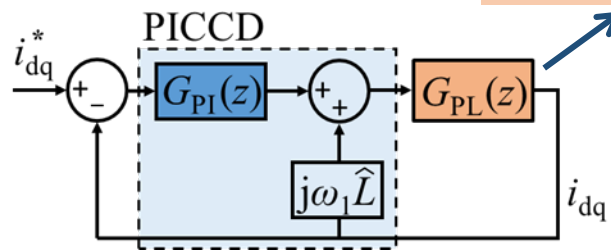
Correct identification of  $R$

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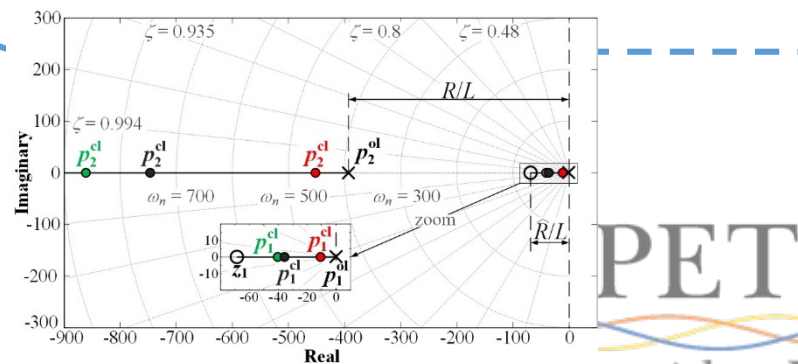
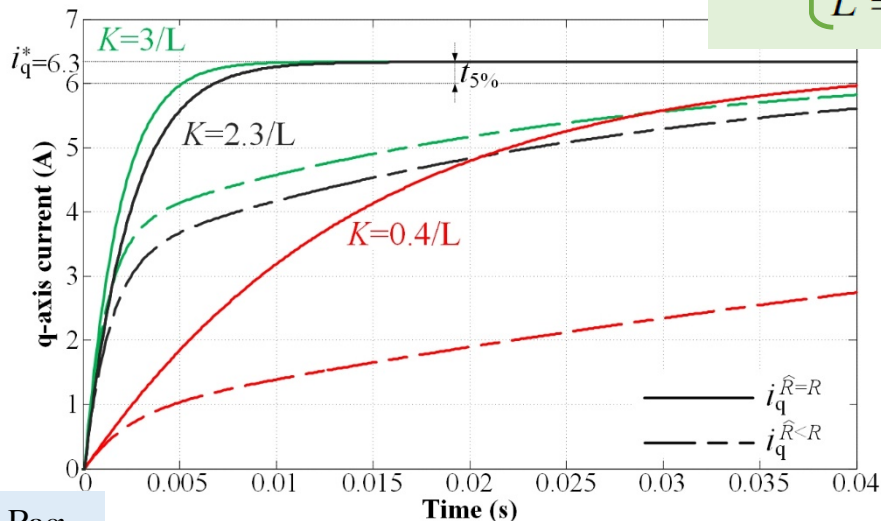
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Underestimation of  $R$

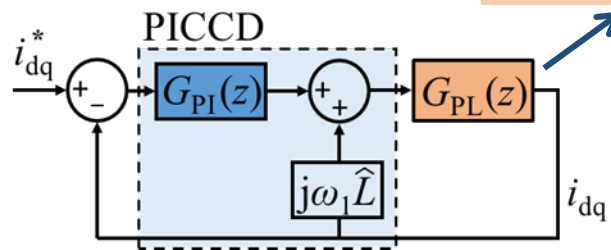
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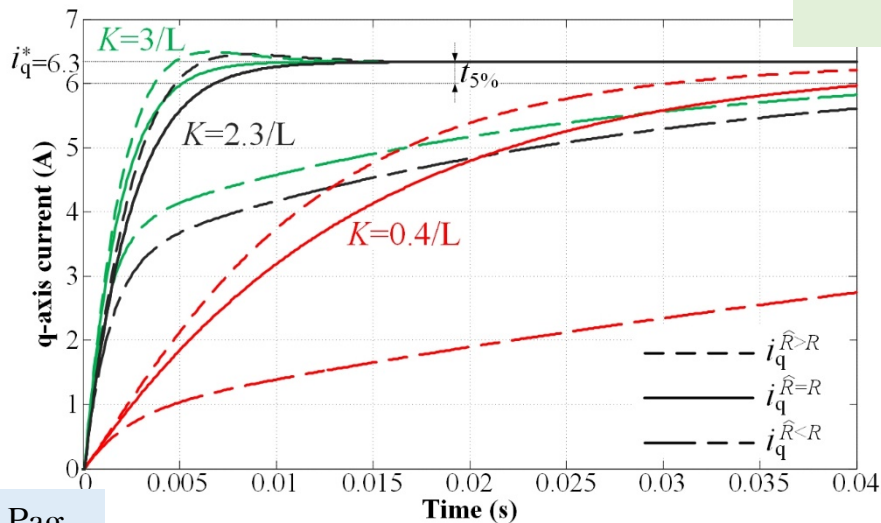
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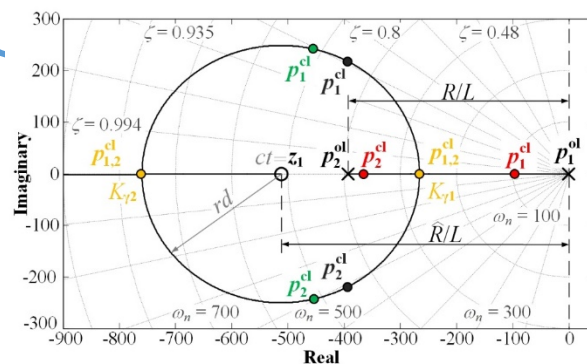
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Overestimation of  $R$



If  $\left\{ \begin{array}{l} \hat{R} > R \\ \& \\ \hat{L} = L \end{array} \right.$

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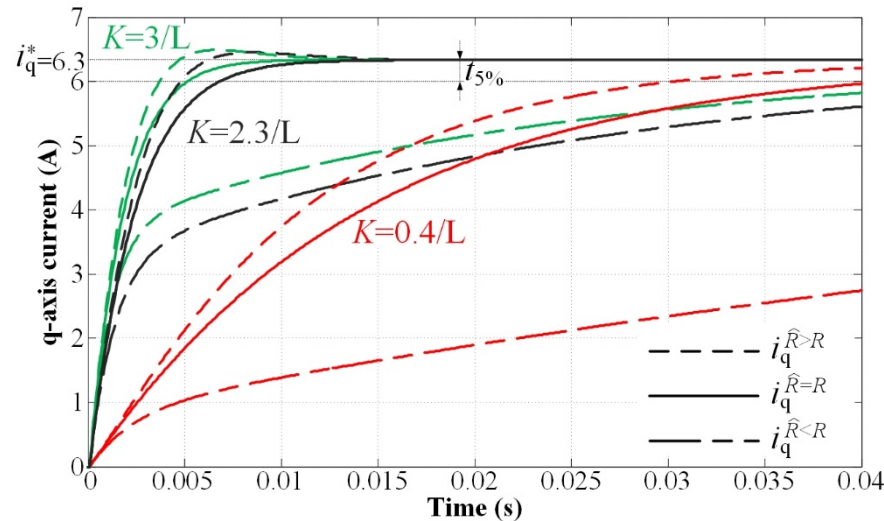


# Current Step Response in the Discrete-Time Domain

From the step response, having  $i_q^{\hat{R}=R}$  as a target, **two indicators** can be used to identify the actual  $R$ :

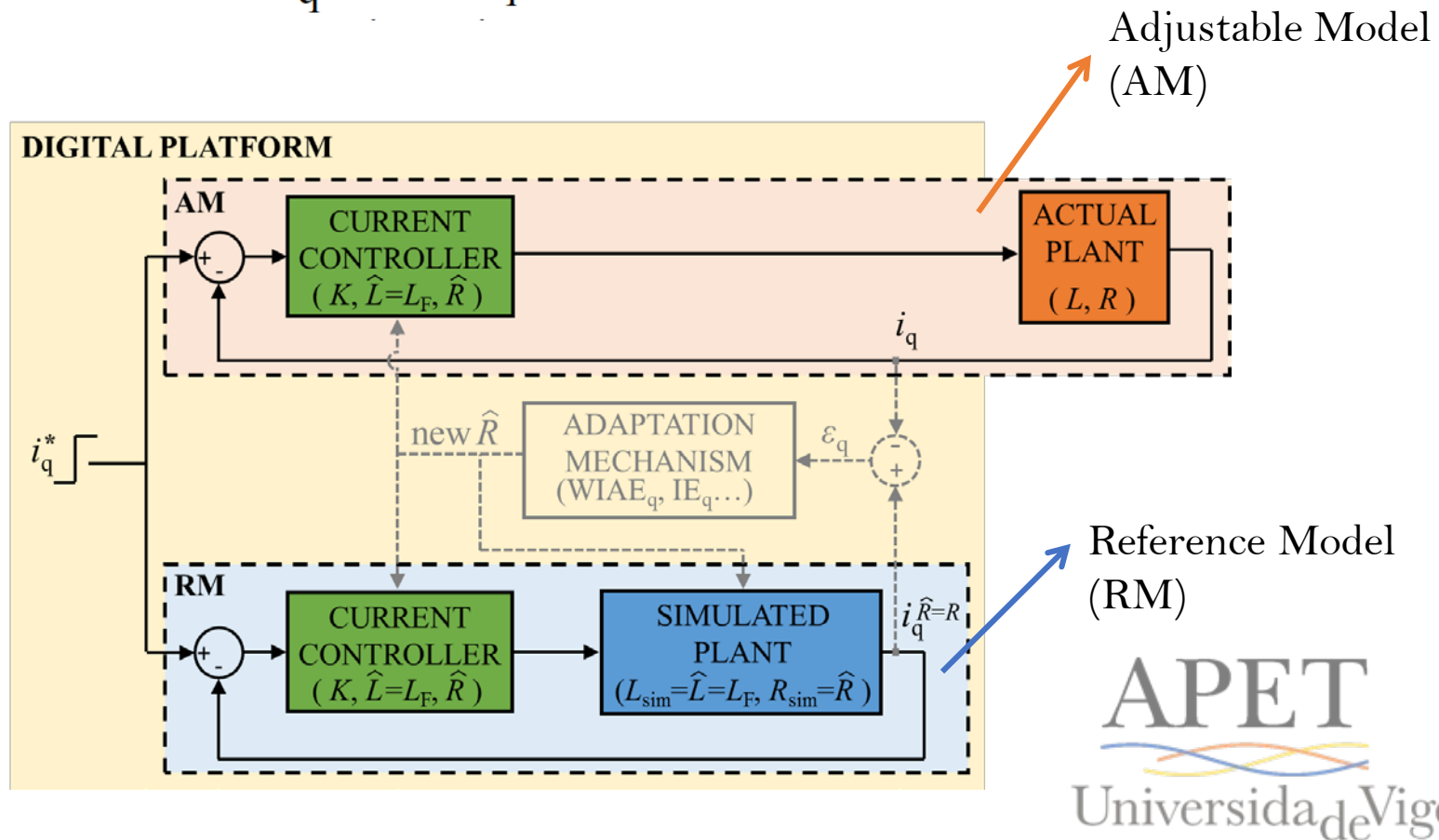
- the sign of the error area (**IE**) → whether  $R$  is **under** or **overestimated**,
- the area (**IAE**) → **how large** is the  $R$  **mismatch**

needs to be modified to weight the underestimate and overestimate cases  
 → **WIAE**.



## Developed Method

- **MRAS-based** technique. Iterative process.
- If  $\hat{R} \approx R \iff i_q^{\hat{R}=R} \approx i_q$



# Developed Method

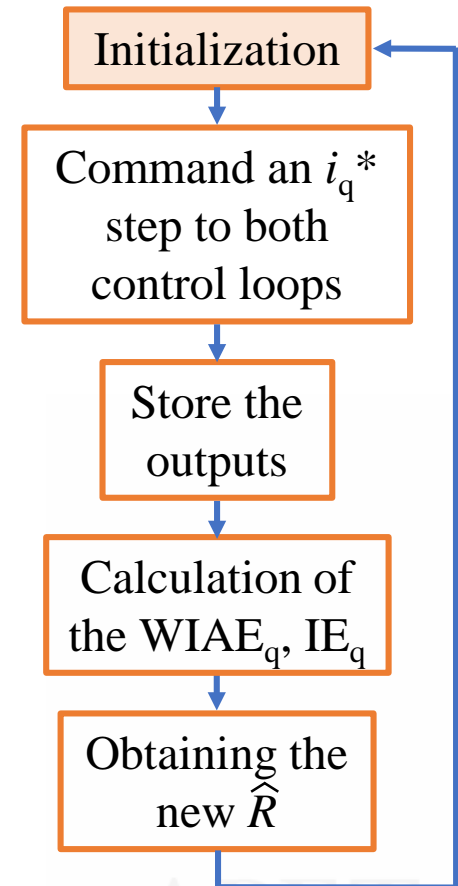
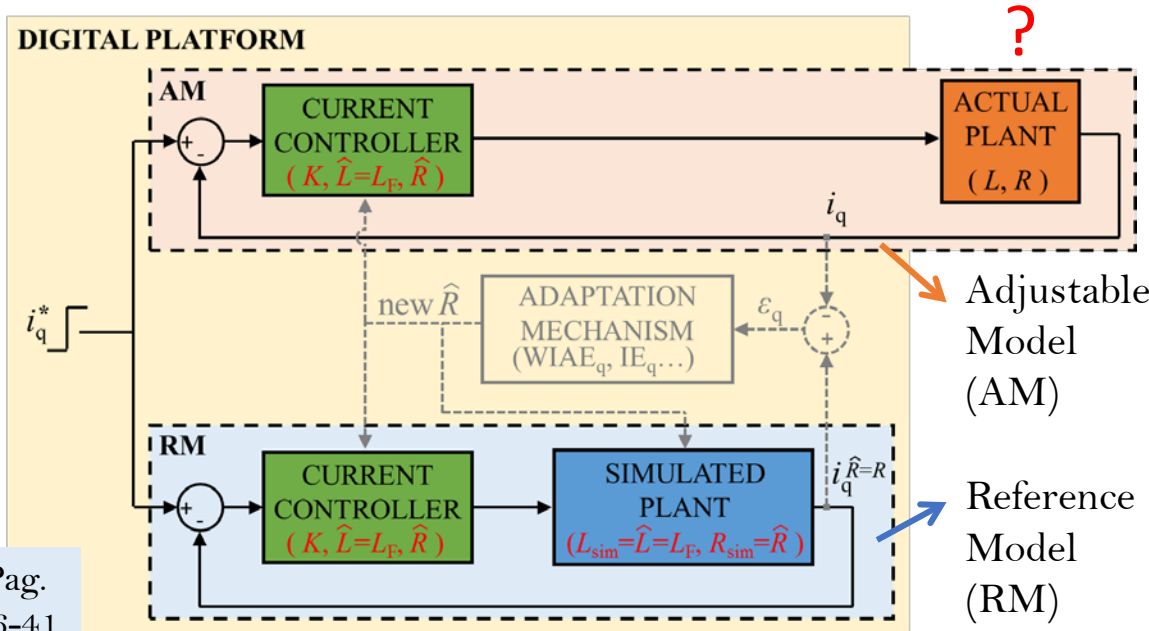
## 1. Initialization

- Auxiliary variables
- Controller parameters

$$\hat{R}(1), \hat{L}=L_F, K(k)=\hat{R}(k)/L_F$$

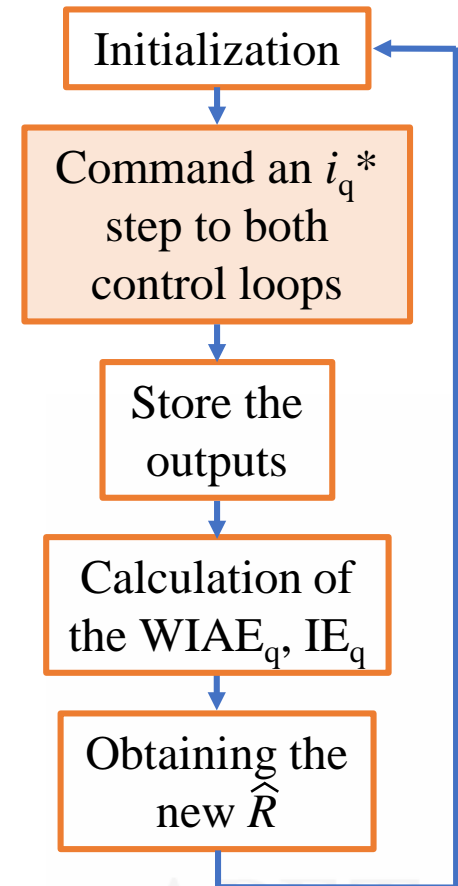
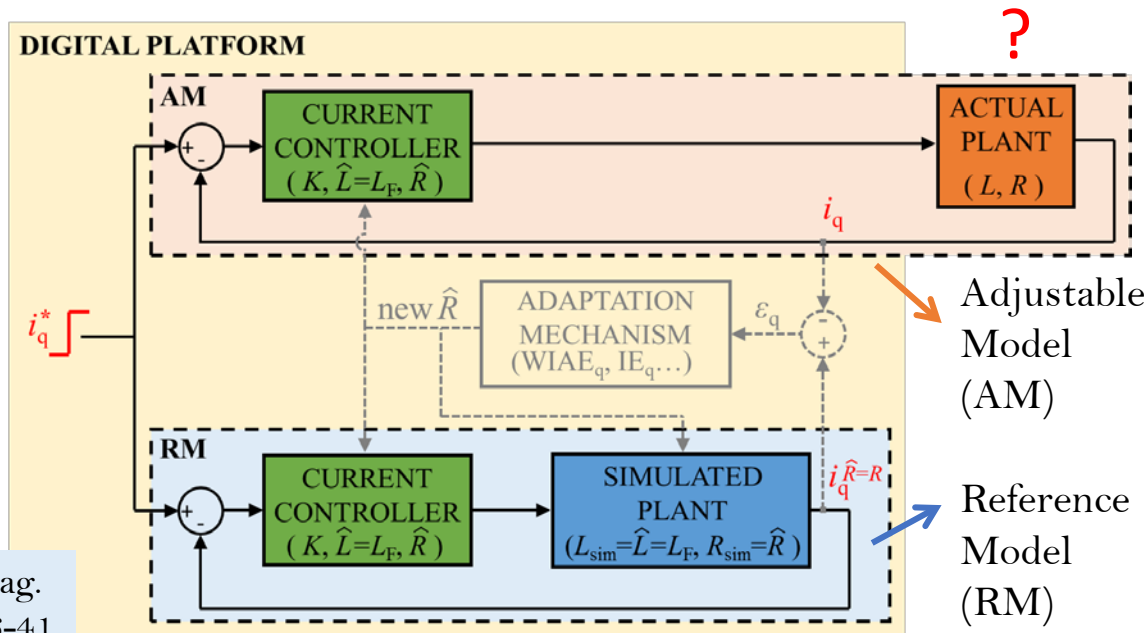
- Simulated plant parameters

$$L_{sim}=L_F, R_{sim}(k)=\hat{R}(k)$$



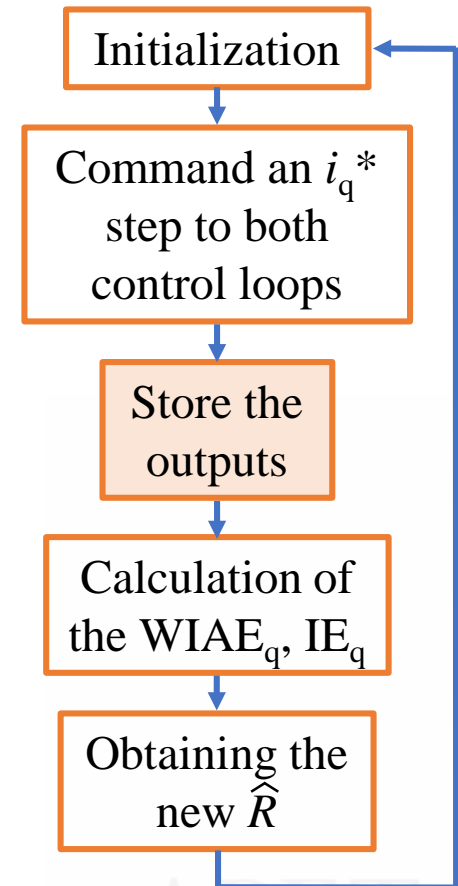
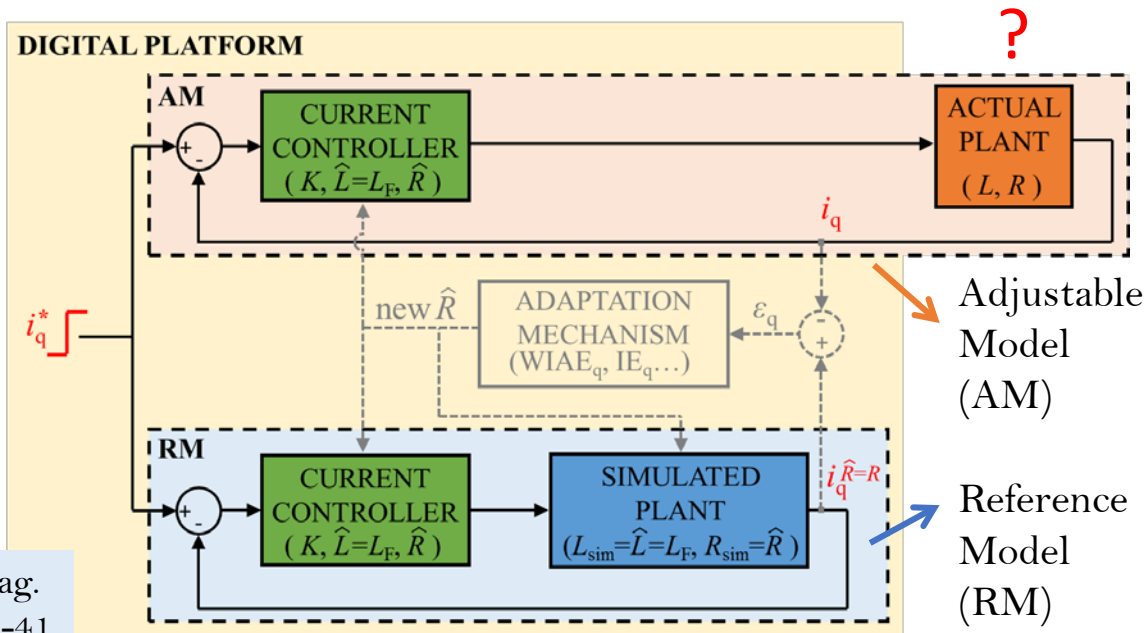
# Developed Method

2. Command an  $i_q^*$  step to both loops at the same time.
3. Store the outputs  $i_q$  and  $i_q^{\hat{R}=R}$ .



## Developed Method

2. Command an  $i_q^*$  step to both loops at the same time.
3. Store the outputs  $i_q$  and  $i_q^{\hat{R}=R}$ .

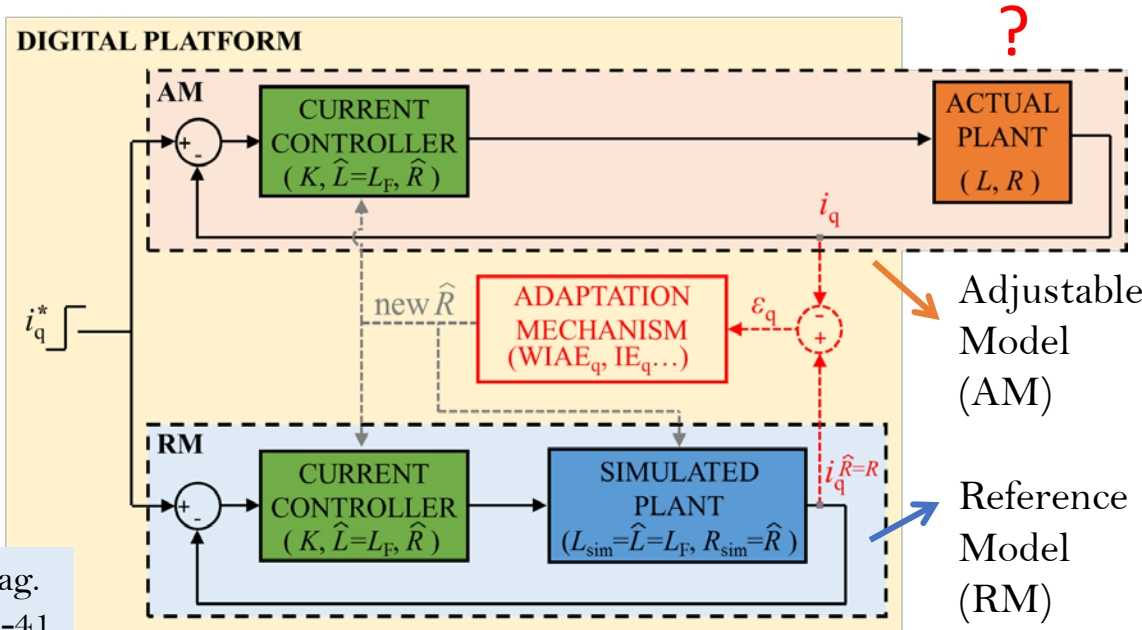


# Developed Method

4. Calculation of two indicators ( $WIAE_q, IE_q$ ) from the error between the two curves.

5. Obtaining the new  $R$  estimate:

▪  $WIAE_q, IE_q \rightarrow \hat{R}$



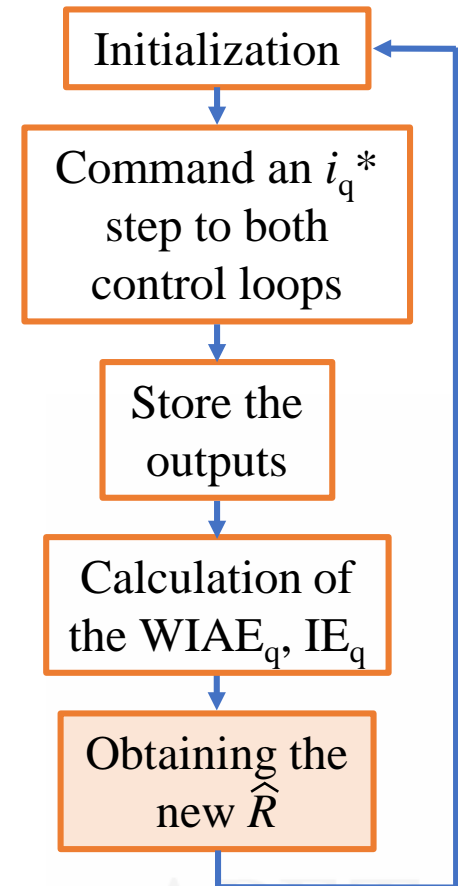
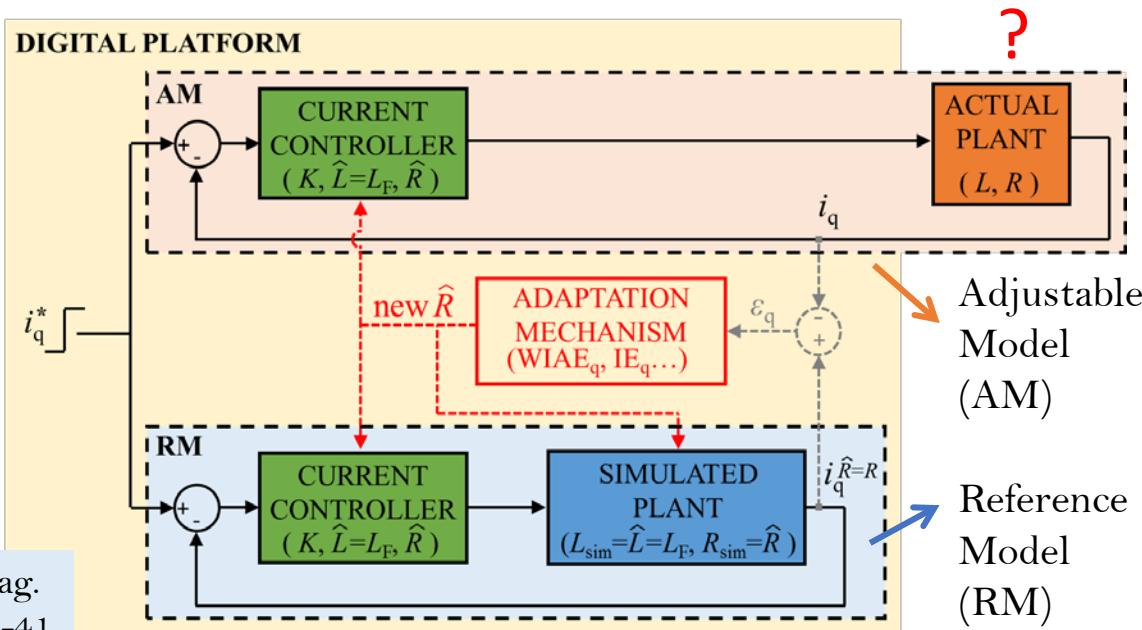
```

graph TD
    A[Initialization] --> B[Command an  $i_q^*$  step to both control loops]
    B --> C[Store the outputs]
    C --> D[Calculation of the  $WIAE_q, IE_q$ ]
    D --> E[Obtaining the new  $\hat{R}$ ]
    E --> A
    
```



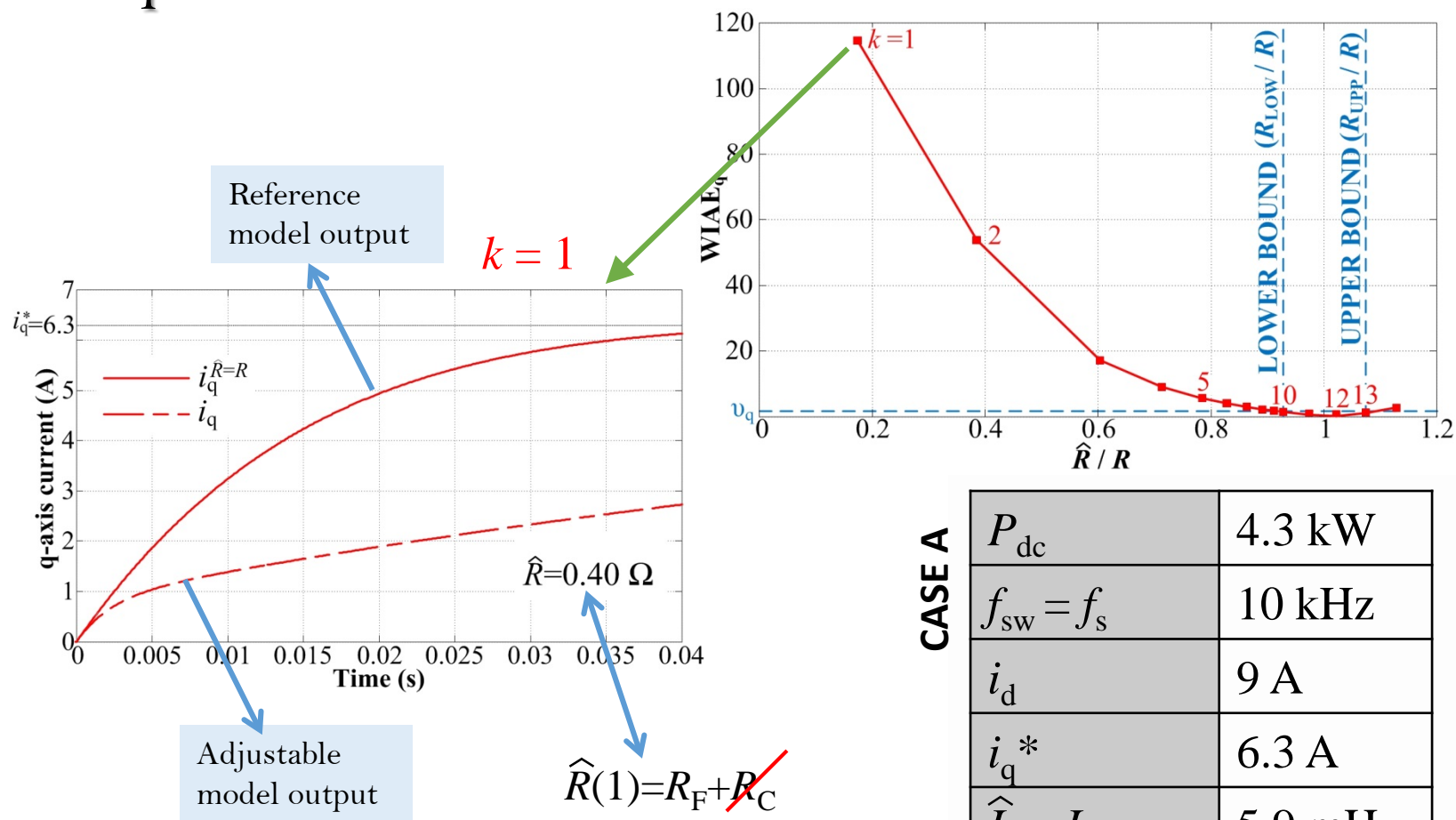
# Developed Method

4. Calculation of two indicators ( $WIAE_q$ ,  $IE_q$ ) from the error between the two curves.
5. Obtaining the new  $R$  estimate:
  - $WIAE_q, IE_q \rightarrow \hat{R}$





# Developed Method

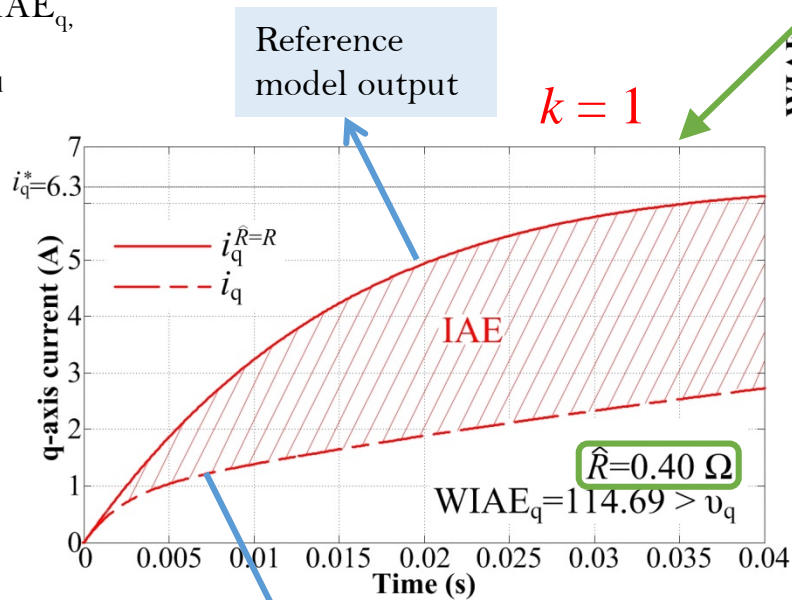


<b>CASE A</b>	$P_{dc}$	4.3 kW
	$f_{sw} = f_s$	10 kHz
	$i_d$	9 A
	$i_q^*$	6.3 A
	$\hat{L} = L_F$	5.9 mH
	$\hat{R} (R_F+R_C)$	2.3 $\Omega$
	$\hat{R}(1) = R_F$	0.4 $\Omega$

# Developed Method

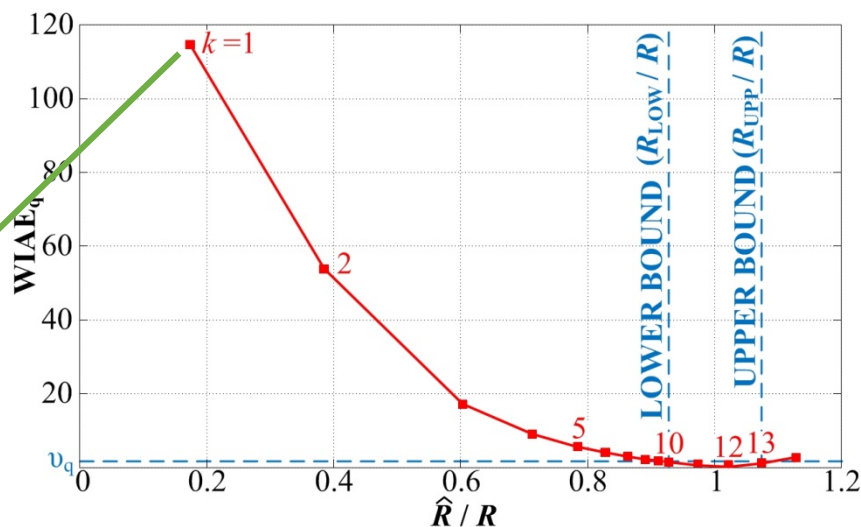
- Main idea:** using the area between both curves to correct the  $R$  mismatch.

- WIAE<sub>q</sub>,
- IE<sub>q</sub>



$R$	$2.3 \Omega$
-----	--------------

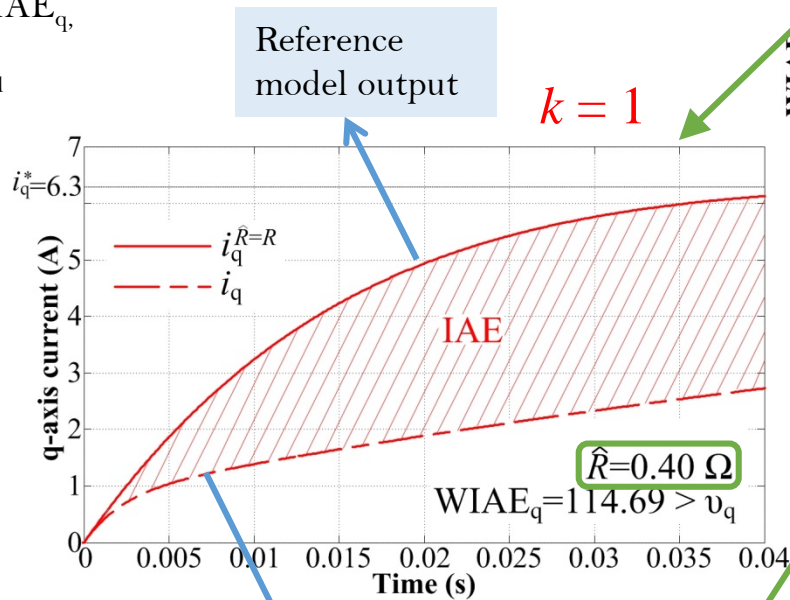
Adjustable model output



# Developed Method

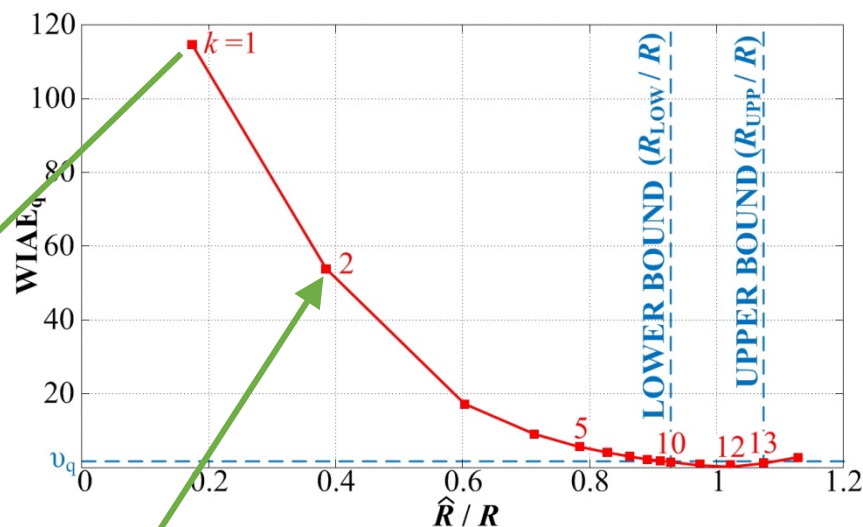
- Main idea:** using the area between both curves to correct the  $R$  mismatch.

- WIAE<sub>q</sub>,
- IE<sub>q</sub>



$R$	$2.3 \Omega$
-----	--------------

Adjustable model output



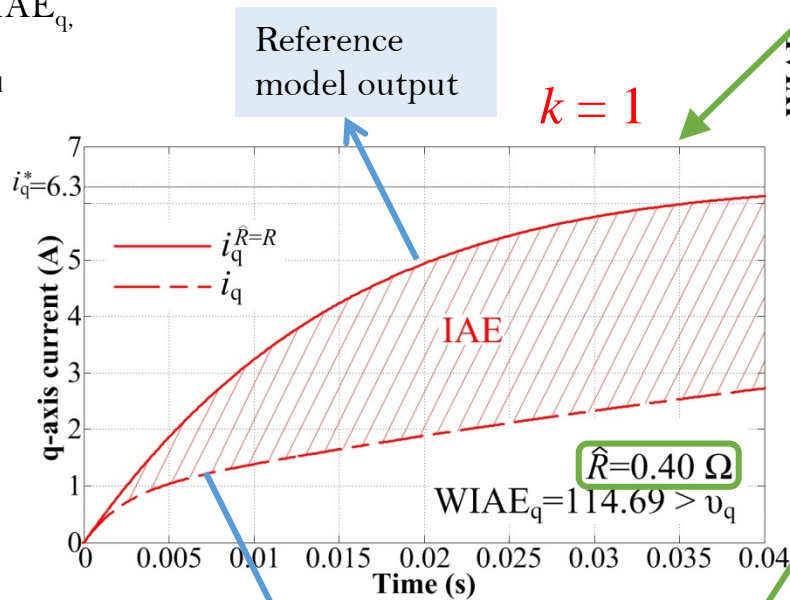
$$\hat{R}(k+1) = [1 + \Delta_q(k)] \cdot \hat{R}(k)$$

$$\Delta_q(k) = f(\text{WIAE}_q(k), i_q^*)$$

# Developed Method

- Main idea:** using the area between both curves to correct the  $R$  mismatch.

- WIAE<sub>q</sub>,
- IE<sub>q</sub>

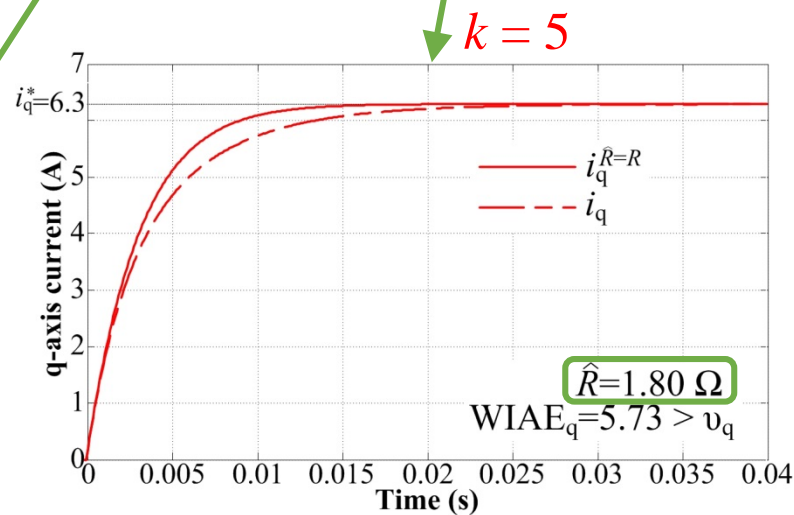
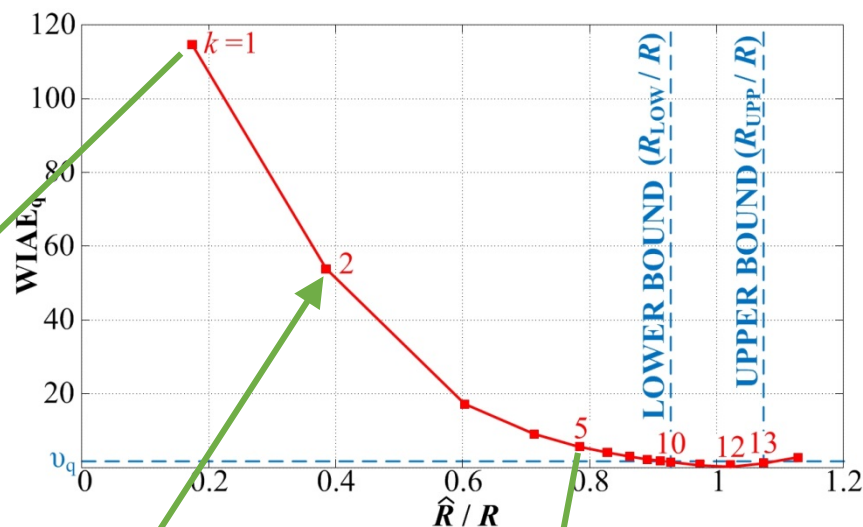


$R$	$2.3 \Omega$
-----	--------------

Adjustable model output

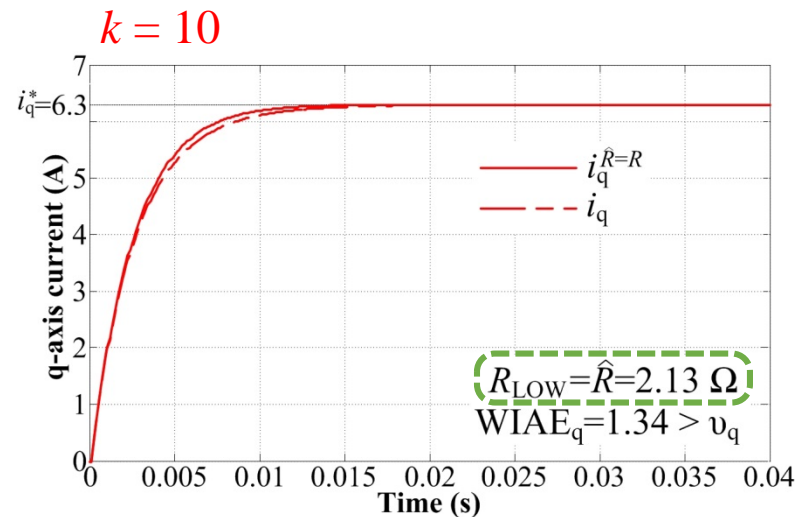
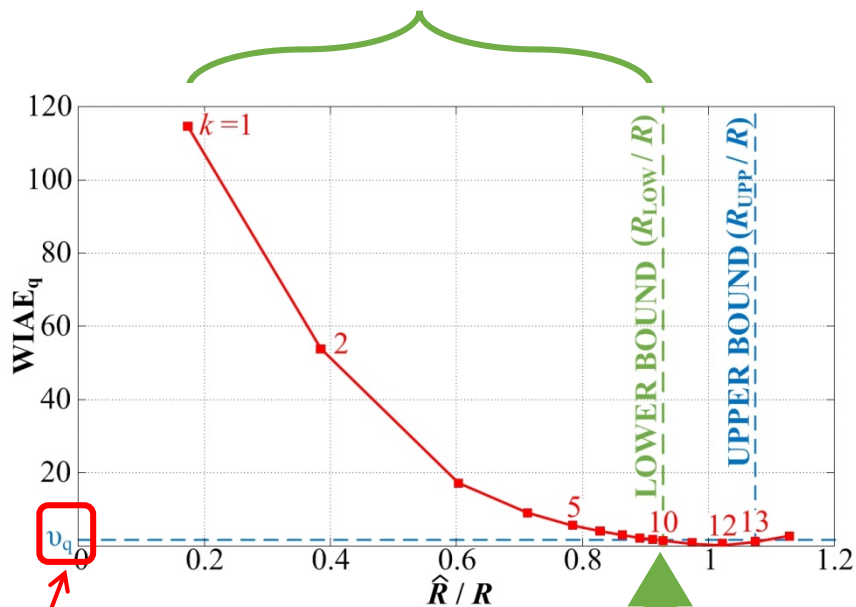
$$\hat{R}(k+1) = [1 + \Delta_q(k)] \cdot \hat{R}(k)$$

$$\Delta_q(k) = f(\text{WIAE}_q(k), i_q^*)$$



# Developed Method

## Approach to $R$ lower bound

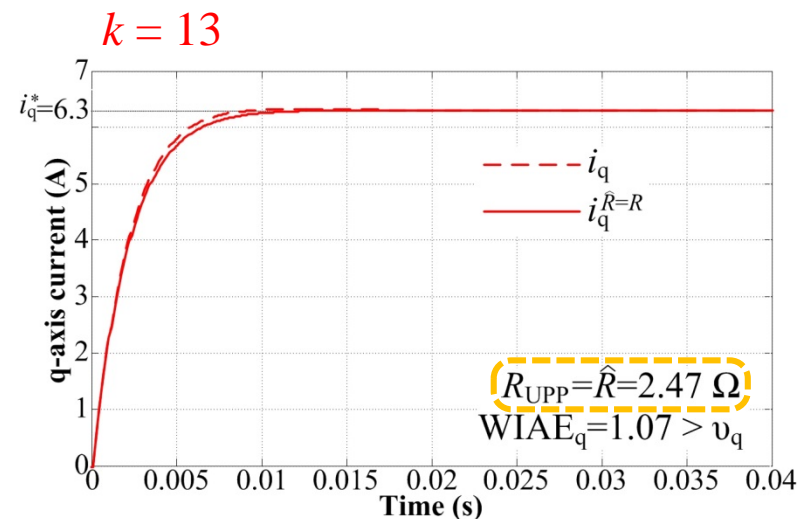
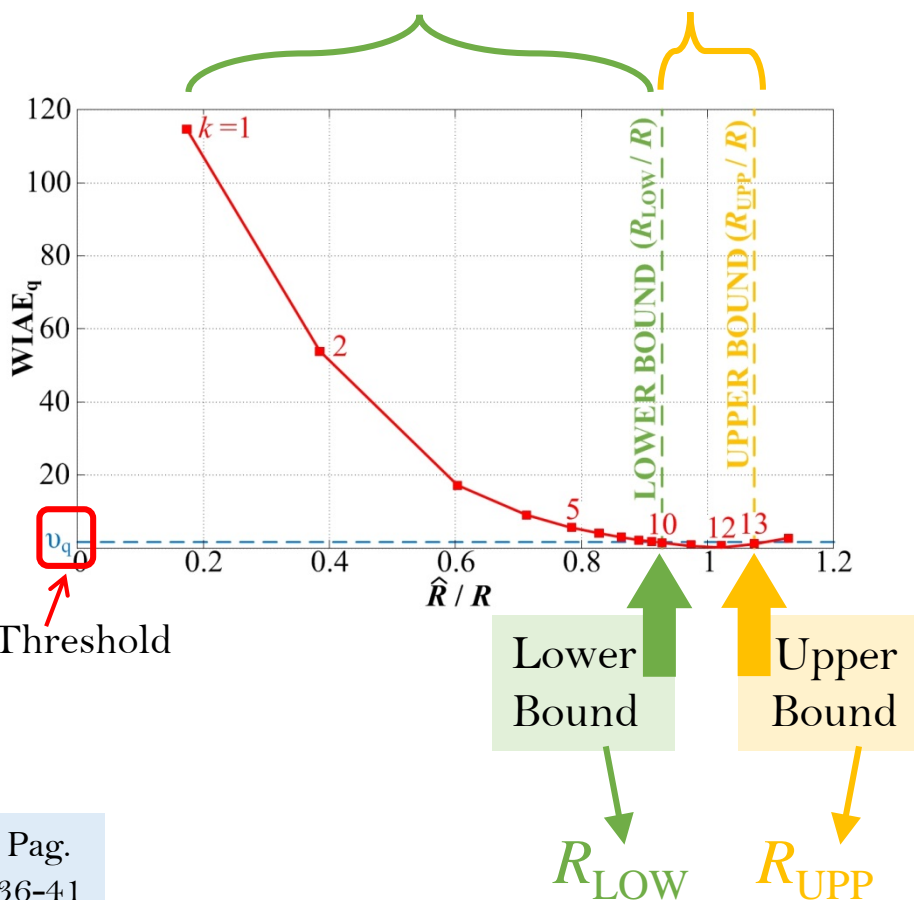


$R_{LOW}$



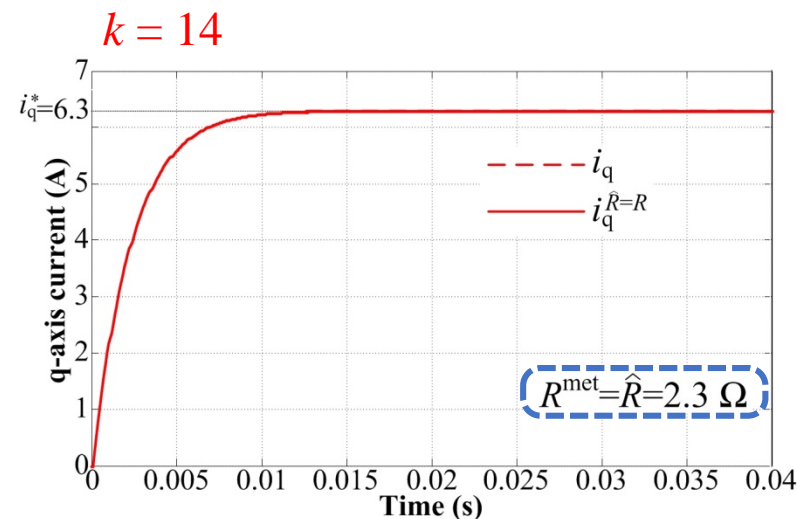
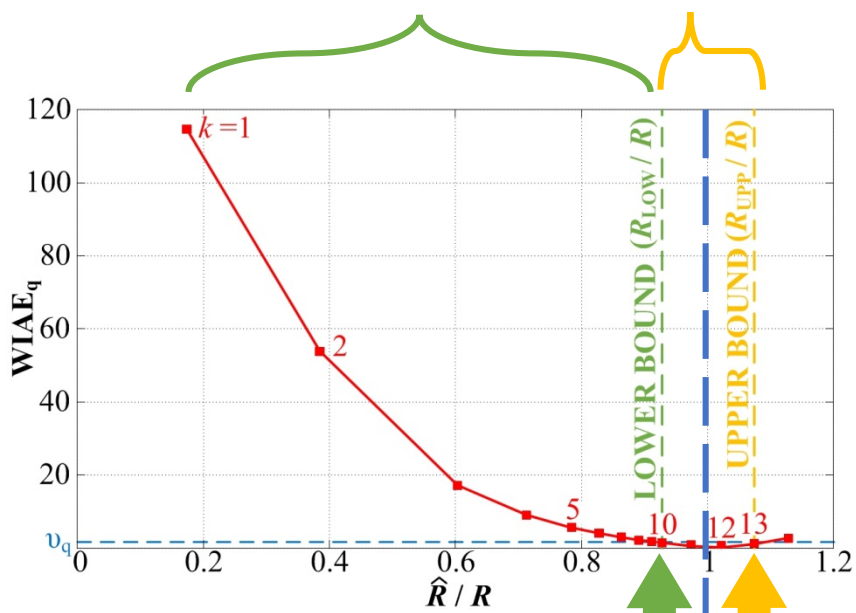
# Developed Method

Approach to  $R$   
lower bound Refinement



# Developed Method

Approach to  $R$   
lower bound Refinement



$$i_q^{\hat{R}=R} \approx i_q$$

$R$  estimation  
end

$$R_{met} = (R_{LOW} + R_{UPP})/2$$

$$R_C = R_{met} - R_F$$



## Other contents of Chapter 2

- **Theoretical examples of representative situations** with L and with LCL filters ( $P_{\text{rated}}$ ,  $V_{\text{LLrated}}$ ,  $P_{\text{level}}$ ,  $f_{\text{sw}}$ ,  $f_s$ ,  $i_{\text{q}}^*$ ,  $L_{\text{F}}$ ,  $R_{\text{F}}$ ,  $R_{\text{C}}$ ).

- For all the cases,  $R_{\text{C}}$  matches quite well  $R_{\text{C}}^{\text{met}}$  in few iterations.

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41-42

- **Implementation options:**

- **Offline**, during a precommissioning stage.
- **Online** → PICCD must be adopted to regulate the positive-sequence fundamental component of the current.

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41-43

- **Effect on the resistance estimate of uncertainties in the inductance value.**

- The error made in  $\hat{R}$  is **irrelevant**, even for  $\hat{L}/L=1.20$  and  $\hat{L}/L=0.80$ .

Pag.  
44

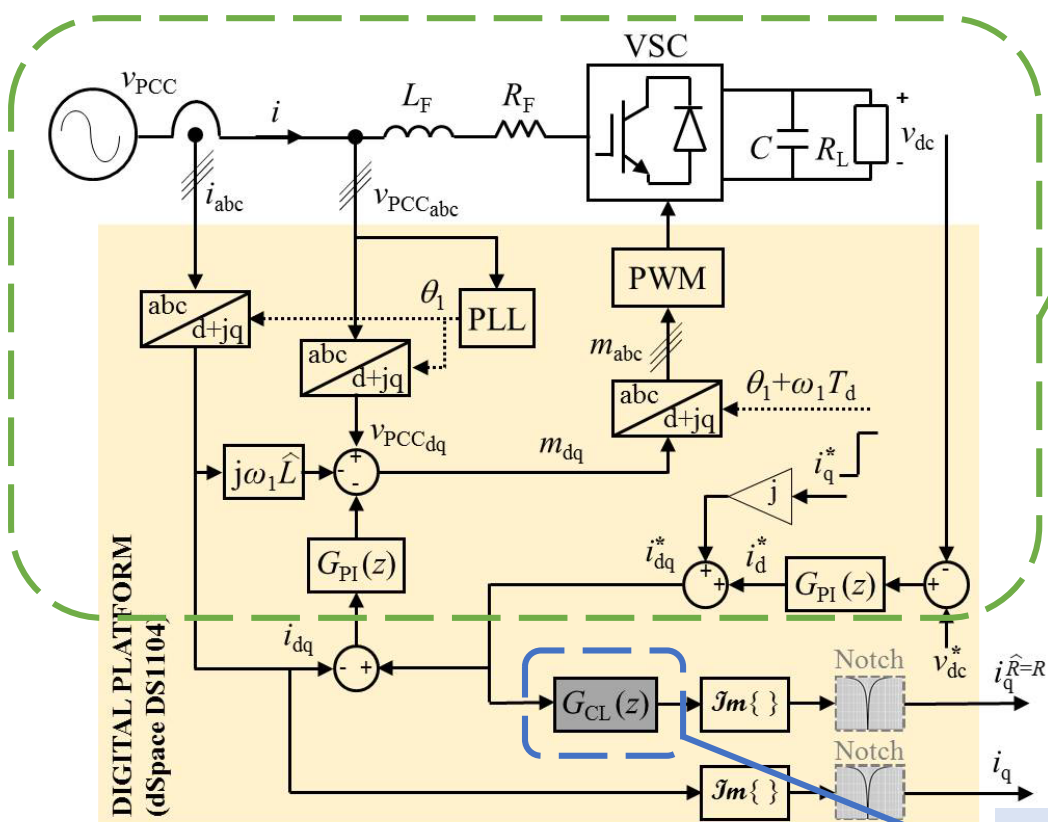
- 2DOF PI controller case (“active resistance”).

- Although including an “**active resistance**” lowers to a certain point the **sensitivity** of the current loop response in the presence of **R uncertainties**, **knowing R** permits to **further enhance the transient response**, especially as **R** grows.

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45-48



# Experimental Setup



**Actual control loop:**

- plant → a 3-ph grid-tied VSC
- control → dSpace.

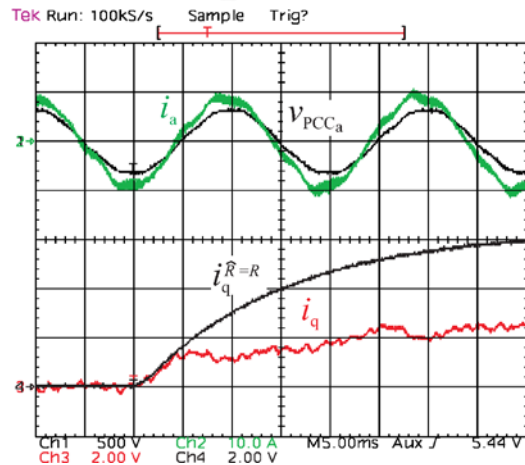
**Simulated control loop:**

- simulated plant + control → dSpace.

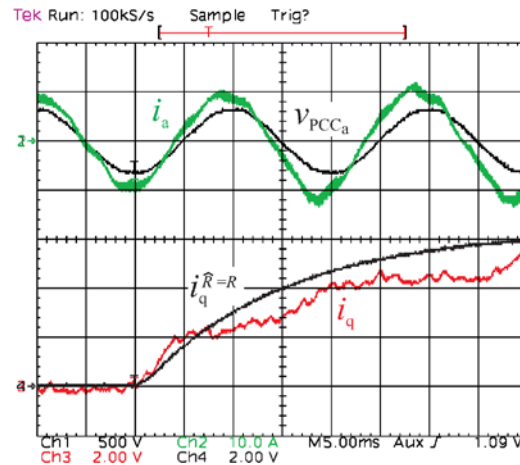
## Experimental Tests

Case	$P_{dc}$	$f_{sw}=f_s$	$L_F$	$R_F$	$i_d$	$i_q^*$	$v_{dc}$	$v_{PCC}$	$R_C^{met}$	$k_{max}$
A	4.3 kW	10 kHz	5.9 mH	0.4 $\Omega$	9.7 A	6.3 A	750 V	230 V	1.9 $\Omega$	14
B	2.8 kW	10 kHz	5.9 mH	0.4 $\Omega$	6.3 A	6.3 A	750 V	230 V	2.6 $\Omega$	16
C	1.8 kW	10 kHz	5.9 mH	0.4 $\Omega$	4.3 A	4.3 A	750 V	230 V	3.8 $\Omega$	22
D	1.8 kW	5 kHz	9.6 mH	0.4 $\Omega$	4.3 A	4.3 A	750 V	230 V	2.7 $\Omega$	13
E	1.8 kW	2.5 kHz	11.7 mH	0.4 $\Omega$	4.3 A	4.3 A	750 V	230 V	1.3 $\Omega$	9

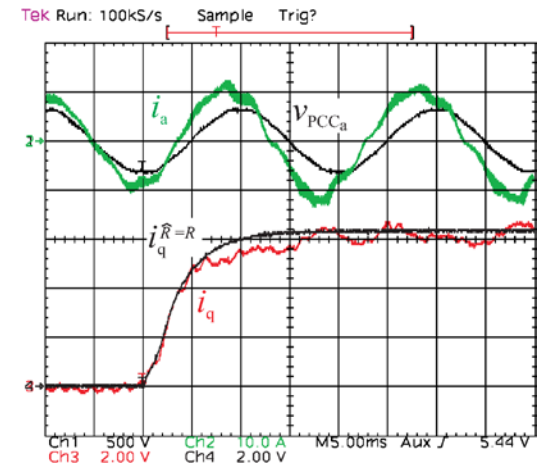
# Experimental Test A



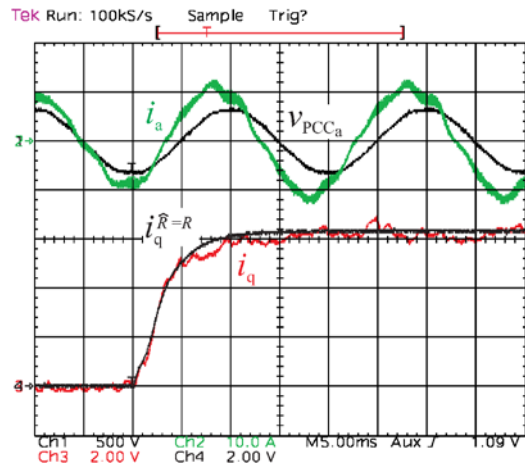
$$k = 1; \hat{R} = 0.40 \Omega;$$



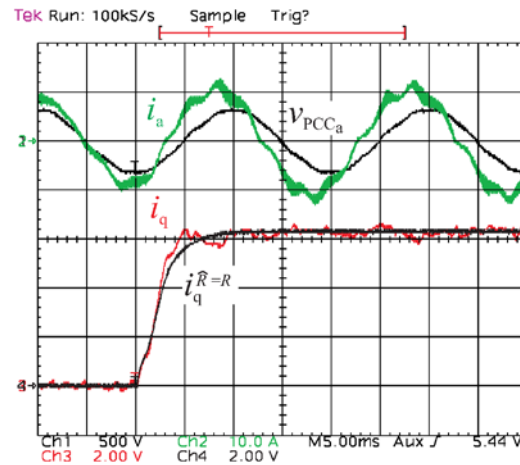
$$k = 2; \hat{R} = 0.89 \Omega;$$



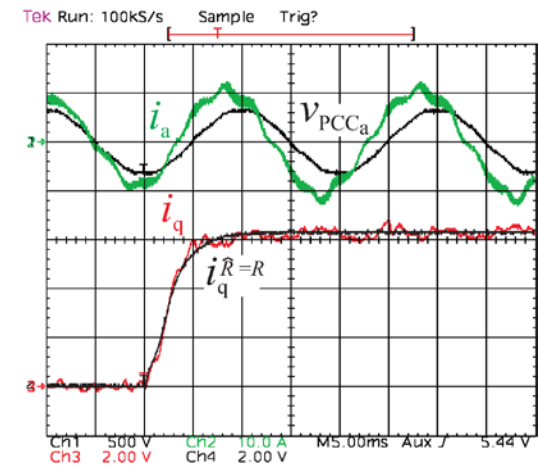
$$k = 5; \hat{R} = 1.80 \Omega;$$



$$k = 10; R_{LOW} = \hat{R} = 2.13 \Omega;$$



$$k = 13; R_{UPP} = \hat{R} = 2.47 \Omega;$$



$$k = 14; R_{met} = 2.30 \Omega$$

## Conclusions of Chapter 2

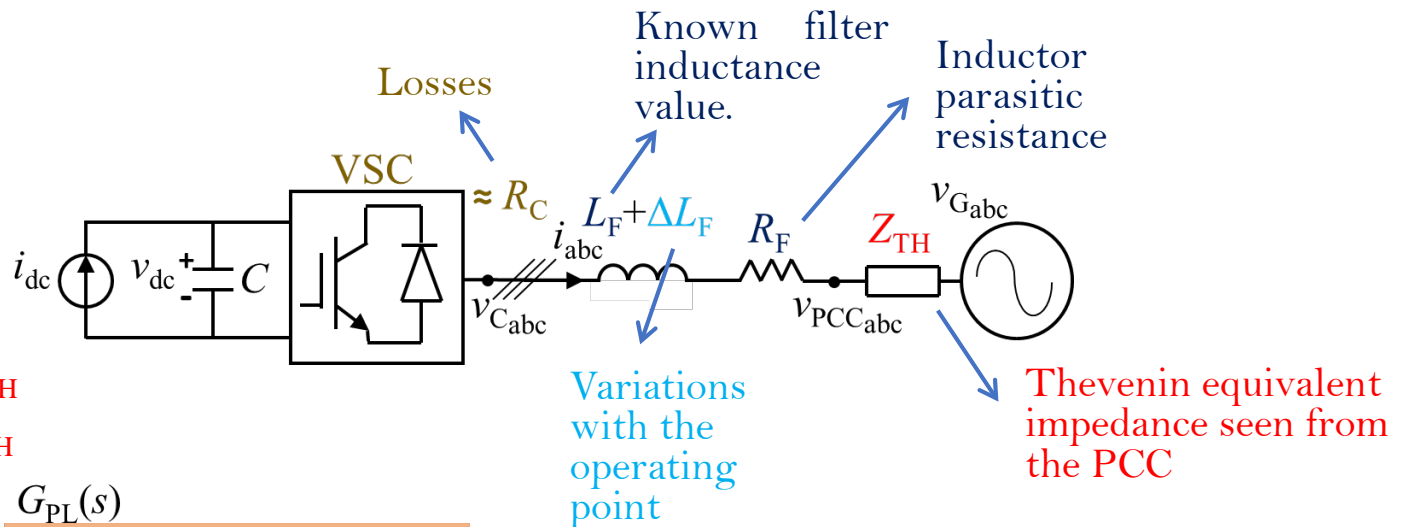
- An **incorrect estimation** of the **equivalent resistance** in the plant model of the **current control closed loop** leads to a **degraded behavior** of it, different from the theoretical one (e.g., in terms of settling time and overshoot). Hence, its **identification** is **essential** for a **rigorous analysis** and **design** of this loop.
- A **method** to **estimate** the **VSC equivalent loss resistance** in specific working conditions has been proposed. Such resistance reflects the influence of the power losses on the plant model.
- The developed algorithm is based on the **iterative minimization** of a **cost function that quantifies the error between the current control closed-loop step responses of the actual and the one including a simulated plant**, with the current controllers tuned according to IMC. Thus, it is **particularly oriented** to the fulfillment of **transient response constraints**.

# Outline

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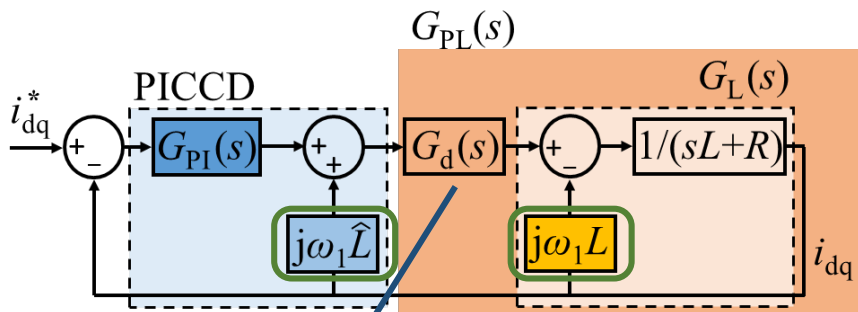
1. Introduction
2. Equivalent Loss Resistance Estimation of Grid-Tied Converters for Current Control Analysis and Design
3. A Method for Identification of the Equivalent Inductance and Resistance in the Plant Model of Current-Controlled Grid-Tied Converters
  - Model and Control of the Current Loop
  - Analysis of the Current Control Closed Loop
  - Identification Method
  - Experimental Results
  - Conclusion
4. Assessment and Optimization of the Transient Response of Proportional-Resonant Current Controllers for Distributed Power Generation Systems
5. Transient Response Evaluation of Stationary-Frame Resonant Current Controllers for Grid-Connected Applications
6. Conclusions and Future Research

# Current Loop



$$L = L_F + \Delta L_F + L_{TH}$$

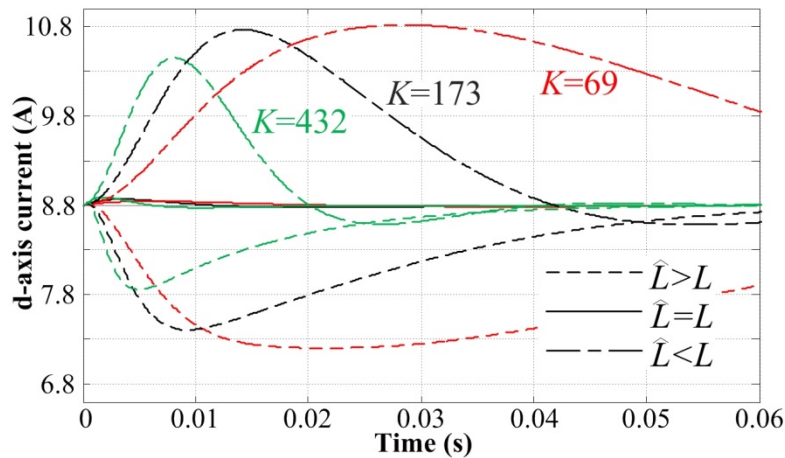
$$R = R_F + R_C + R_{TH}$$



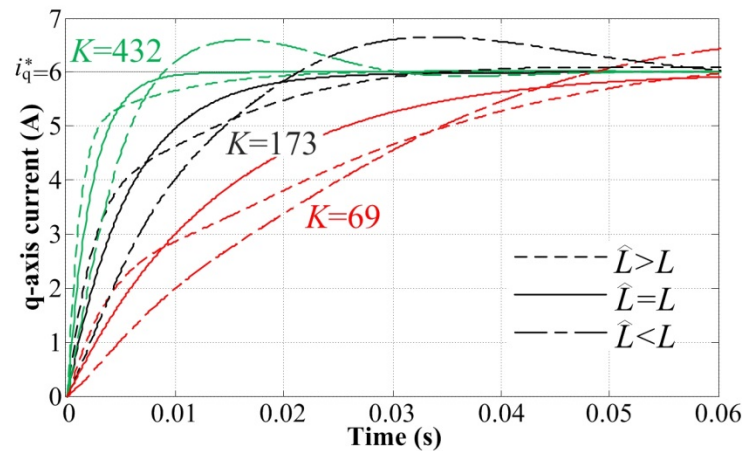
Remaining delay after applying delay compensation in SRF.

To study the **impact of the  $L$  uncertainties on the current closed loop**, it is important **not to neglect the delay** (even for a first approach).

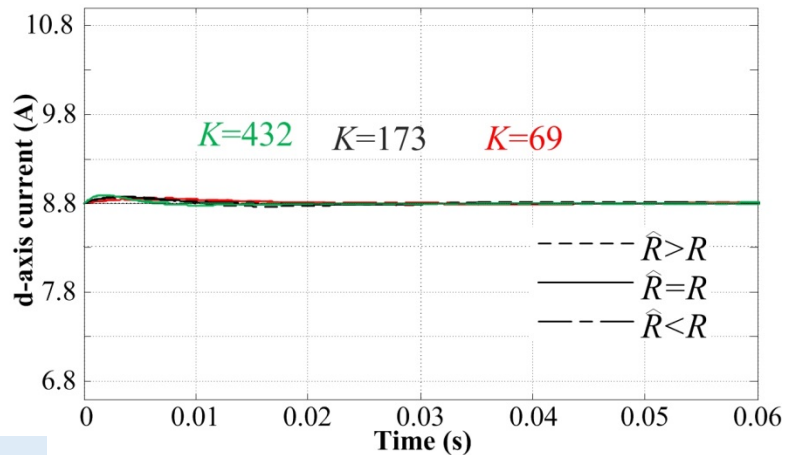
# Influence of Mismatches on the Time-Domain Step Responses



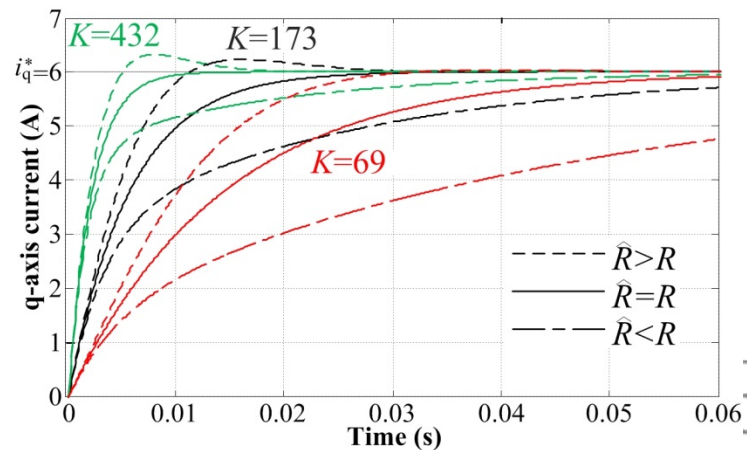
Effect of  $\hat{L}$  on  $i_d$ .



Effect of  $\hat{L}$  on  $i_q$ .



Effect of  $\hat{R}$  on  $i_d$ .

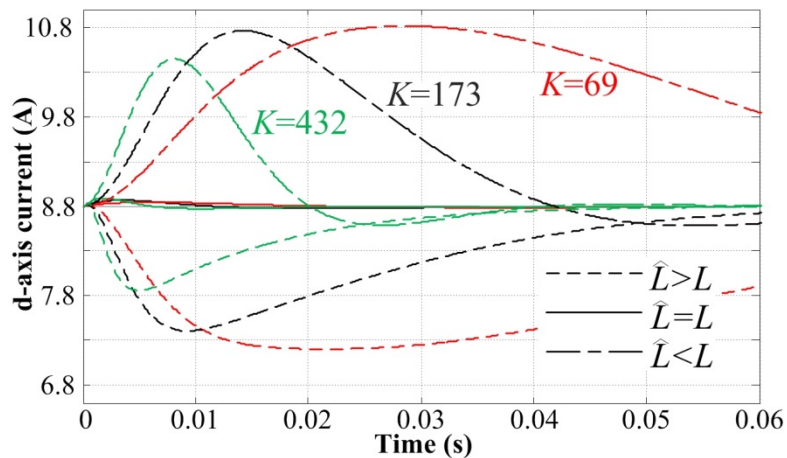


Effect of  $\hat{R}$  on  $i_q$ .

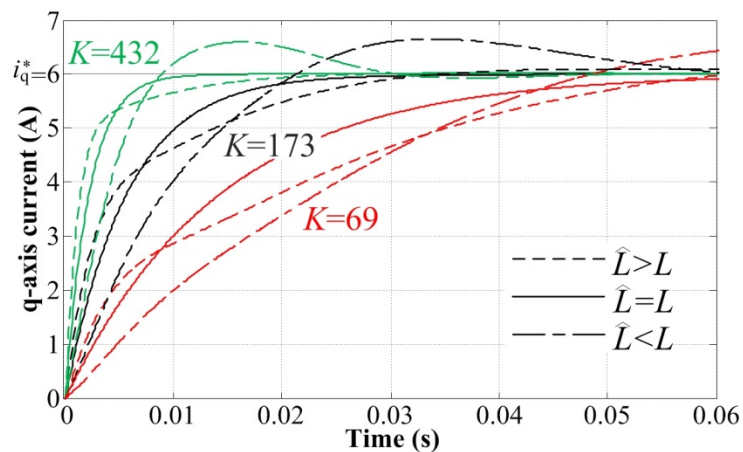




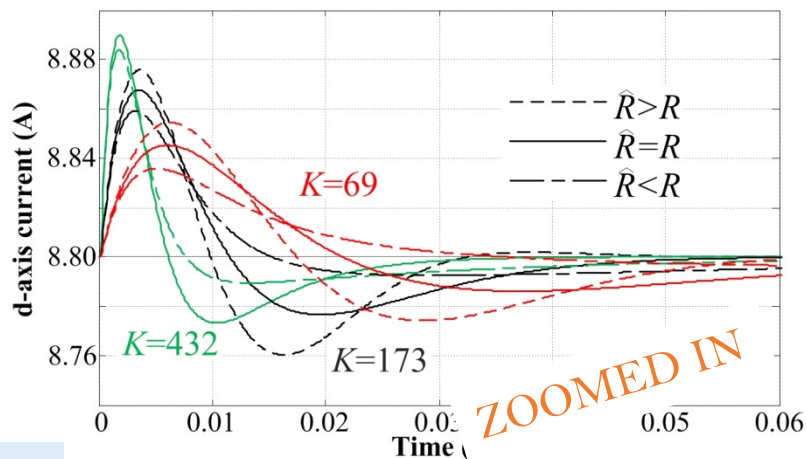
# Influence of Mismatches on the Time-Domain Step Responses



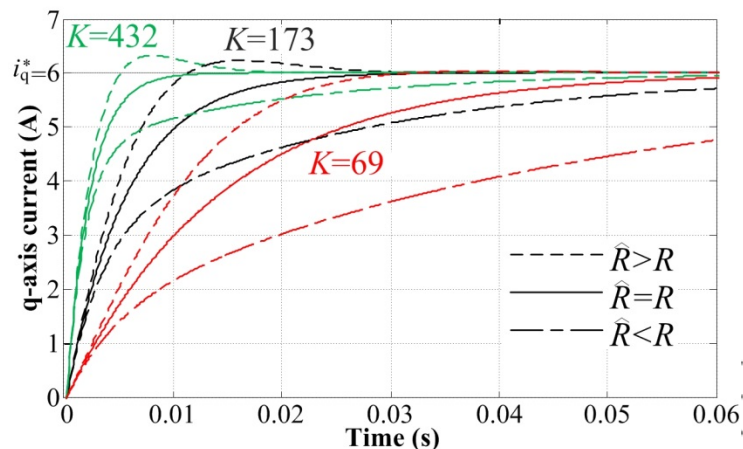
Effect of  $\hat{L}$  on  $i_d$ .



Effect of  $\hat{L}$  on  $i_q$ .



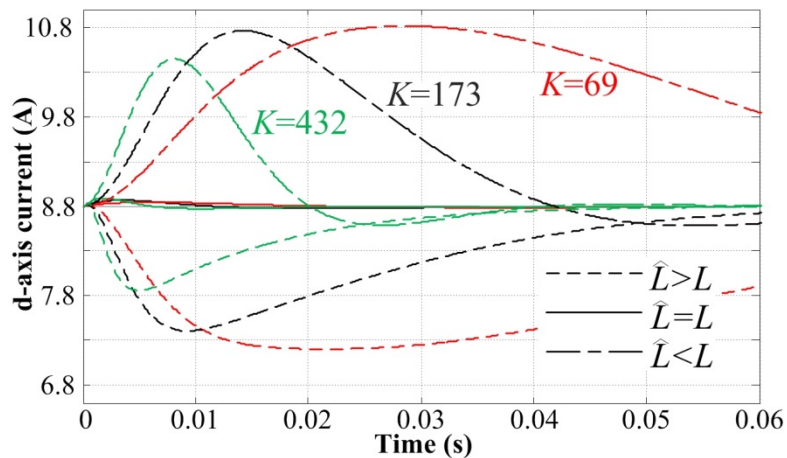
Effect of  $\hat{R}$  on  $i_d$ .



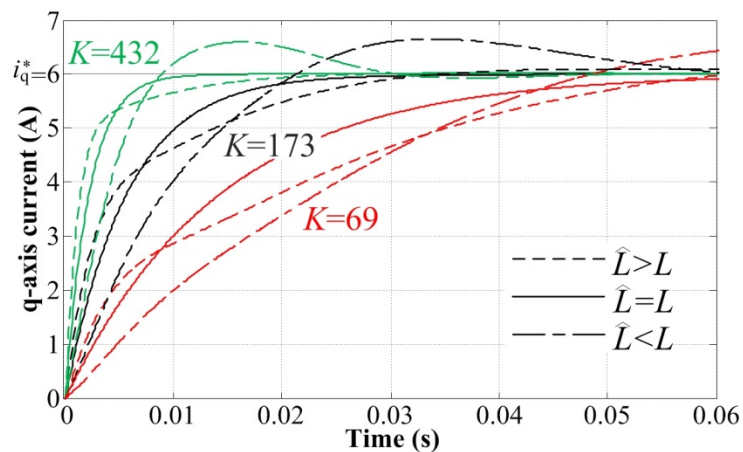
Effect of  $\hat{R}$  on  $i_q$ .



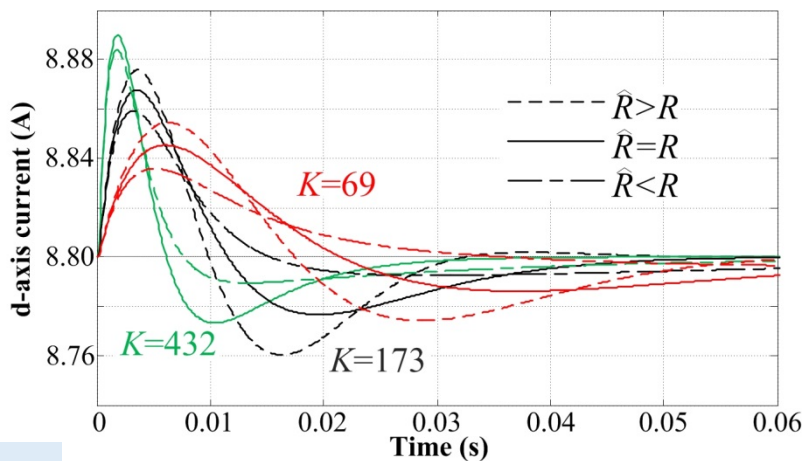
# Influence of Mismatches on the Time-Domain Step Responses



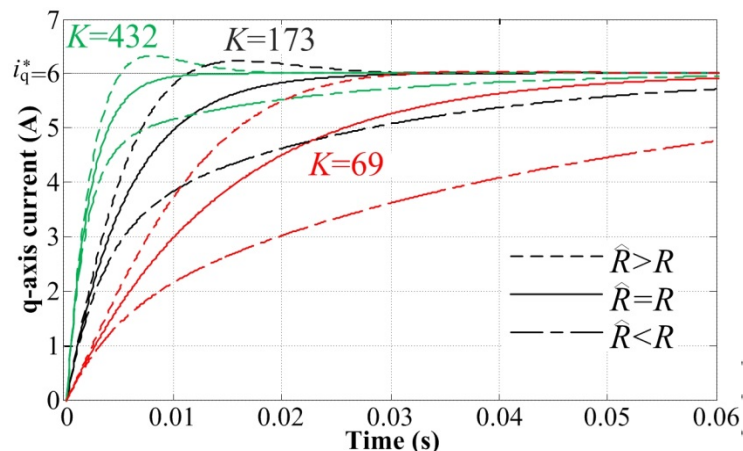
Effect of  $\hat{L}$  on  $i_d$ .



Effect of  $\hat{L}$  on  $i_q$ .



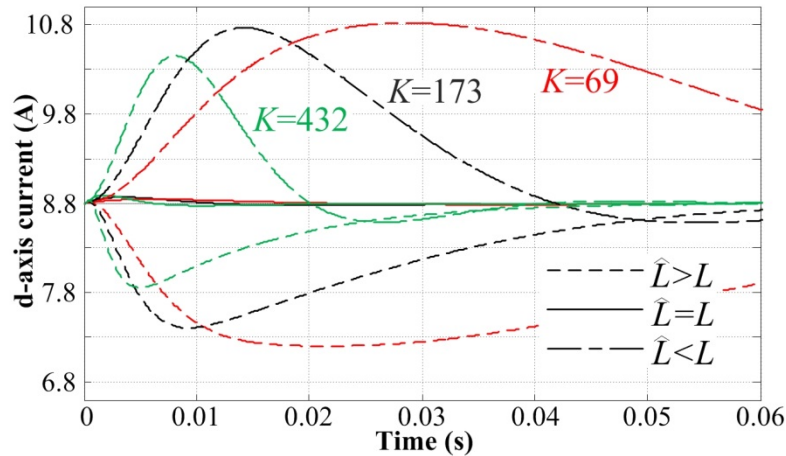
Effect of  $\hat{R}$  on  $i_d$ .



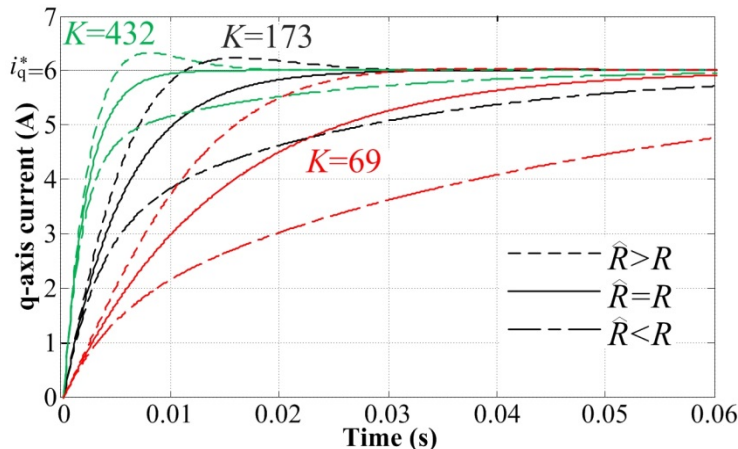
Effect of  $\hat{R}$  on  $i_q$ .



# Influence of Mismatches on the Time-Domain Step Responses



Effect of  $\hat{L}$  on  $i_d$ .



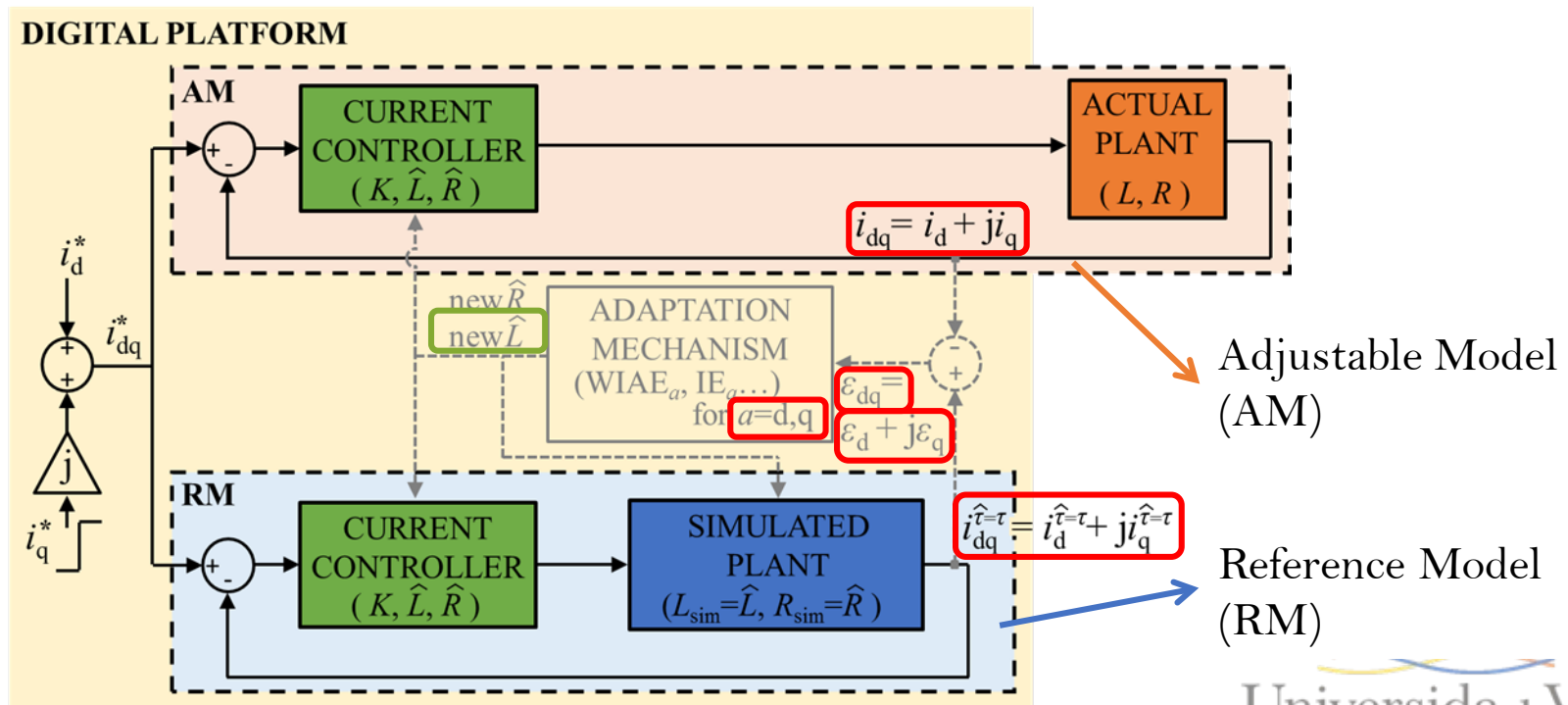
Effect of  $\hat{R}$  on  $i_q$ .

## Two indicators:

- the sign of the error area (**IE**)  
→ whether the parameter is **under** or **overestimated**,
- the area (**IAE**)  
→ how large is the **parameter mismatch**.

# Developed Method

- Able to estimate **both parameters**:  $L = L_F + \Delta L_F + L_{TH}$  and  $R = R_F + R_C + R_{TH}$ .
- **Both orthogonal components** of the plant output are considered.
- The **inability of the axes decoupling** to perform properly **in the presence of parameter mismatches** is exploited.
- If  $\hat{R} \approx R$  and  $\hat{L} \approx L$



# Developed Method

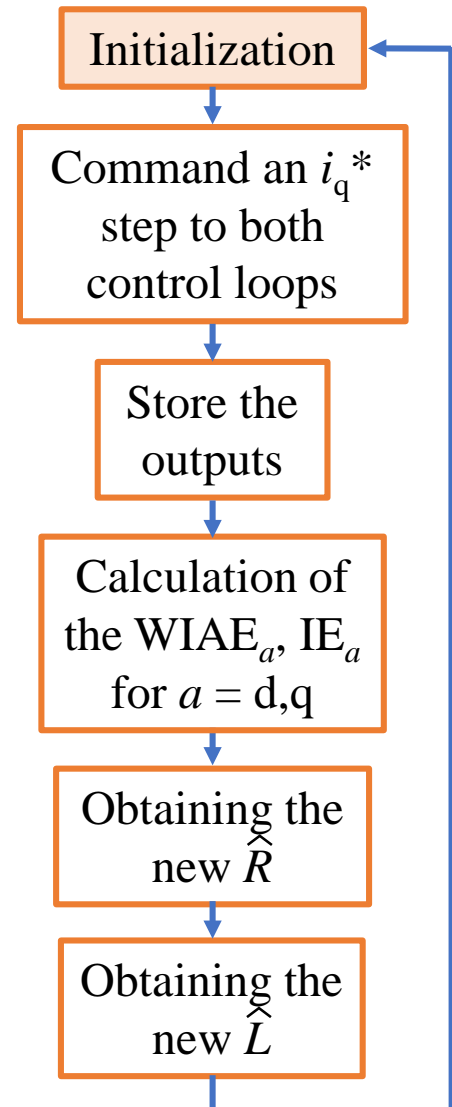
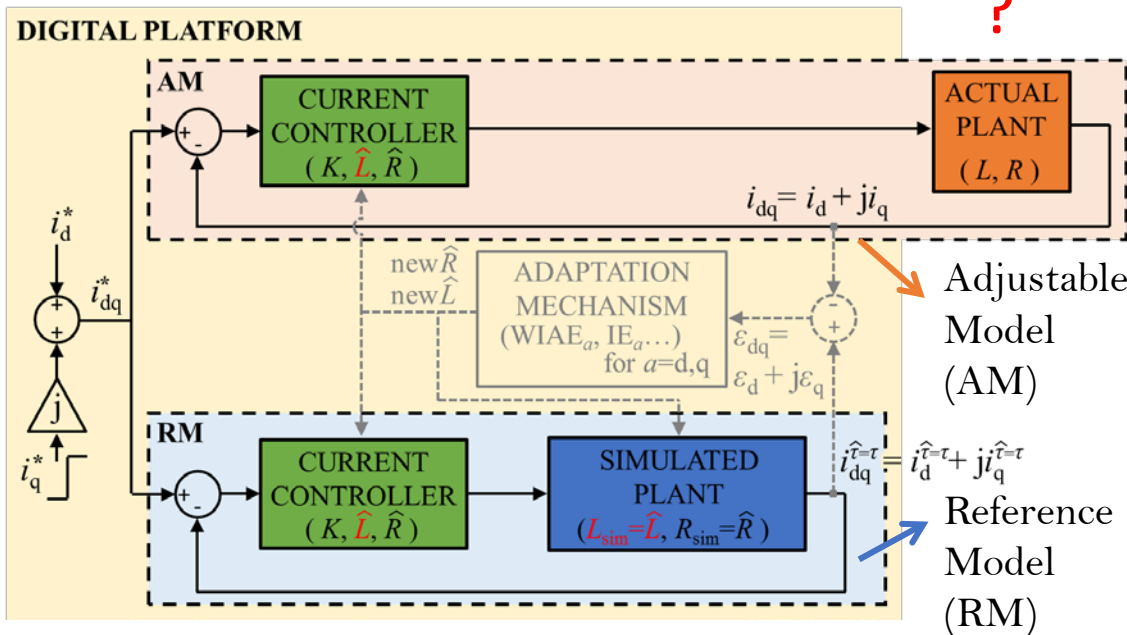
## 1. Initialization → extra variables

- Auxiliary variables
- Controller parameters

$$\hat{R}(1), \hat{L}(1), K(k) = \hat{R}(k) / \hat{L}(k)$$

- Simulated plant parameters

$$L_{sim} = \hat{L}(k), R_{sim}(k) = \hat{R}(k)$$

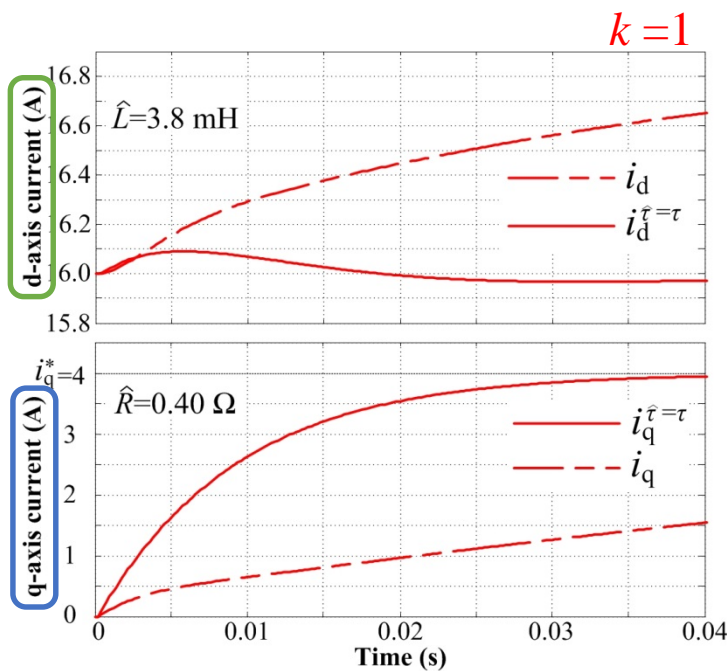


# Developed Method

Coupling

Step

Pag. 67-73



CASE C

$f_{sw} =$	5 kHz
$f_s$	9.9 mHz
$L$	9.9 mH
$\hat{L}(1) = L_F$	3.8 mH
$R$	3 $\Omega$
$\hat{R}(1) = R_F$	0.4 $\Omega$

Initialization

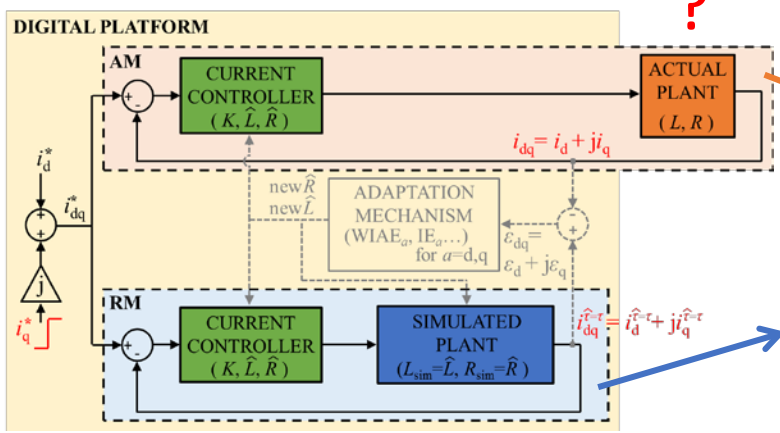
Command an  $i_q^*$  step to both control loops

Store the outputs

Calculation of the  $WIAE_a, IE_a$  for  $a = d, q$

Obtaining the new  $\hat{R}$

Obtaining the new  $\hat{L}$





# Developed Method

At each iteration (within each commanded step), a correct estimate of both parameters is aimed.

## $L$ identification Vs $R$ identification:

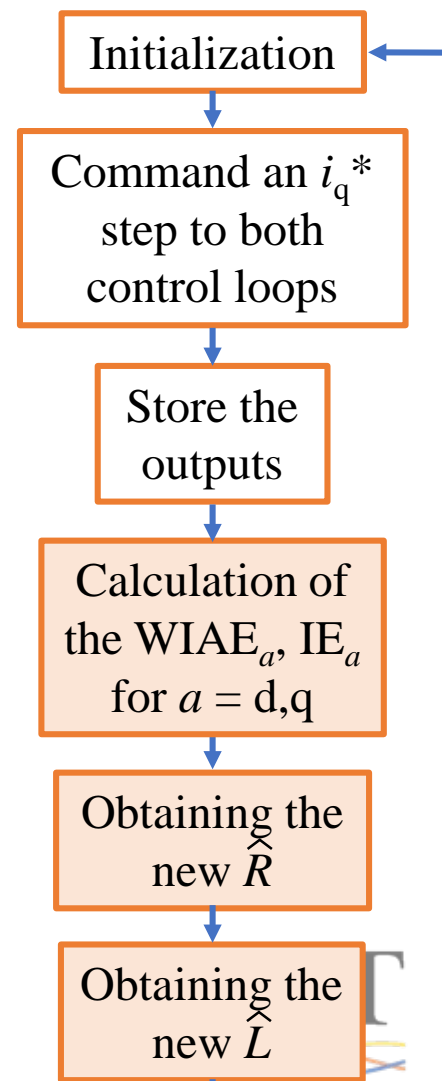
- $WIAE_d = IAE_d$  for under and overestimate cases.
- Initial overestimation is also regarded.
- As the delay has an important influence on the axis cross coupling,  $T_s$  should be also considered when updating the new  $L$  estimate.

$$WIAE_d = IAE_d$$

$$WIAE_q \begin{cases} IAE_q & \text{if } IAE_q \geq 0 \\ (IAE_q)^2 & \text{if } IAE_q < 0 \end{cases}$$

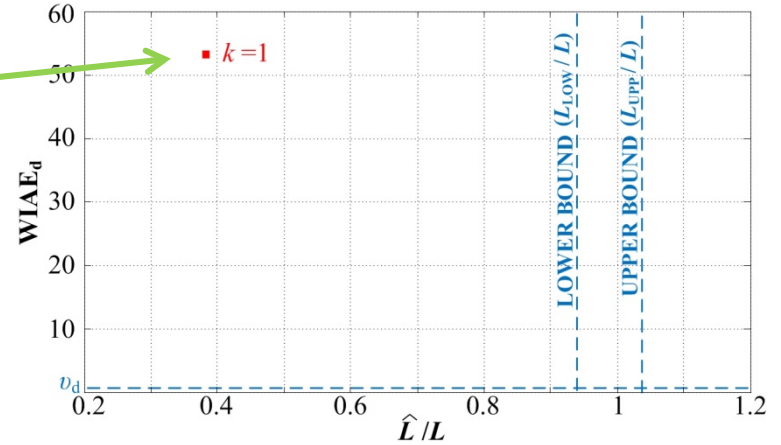
$$\hat{L}(k+1) = [1 + L_{F\_under} \cdot \Delta_d(k)] \cdot \hat{L}(k)$$

$$\Delta_d(k) = f(WIAE_d(k), i_q^*, T_s)$$

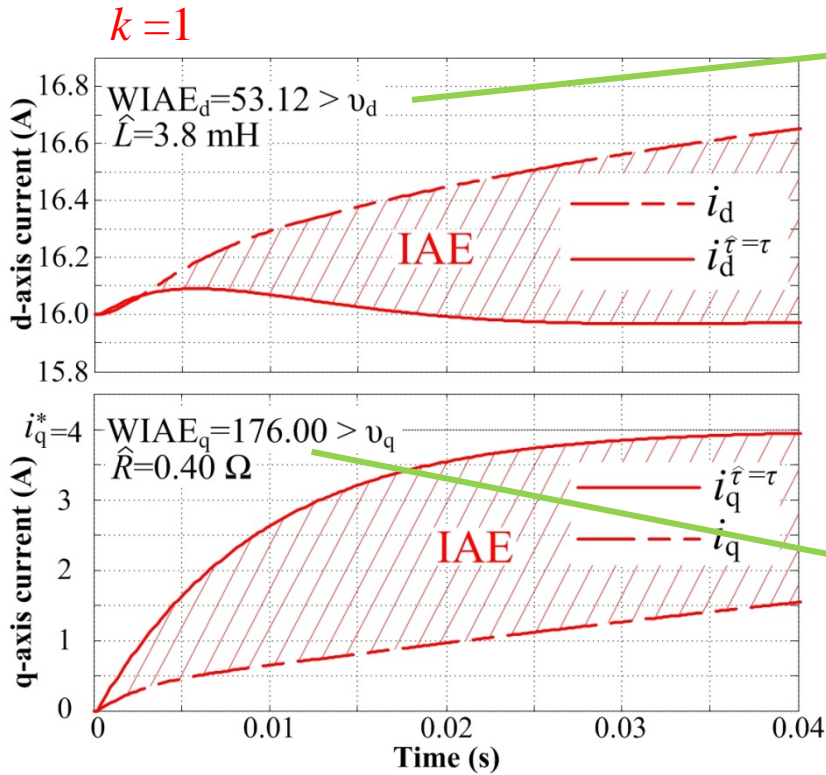
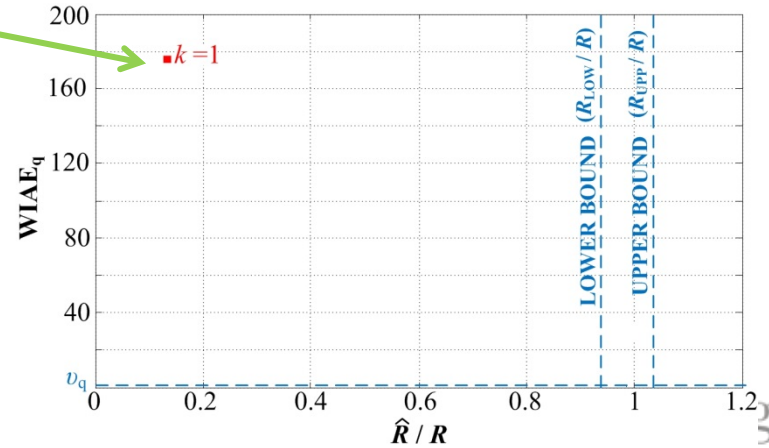


# Developed Method

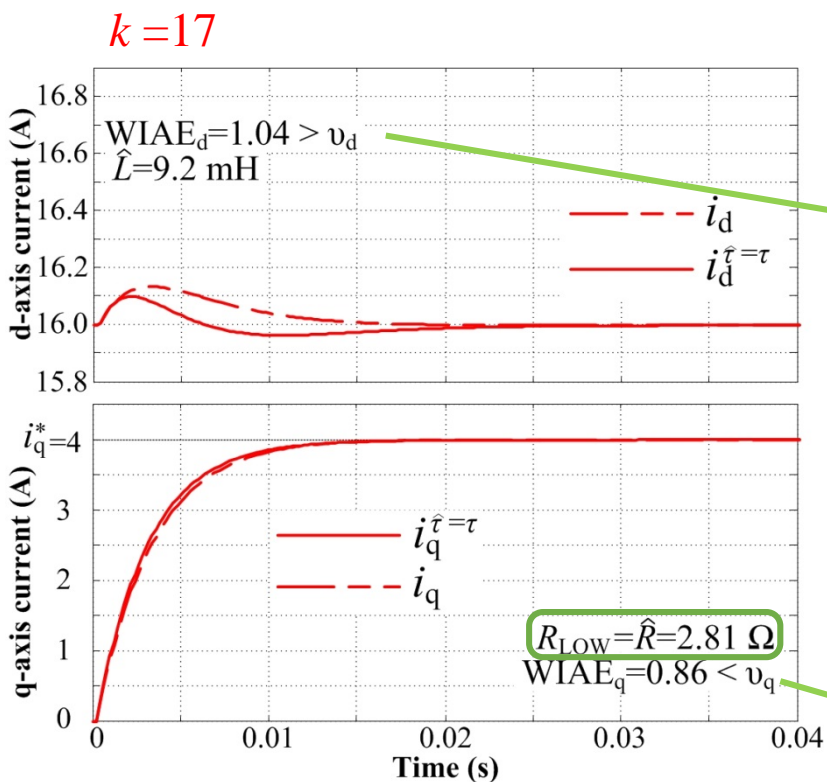
Approach to  $L$  1<sup>st</sup> bound



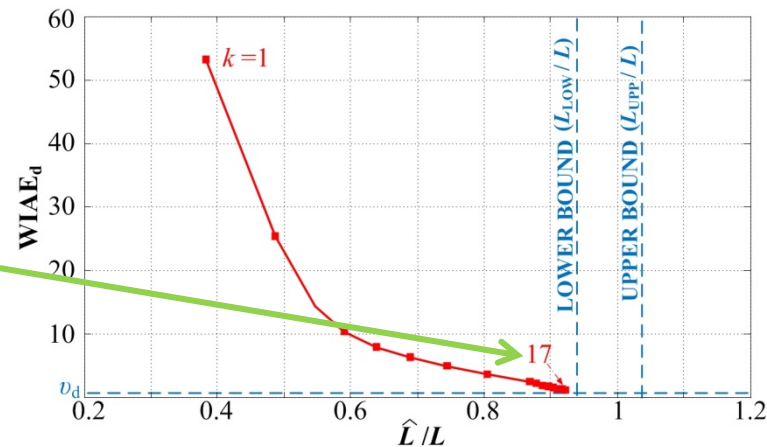
Approach to  $R$  1<sup>st</sup> bound



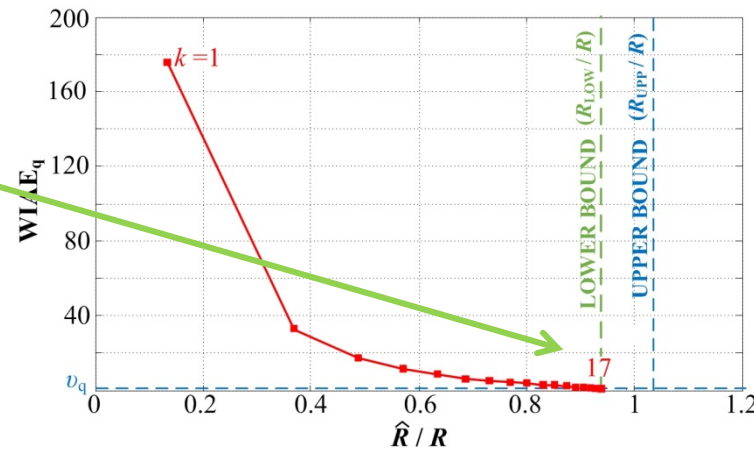
# Developed Method



## Approach to $L$ 1<sup>st</sup> bound



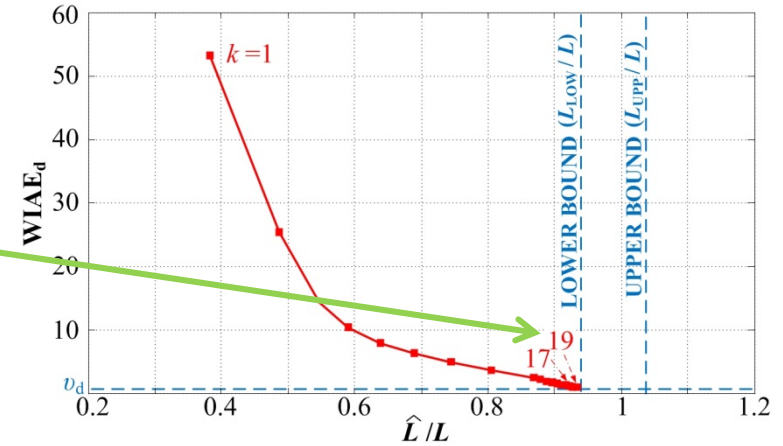
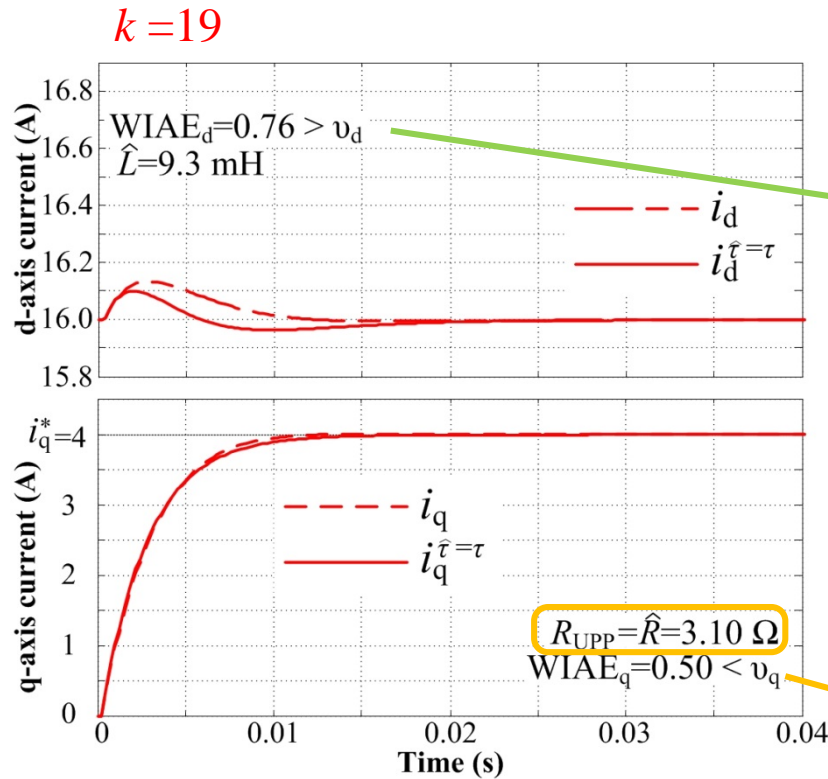
## Approach to $R$ 1<sup>st</sup> bound



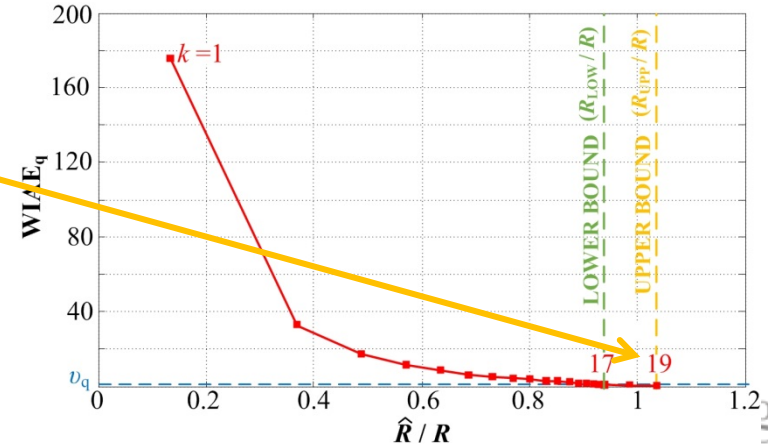


# Developed Method

## Approach to $L$ 1<sup>st</sup> bound

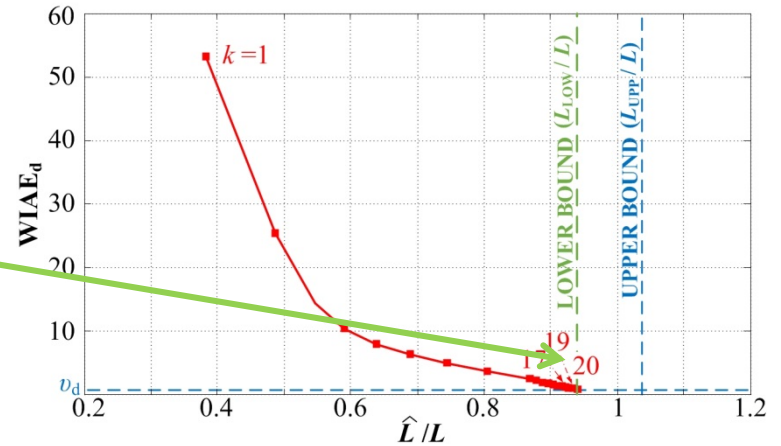
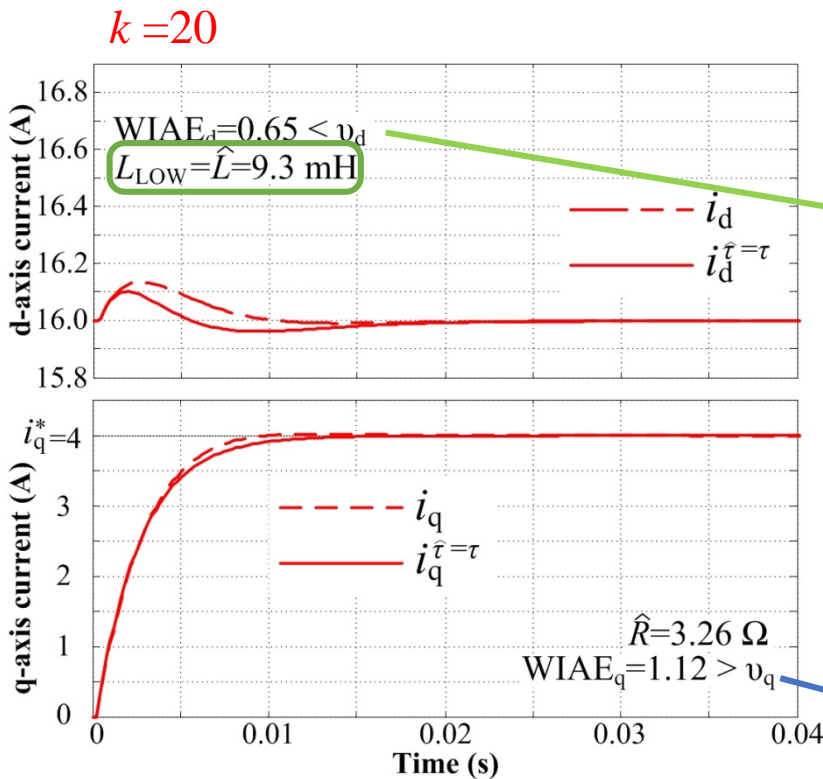


## R refinement

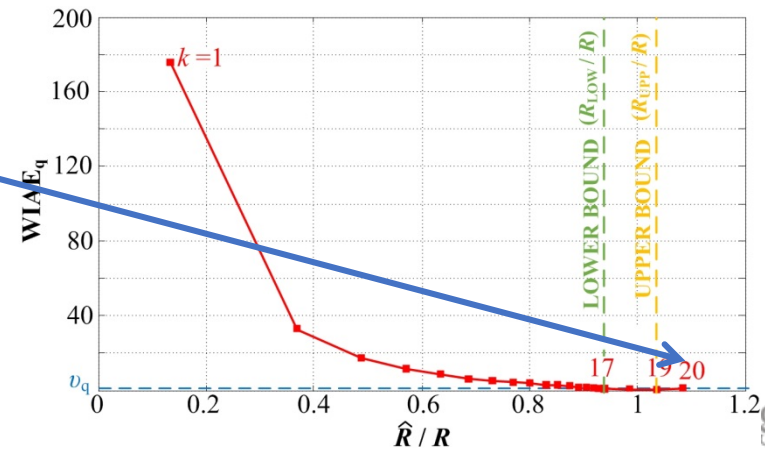


# Developed Method

## Approach to $L$ 1<sup>st</sup> bound

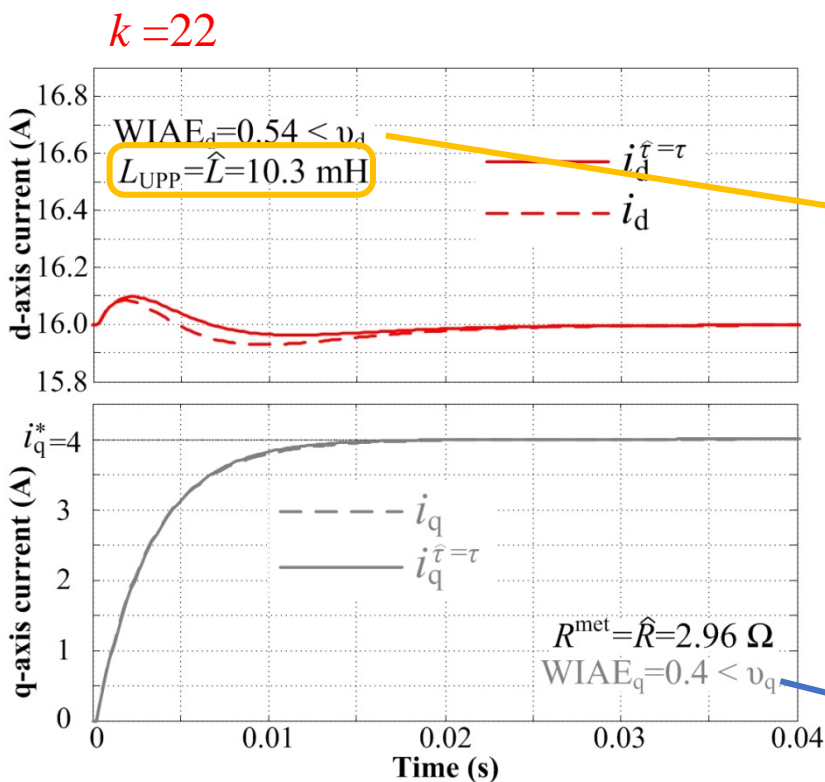


## R estimation end



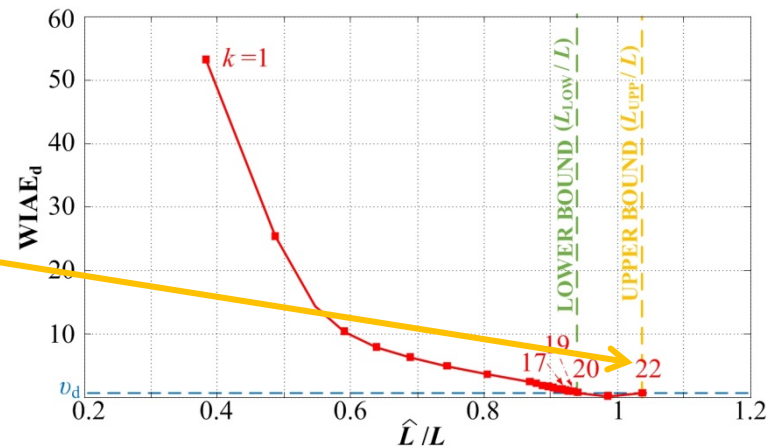
$$R_{met} = (R_{LOW} + R_{UPP}) / 2 = 2.96 \Omega$$

# Developed Method

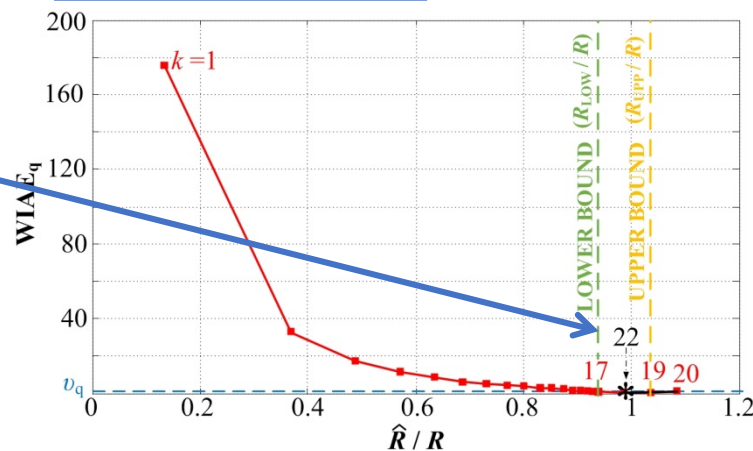


$$R^{met} = (R_{LOW} + R_{UPP})/2 = 2.96 \Omega$$

## L refinement



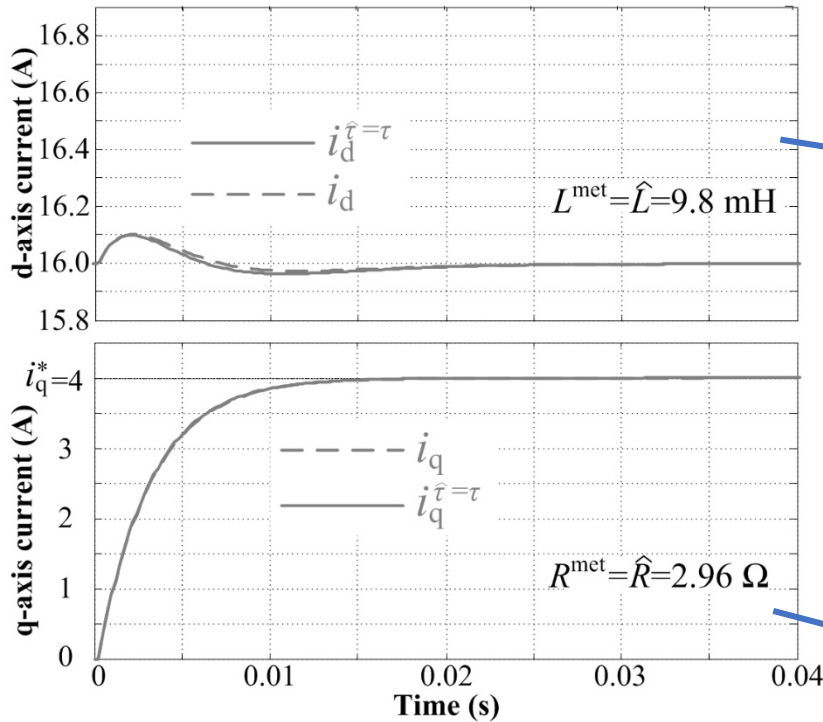
## R estimation end



# Developed Method

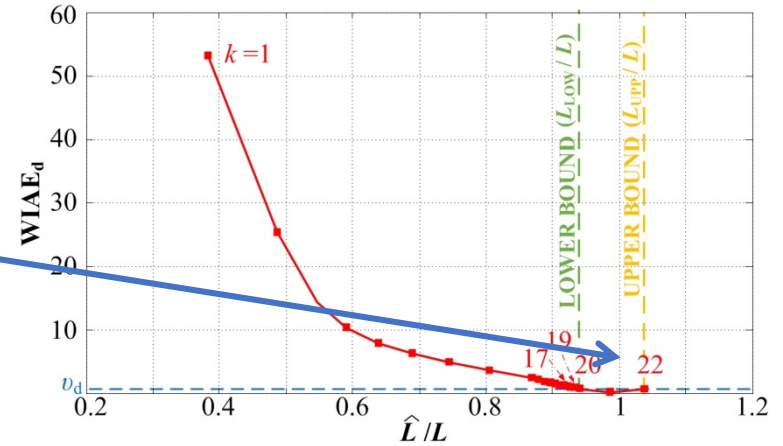
$$L^{\text{met}} = (L_{\text{LOW}} + L_{\text{UPP}})/2 = 9.8 \text{ mH}$$

*Estimation end*

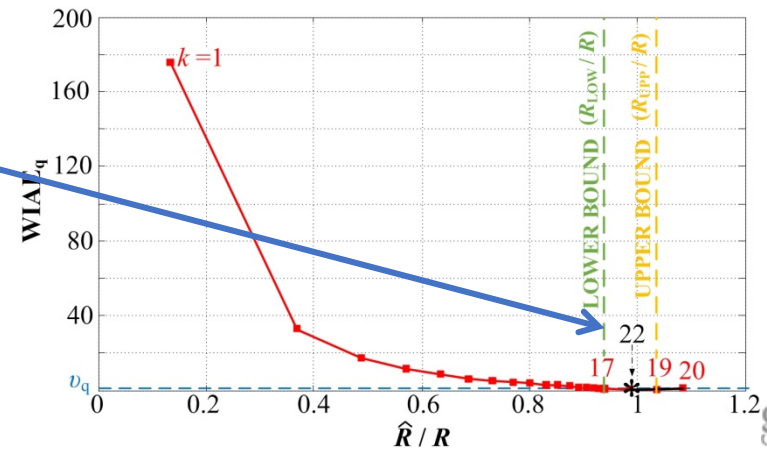


$$R^{\text{met}} = (R_{\text{LOW}} + R_{\text{UPP}})/2 = 2.96 \Omega$$

$L$  estimation end



$R$  estimation end



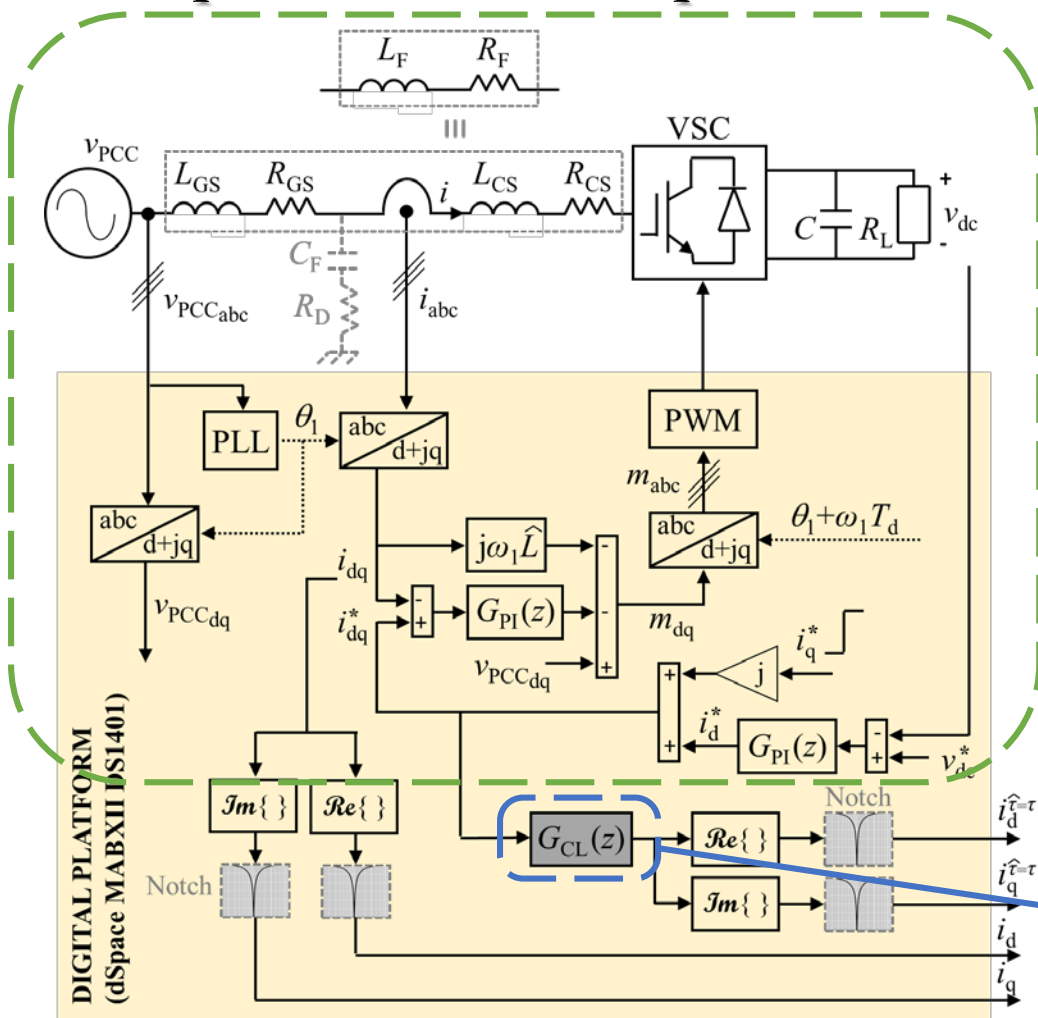
## Other contents of Chapter 3

- **Analysis of the root-locus diagrams with  $L$  and LCL filters.**
  - To evaluate the validity of the  **$L$  admittance model for LCL filters.**
  - To study the **loop stability.**
  - To establish a **proper  $K$  gain** for the method.
  - To corroborate that a **correct estimation** of the plant parameters leads to a **better transient response**, in terms of overshoot and settling time.
- **Parameter tuning guidelines.**
- **Theoretical examples of representative situations** with  $L$  and with LCL filters ( $P_{\text{rated}}$ ,  $V_{LL_{\text{rated}}}$ ,  $P_{\text{level}}$ ,  $f_{\text{sw}}$ ,  $f_s$ ,  $i_q^*$ ,  $L_F$ ,  $R_F$ ,  $R_C$ ).
  - For all the cases,  $R_C$  matches quite well  $R_C^{\text{met}}$  in few iterations.
  - **Study of the regions of convergence** as a function of the parameter mismatches.
- **Implementation options:**
  - **Offline**, during a precommissioning stage.
  - **Online** → PICCD must be adopted to regulate the positive-sequence fundamental component of the current.

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60-64Pag.  
73, 74Pag.  
75-77Pag.  
74, 75



# Experimental Setup



## Actual control loop:

- plant → a 3-ph grid-tied VSC
- control → dSpace.

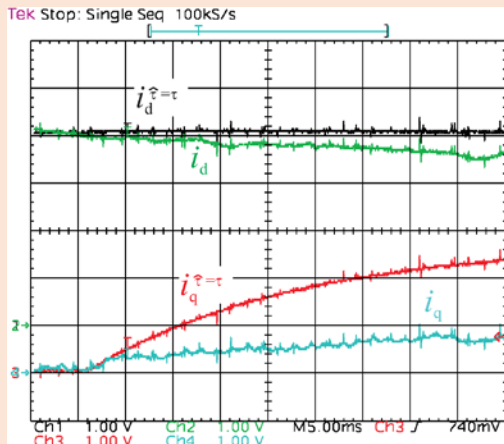
## Simulated control loop:

- simulated plant + control → dSpace.

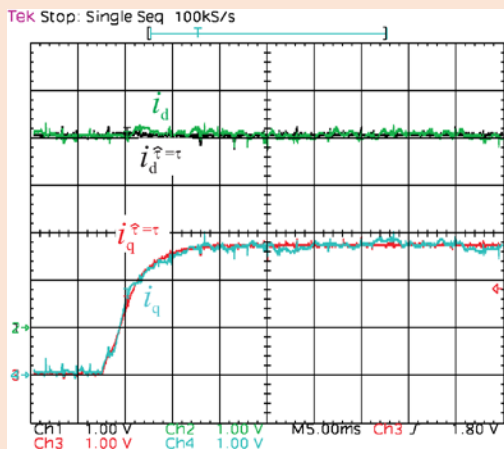
## Experimental Tests

Case (filter)	$P_{dc}$	$\frac{f_{sw}}{f_s}$	$L_F$ ( $L_{GS}+L_{CS}$ )	$R$	$\hat{L}(1)$	$\hat{R}(1)=R_F$ ( $R_{GS}+R_{CS}$ )	$L^{met}$	$R^{met}$	$k_{max}$
A (L)	4.3 kW	10 kHz 10 kHz	5.9 mH	2.3 $\Omega$	$1.6L_F$ = 9.4 mH	0.4 $\Omega$	5.9 mH	2.29 $\Omega$	20
B (LCL)	4.3 kW	5 kHz 10 kHz	10.9 mH (5+5.9)	1.9 $\Omega$	$1.6L_F$ = 17.4 mH	0.45 $\Omega$ (0.05+0.4)	11 mH	1.88 $\Omega$	15
C (L)	2 kW	5 kHz 5 kHz	9.5 mH	3 $\Omega$	$0.4L_F$ = 3.8 mH	0.4 $\Omega$	9.8 mH	2.96 $\Omega$	23
C (L)	2 kW	2.5 kHz 2.5 kHz	12.1 mH	1.7 $\Omega$	$0.4L_F$ = 4.8 mH	0.4 $\Omega$	12.6 mH	1.77 $\Omega$	10

### Test A

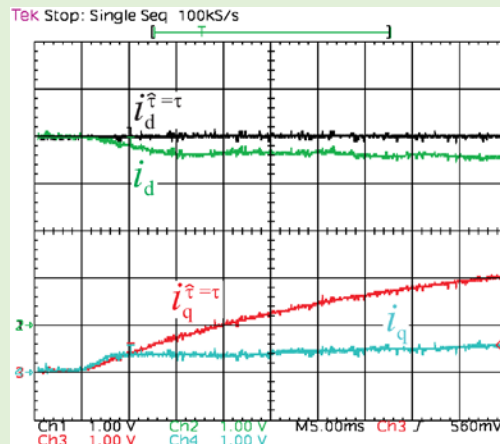


$k = 1; \hat{R} = 0.4 \Omega;$   
 $\hat{L} = 9.4 \text{ mH}$

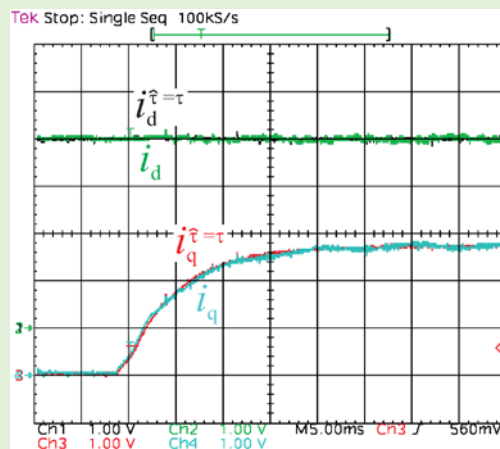


$k = 20; R^{\text{met}} = 2.29 \Omega;$   
 $L^{\text{met}} = 5.9 \text{ mH}$

### Test B

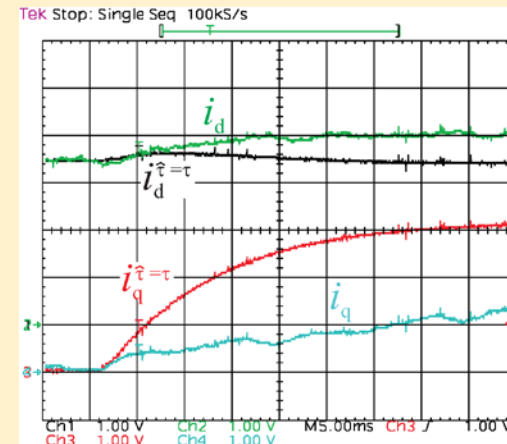


$k = 1; \hat{R} = 0.45 \Omega;$   
 $\hat{L} = 17.4 \text{ mH}$

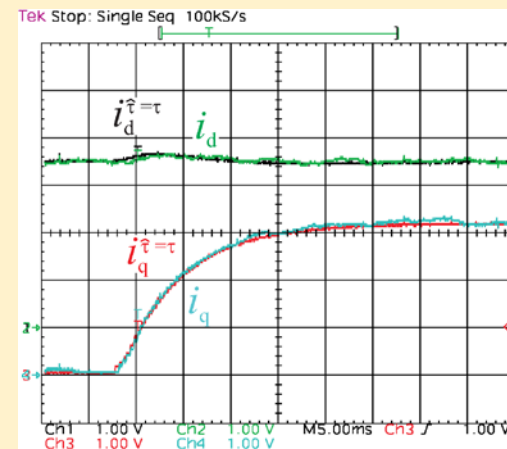


$k = 15; R^{\text{met}} = 1.88 \Omega;$   
 $L^{\text{met}} = 11 \text{ mH}$

### Test C



$k = 1; \hat{R} = 0.4 \Omega;$   
 $\hat{L} = 4.8 \text{ mH}$



$k = 10; R^{\text{met}} = 1.77 \Omega;$   
 $L^{\text{met}} = 12.6 \text{ mH}$



## Conclusions of Chapter 3

- A **method to identify** the two parameters of the current loop plant time constant at certain working conditions has been proposed:
  - the equivalent inductance
  - the equivalent resistance
- ➔ Thus, the **dynamics** of the actual loop **may be properly studied** and the **controller parameters** can be **precisely tuned**.
- The **validity of modeling an LCL filter as an L one** from the viewpoint of the current loop is **analyzed** in detail, as a function of the **gain value**. ➔ It is **demonstrated** that the **method** is also **valid** when **LCL filters** are employed.
- The **developed iterative algorithm** works in **closed loop**, at the same sampling frequency as the rest of the control. It **takes advantage of the current closed loop properties**, and **of the current controller itself** to perform the estimation. Hence, it is **particularly designed** to satisfy **time-domain specifications**.

# Outline

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1. Introduction
2. Equivalent Loss Resistance Estimation of Grid-Tied Converters for Current Control Analysis and Design
3. A Method for Identification of the Equivalent Inductance and Resistance in the Plant Model of Current-Controlled Grid-Tied Converters
4. Assessment and Optimization of the Transient Response of Proportional-Resonant Current Controllers for Distributed Power Generation Systems
  - Introduction
  - Error Root-Locus Analysis for Transient Optimization
  - Design Study
  - Experimental Results
  - Conclusion
5. Transient Response Evaluation of Stationary-Frame Resonant Current Controllers for Grid-Connected Applications
6. Conclusions and Future Research

## Framework

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- In order to fulfill the dynamic **GC requirements** (**LVRT** and **grid support**), an **enhanced transient response of the current loop is crucial**, which can be achieved thanks to a **precise tuning of the current controllers**.
- **Resonant regulators** (such as PR ones) have been proved to be a **good choice for grid connection**.
- There is a **lack of specific methods for PR controller tuning considering this demanding scenario**.

# Transient Assessment From the Error Signal Roots

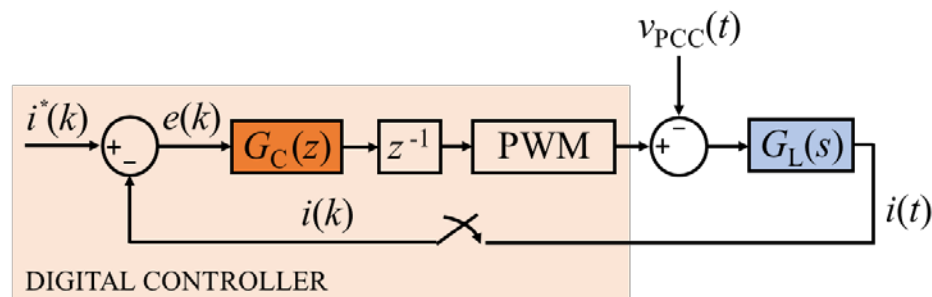
- **Methodology** based on the **root-locus inspection** in the **z-domain** of the **current error signal caused by transients**:
  - Transients in the current reference  $\Delta i^*(z)$
  - Transients in the disturbance  $\Delta v_{PCC}(z)$

1st step:

**Discrete-time expression of the global error**

$$E(z) = I^*(z) - I(z)$$

$$E(z) = E_{\Delta i^*}(z)|_{\Delta v_{PCC}=0} + E_{\Delta v_{PCC}}(z)|_{\Delta i^*=0}$$



# Transient Assessment From the Error Signal Roots

- **Methodology** based on the **root-locus inspection** in the **z-domain** of the **current error signal caused by transients**:
  - Transients in the current reference  $\Delta i^*(z)$
  - Transients in the disturbance  $\Delta v_{PCC}(z)$

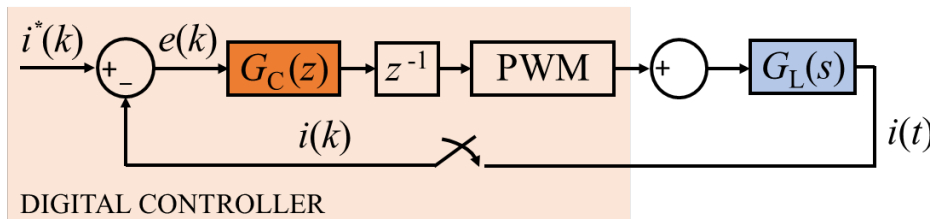
1st step:

**Discrete-time expression of the global error**

$$E(z) = E_{\Delta i^*}(z)|_{\Delta v_{PCC}=0} + E_{\Delta v_{PCC}}(z)|_{\Delta i^*=0}$$

$$E_{\Delta i^*}(z)|_{\Delta v_{PCC}=0} = \frac{1}{1 + G_C(z)z^{-1}G_L^{ZOH}(z)} \Delta i^*(z)$$

$$\Delta i^*(z) = (A_{\text{new}} - A_{\text{old}}) \underbrace{\frac{1 - z^{-1} \cos(\omega'_1 T_s)}{1 - 2z^{-1} \cos(\omega'_1 T_s) + z^{-2}}}_{\text{cosine term}} + (B_{\text{new}} - B_{\text{old}}) \underbrace{\frac{z^{-1} \sin(\omega'_1 T_s)}{1 - 2z^{-1} \cos(\omega'_1 T_s) + z^{-2}}}_{\text{sine term}}$$



# Transient Assessment From the Error Signal Roots

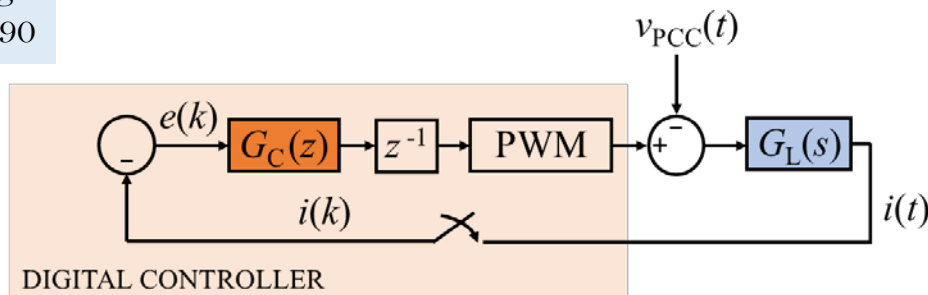
- **Methodology** based on the **root-locus inspection** in the **z-domain** of the **current error signal caused by transients**:
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**Discrete-time expression of the global error**

$$E(z) = E_{\Delta i^*}(z)|_{\Delta v_{PCC}=0} + E_{\Delta v_{PCC}}(z)|_{\Delta i^*=0}$$

$$E_{\Delta v_{PCC}}(z)|_{\Delta i^*=0} = \frac{G_L^{Tustin}(z)}{1 + G_C(z)z^{-1}G_L^{ZOH}(z)} \Delta v_{PCC}(z)$$



# Transient Assessment From the Error Signal Roots

## 1st step:

**Discrete-time expression of the global error.**

- $E(z) = E_{\Delta i^*}(z)|_{\Delta v_{PCC}=0} + E_{\Delta v_{PCC}}(z)|_{\Delta i^*=0}$

## 2nd step:

Graphical representation of the error signal roots as a function of the controller gain → Root loci.

- Influence on the stability, decay rate, damping.

## 3rd step:

Accurate prediction of the error waveform.

- Analysis of the effects of the root position on the transient response.

## 4th step:

Gain tuning.

- Optimization of the error transient response can be achieved:
  - By making the poles fast → large decay rates
  - By placing the poles next to zeros that cancel their effect → small residues



# Transient Assessment From the Error Signal Roots

## 1st step:

**Discrete-time expression of the global error.**

- $E(z) = E_{\Delta i^*}(z)|_{\Delta v_{PCC}=0} + E_{\Delta v_{PCC}}(z)|_{\Delta i^*=0}$

## 2nd step:

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# Transient Assessment From the Error Signal Roots

## 1st step:

**Discrete-time expression of the global error.**

- $E(z) = E_{\Delta i^*}(z)|_{\Delta v_{PCC}=0} + E_{\Delta v_{PCC}}(z)|_{\Delta i^*=0}$

## 2nd step:

**Graphical representation of the error signal roots as a function of the controller gain → Root loci.**

- Influence on the stability, decay rate, damping.

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**Accurate prediction of the error waveform.**

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# Transient Assessment From the Error Signal Roots

## 1st step:

**Discrete-time expression of the global error.**

- $E(z) = E_{\Delta i^*}(z)|_{\Delta v_{PCC}=0} + E_{\Delta v_{PCC}}(z)|_{\Delta i^*=0}$

## 2nd step:

**Graphical representation of the error signal roots as a function of the controller gain → Root loci.**

- Influence on the stability, decay rate, damping.

## 3rd step:

**Accurate prediction of the error waveform.**

- Analysis of the effects of the root position on the transient response.

## 4th step:

**Gain tuning.**

- **Optimization** of the error transient response can be achieved:
  - by making the **poles fast** → large decay rates,
  - by placing the **poles next to zeros** that cancel their effect → **small residues**.

## Transient Assessment From the Error Signal Roots

1st step:

Discrete-time expression of the global error.

2nd step:

Graphical representation of the error signal roots as a function of the controller gain → Root loci.

3rd step:

Accurate prediction of the error waveform.

4th step:

Gain tuning.

Specific  
conditions



Design  
Study

# Tests

1st step:

**Discrete-time expression of the global error.**

2nd step:

**Graphical representation of the error signal roots as a function of the controller gain → Root loci.**

3rd step:

**Accurate prediction of the error waveform.**

4th step:

**Gain tuning.**

Three control situations:

- A. PR controller tuned at  $f_1$ . High sampling frequency ( $f_s = 10$  kHz).
- B. PR controller tuned at  $f_1, f_5$  and  $f_7$ . High sampling frequency ( $f_s = 10$  kHz).
- C. PR controller tuned at  $f_1$ . Low sampling frequency ( $f_s = 2.5$  kHz).

Two transients:

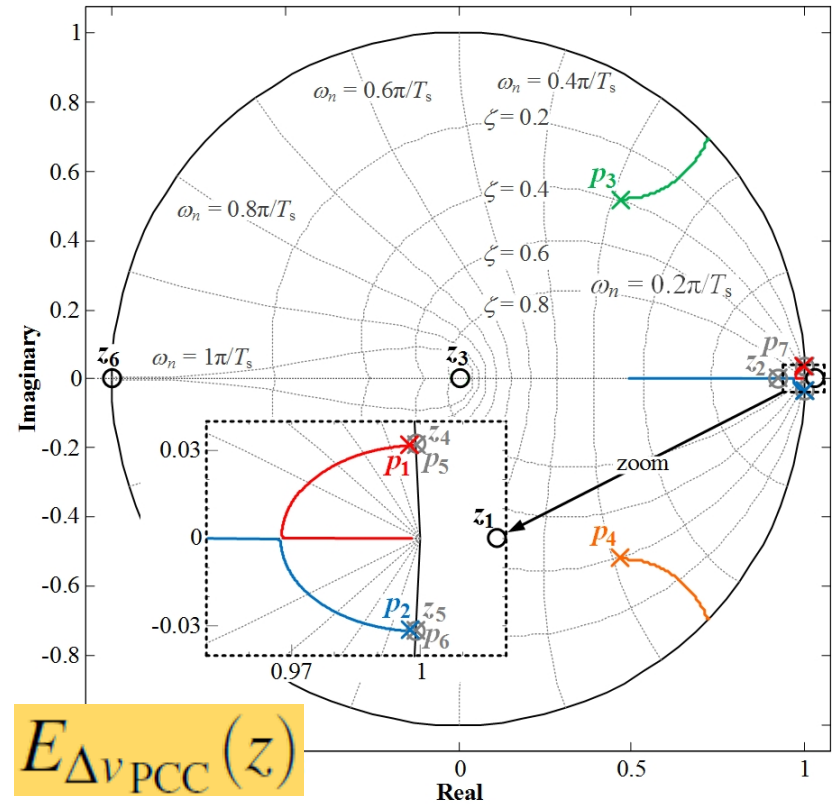
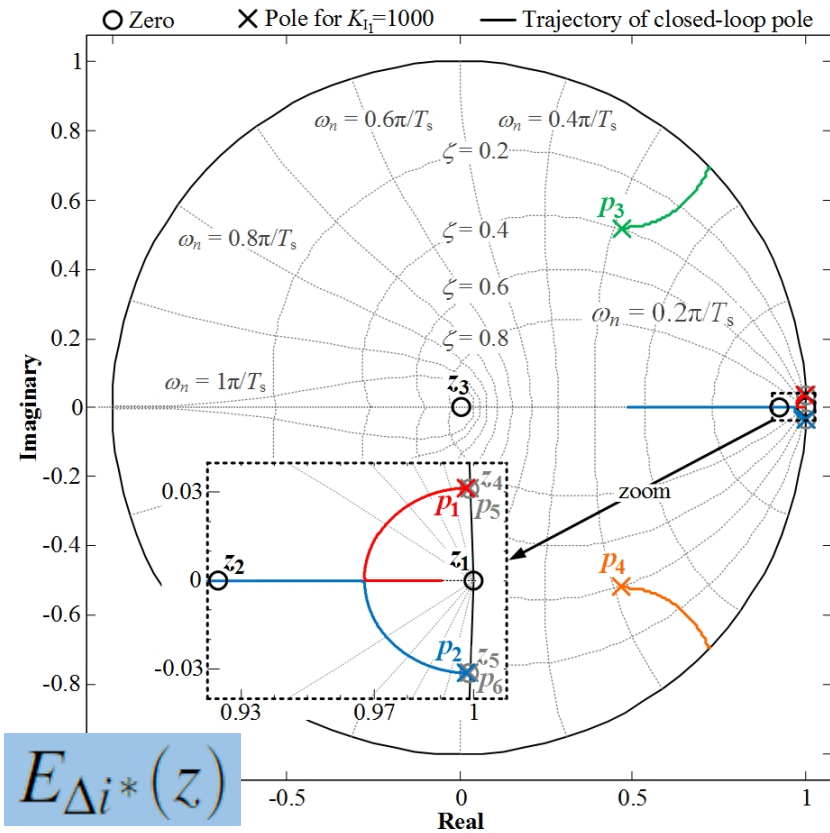
- I. Transients in the current reference: a phase change of  $90^\circ$  in  $i^*$ .  $\Delta i^*(z)$
- II. Transients in the disturbance: a type 'C' sag in  $v_{PCC}$ .  $\Delta v_{PCC}(z)$

# A. PR Controller Tuned at $f_1$ . High $f_s$ (10 kHz)

**2nd step:**

Graphical representation of the error signal roots as a function of the controller gain  $\rightarrow$  Root loci.

Pag.  
90-94



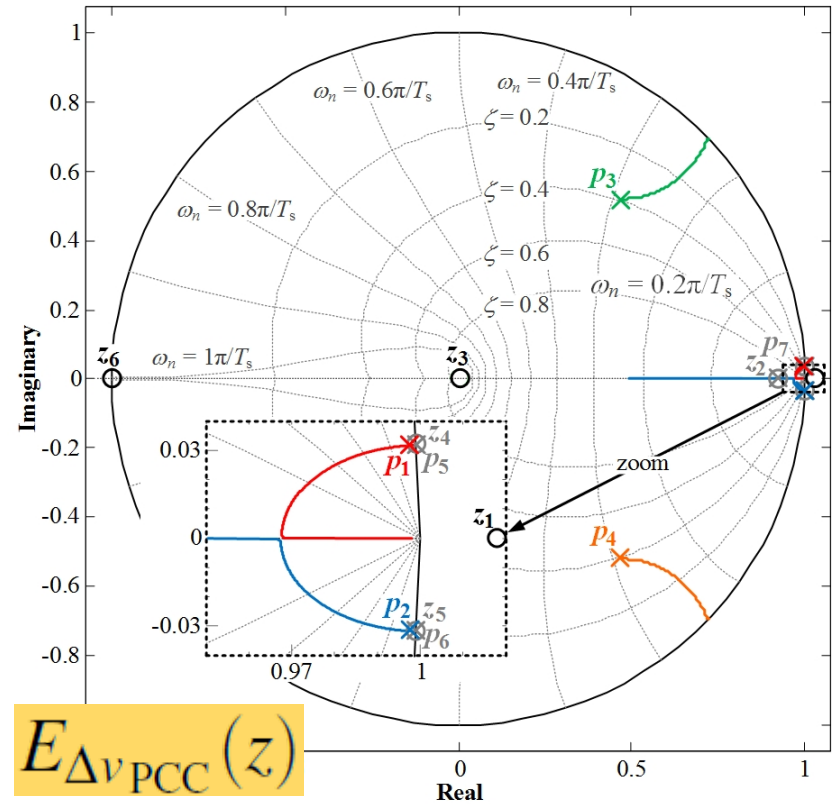
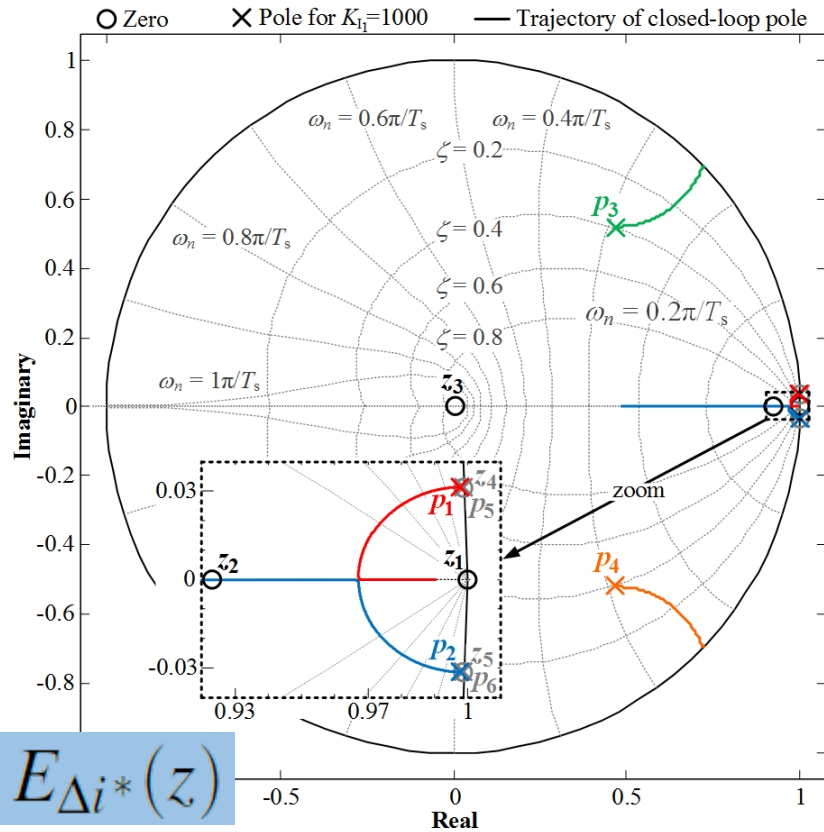
# A. PR Controller Tuned at $f_1$ . High $f_s$ (10 kHz)

**3rd step:**

**Analysis of the effects of the root position on the transient response.**

Analysis of four values of  $K_{I1}$ .

Pag. 90-94





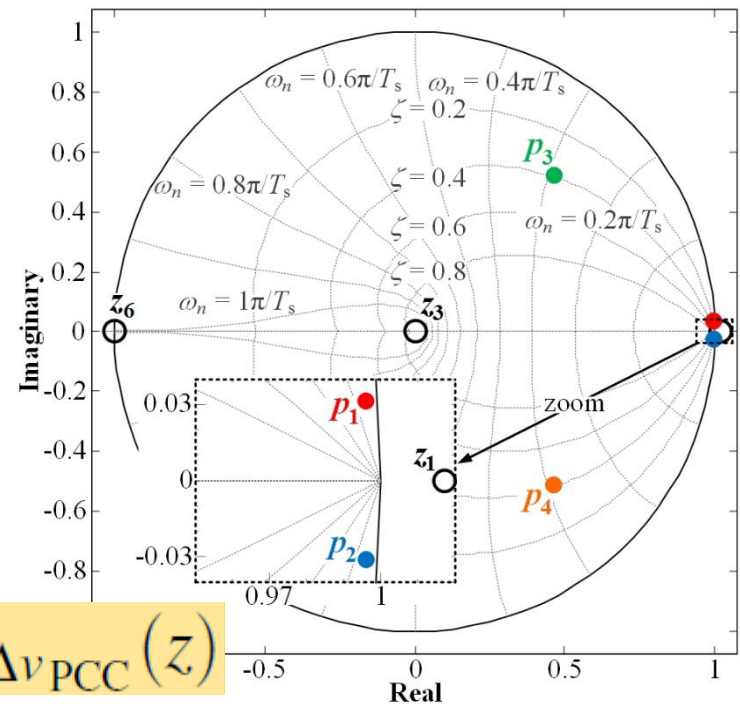
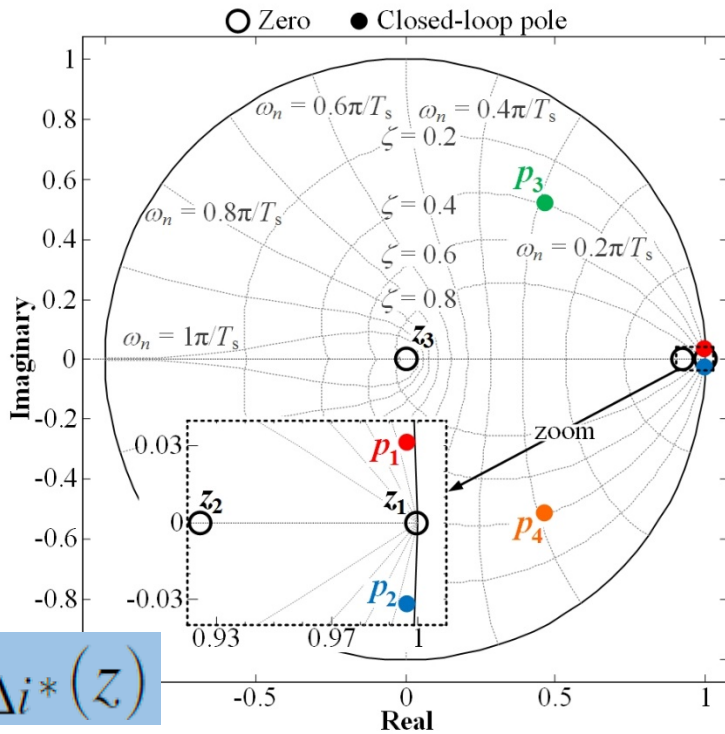
# A. PR Controller Tuned at $f_1$ . High $f_s$ (10 kHz)

Typical value  $K_{I1} = 2000$ :

- $p_1$  &  $p_2$  (dominant) slow and oscillating;
- $p_3$  &  $p_4$  faster than  $p_1$  &  $p_2$ , and also oscillating.

➔ Not a good choice.

Pag.  
93-96



## A. PR Controller Tuned at $f_1$ . High $f_s$ (10 kHz)

$K_{I1} = 17645$ :

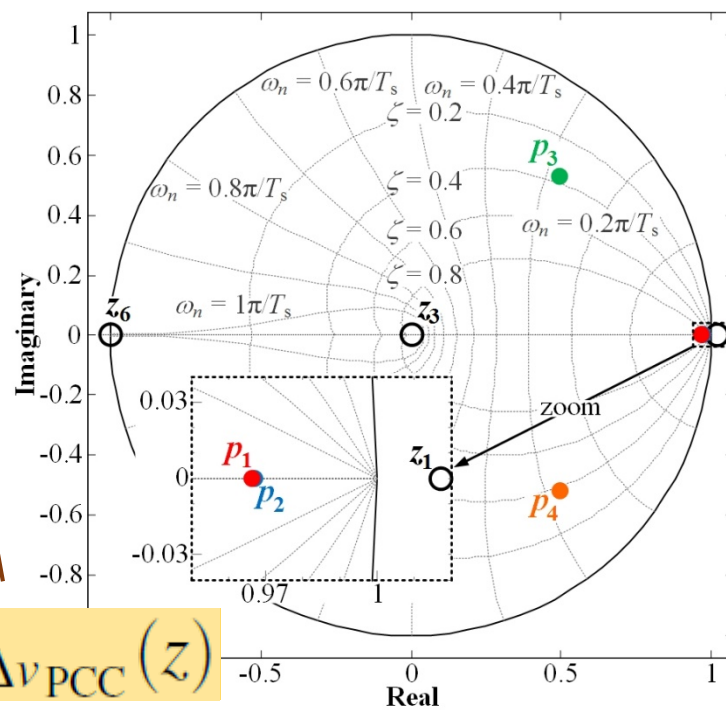
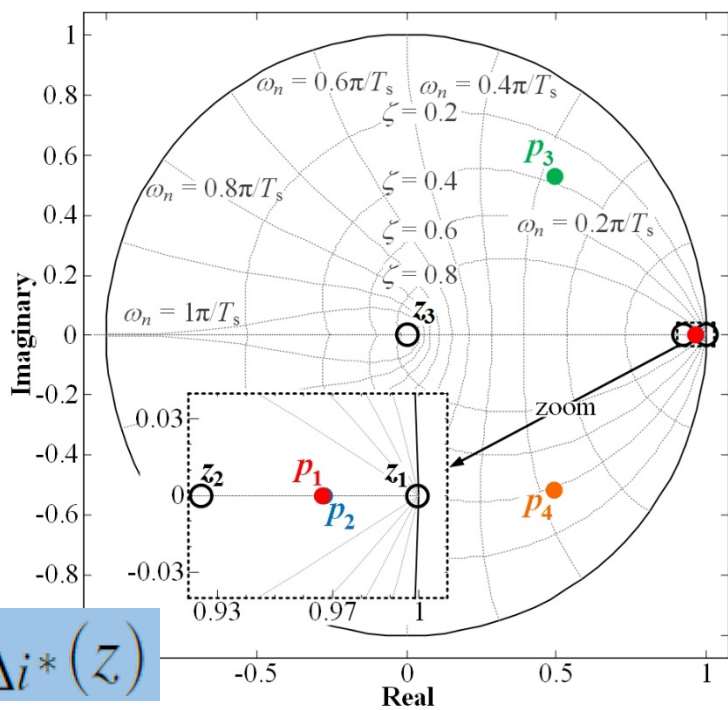
- $p_1 = p_2$  dominant and nonoscillating;
- $p_3$  &  $p_4$  practically unchanged with respect to those with  $K_{I1} = 2000$ .

Not such a big impact of zeros on the dominant poles.

Optimal for changes in the disturbance.

Fastest position of  $p_1$ .

Pag. 93-96



# A. PR Controller Tuned at $f_1$ . High $f_s$ (10 kHz)

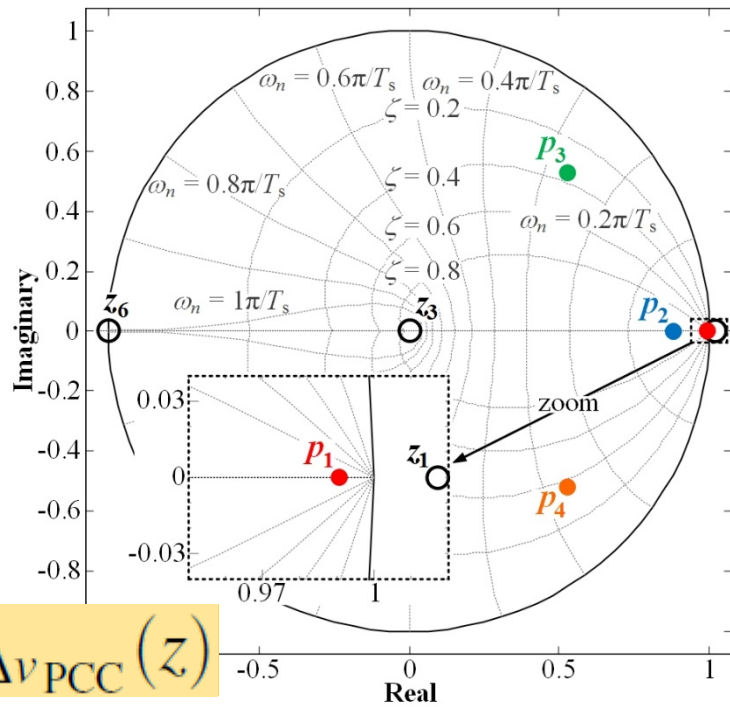
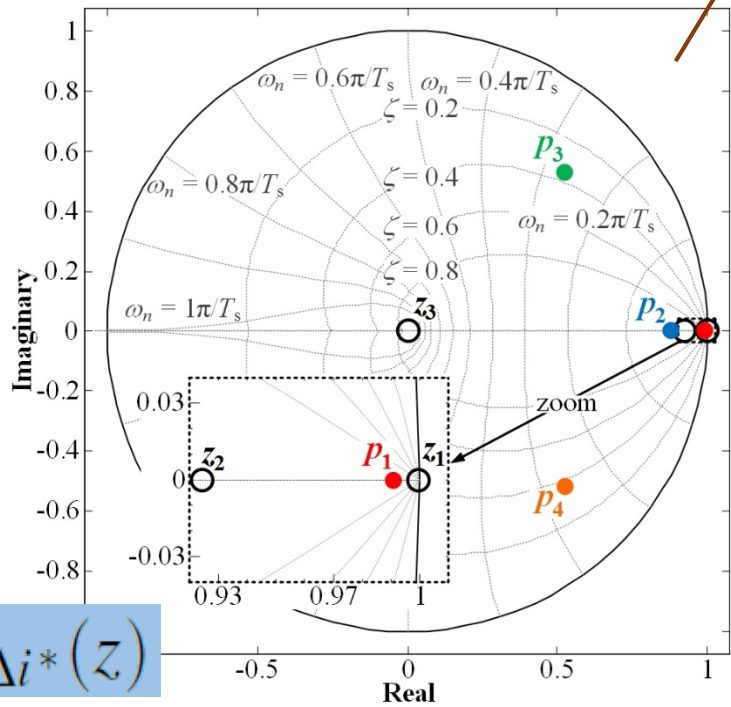
$K_{I1} = 34000$ :

- $p_1 > p_2$  dominant and nonoscillating;
- $p_3$  &  $p_4$  practically unchanged with respect to those with  $K_{I1} = 2000$ .

Zeros closer to the dominant poles.

Optimal for changes in the current reference.

Pag. 93-96



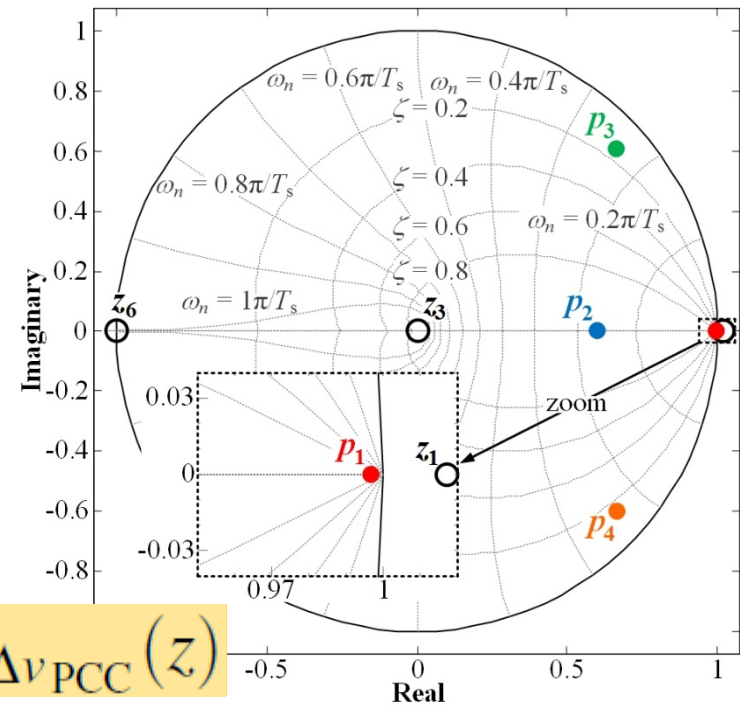
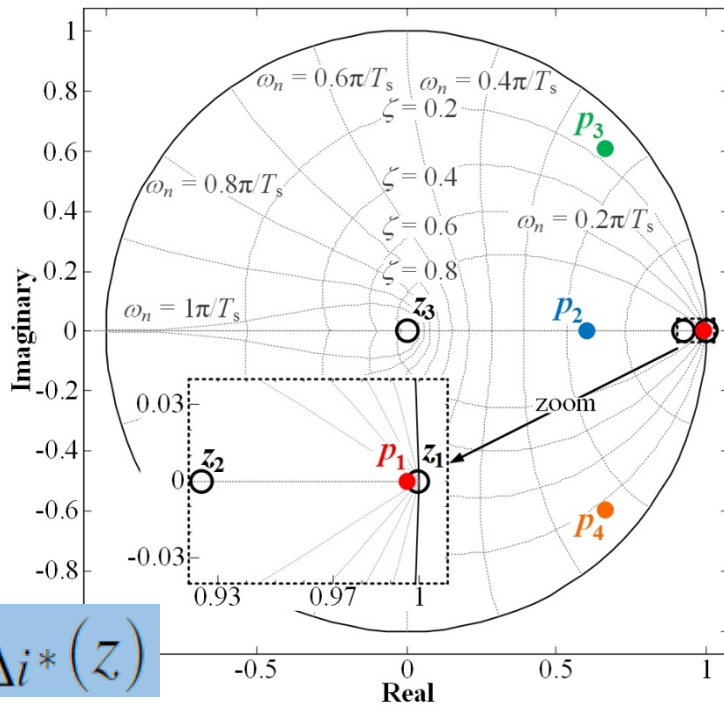
# A. PR Controller Tuned at $f_1$ . High $f_s$ (10 kHz)

$K_{I1} = 100000$ :

- $p_1$  slower and almost cancelled by a zero;
- $p_2$  faster and nonoscillating;
- $p_3$  &  $p_4$  dominant and very oscillating.

➔ Not a good choice.

Pag.  
93-96



## A. PR Controller Tuned at $f_1$ . High $f_s$ (10 kHz)

4th step:

Gain tuning.

Pag.  
93-96

A tradeoff is  
needed.

$$E_{\Delta i^*}(z)$$

Optimal gain

$$K_{I_1} = 34000$$

$$E_{\Delta v_{PCC}}(z)$$

$$K_{I_1} = 17645$$

## A. PR Controller Tuned at $f_1$ . High $f_s$ (10 kHz)

4th step: Gain tuning.

Pag.  
93-96

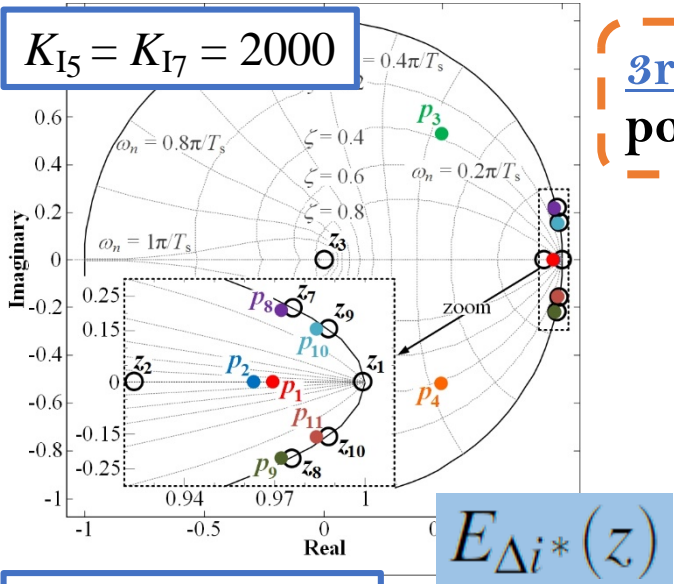
A tradeoff is  
needed.

	Optimal gain
$E_{\Delta i^*}(z)$	$K_{I_1} = 34000$
$E_{\Delta v_{PCC}}(z)$	$K_{I_1} = 17645$

The disturbance rejection response is usually more critical than the reference tracking one.



## B. PR Controller Tuned at $f_1, f_5$ and $f_7$ . High $f_s$ (10 kHz)

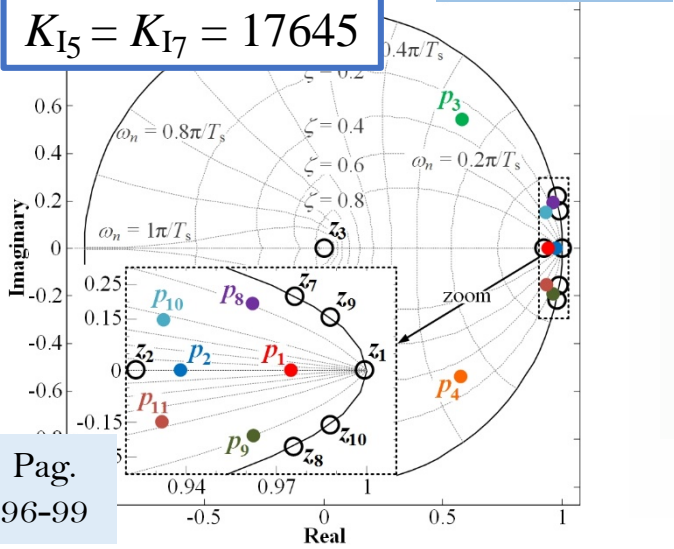


**3rd step:** Analysis of the effects of the root position on the transient response.

$K_{I1} = 17645 +$  two different values of  $K_{I5}$  and  $K_{I7}$ .

New zeros at the unit circle boundary:

- Impossible to place the new poles far from the unit circle boundary and at the same time, next to those zeros.
- Difficult to draw conclusions from the root loci.



Accurate prediction of the error waveform.

Partial-fraction expansions: poles & residues.

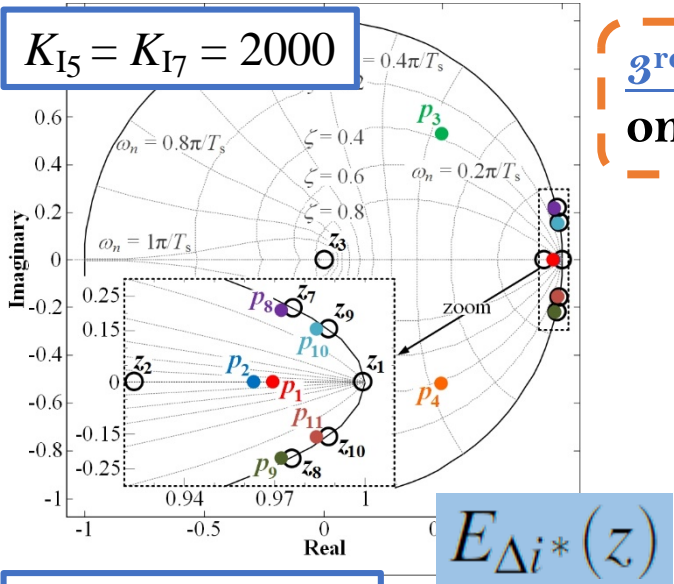
Overshoot & settling time.

4th step:

Gain selection.



## B. PR Controller Tuned at $f_1, f_5$ and $f_7$ . High $f_s$ (10 kHz)

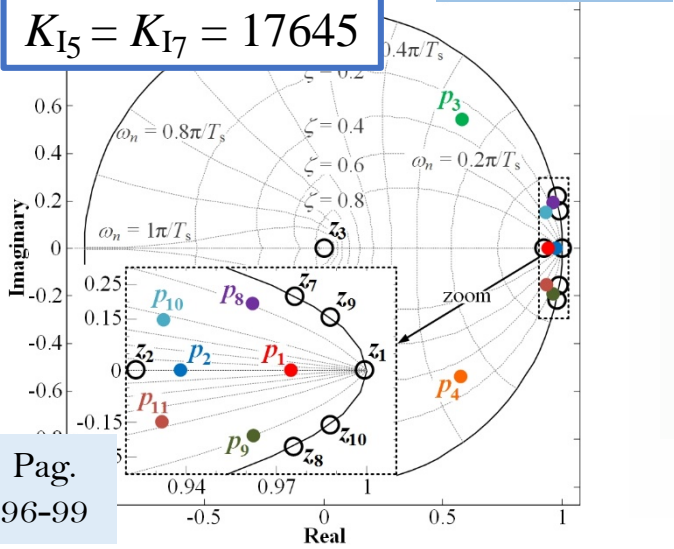


**3<sup>rd</sup> step:** Analysis of the effects of the root position on the transient response.

$K_{I1} = 17645 +$  two different values of  $K_{I5}$  and  $K_{I7}$ .

**New zeros at the unit circle boundary:**

- Impossible to place the new poles far from the unit circle boundary and at the same time, next to those zeros.
- Difficult to draw conclusions from the root loci.



Accurate prediction of the error waveform.

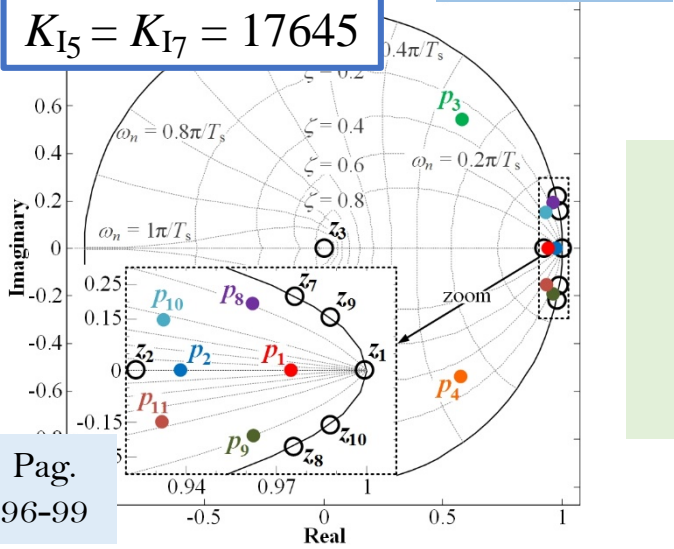
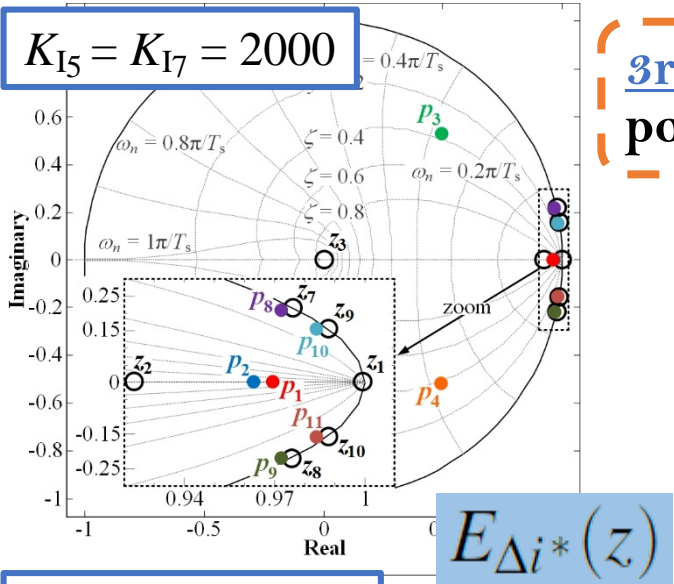
Partial-fraction expansions: poles & residues.

Overshoot & settling time.

4<sup>th</sup> step:

Gain selection.

## B. PR Controller Tuned at $f_1, f_5$ and $f_7$ . High $f_s$ (10 kHz)



**3rd step:** Analysis of the effects of the root position on the transient response.

$K_{I1} = 17645 +$  two different values of  $K_{I5}$  and  $K_{I7}$ .

**New zeros at the unit circle boundary:**

- Impossible to place the new poles far from the unit circle boundary and at the same time, next to those zeros.
- Difficult to draw conclusions from the root loci.

**Accurate prediction of the error waveform.**

Partial-fraction expansions: poles & residues.

Settling time & overshoot.

**4th step:**  
Gain selection.

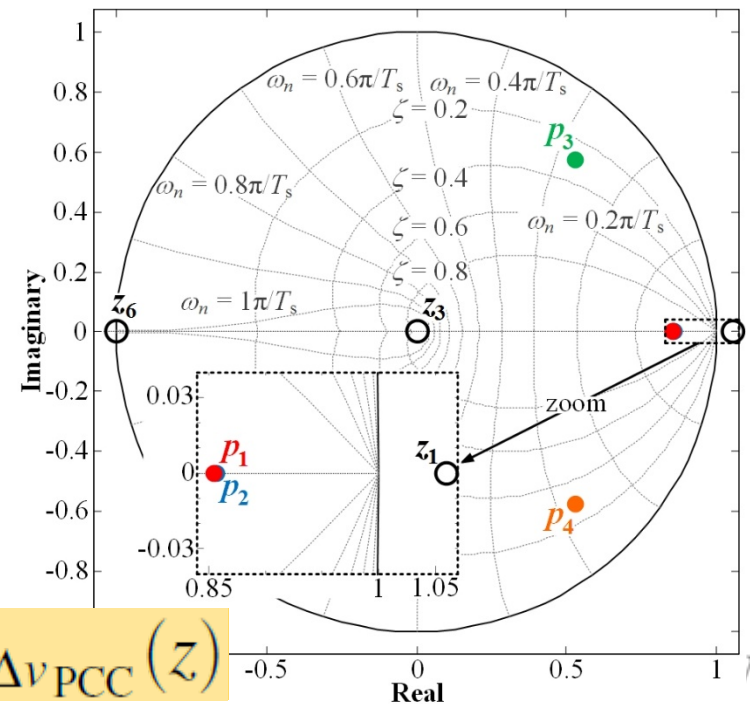
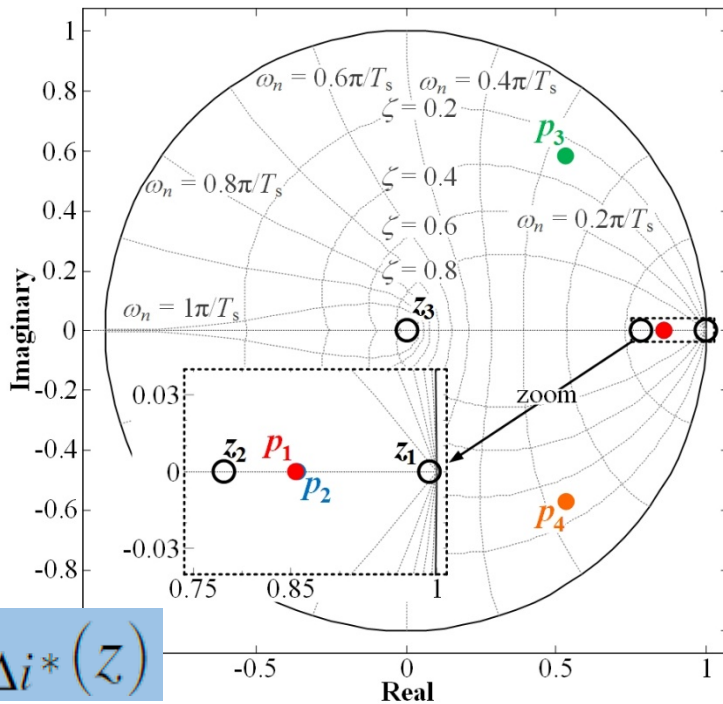
$K_{I5} = K_{I7} = 17645$

## C. PR Controller Tuned at $f_1$ . Low $f_s$ (2.5 kHz)

### Gain tuning.

- To favor the settling time of the disturbance rejection response.
- $K_{I1} = 5262 \rightarrow p_1 = p_2$  dominant and **nonoscillating**.
- Compared to the corresponding ones at 10 kHz,  $p_3$  &  $p_4$  have **more impact at 2.5 kHz**, due to the **delay effect**.

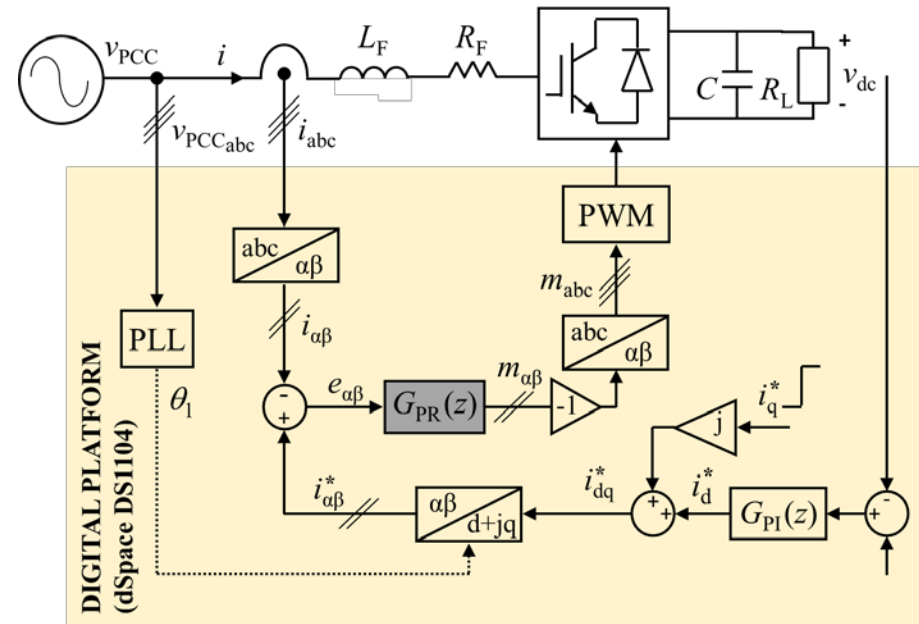
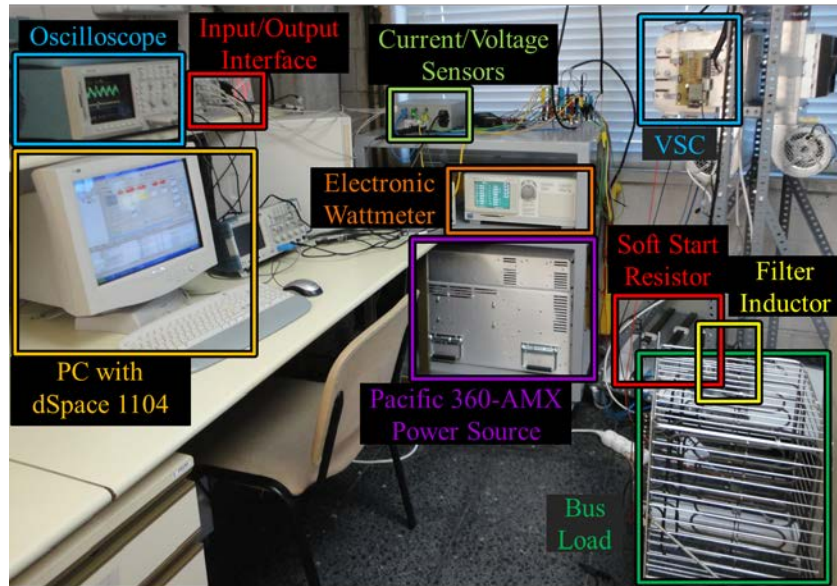
Pag.  
96-99



$$E_{\Delta i}^*(z)$$

$$E_{\Delta v_{PCC}}(z)$$

# Experimental Setup



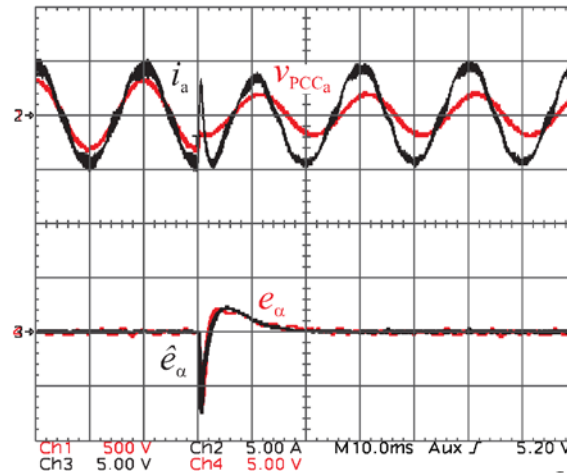
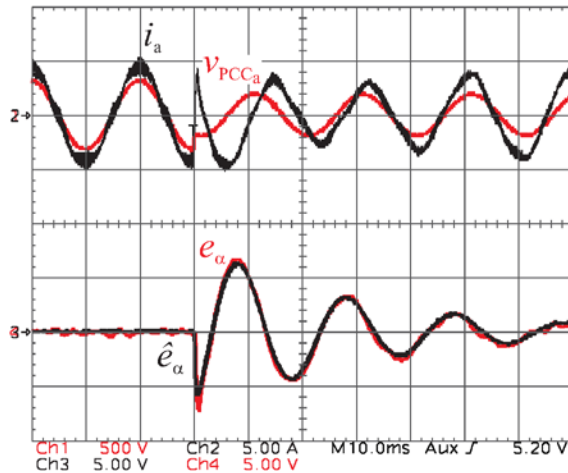
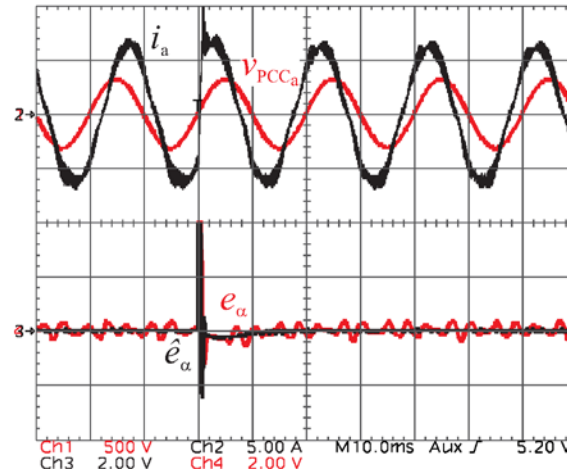
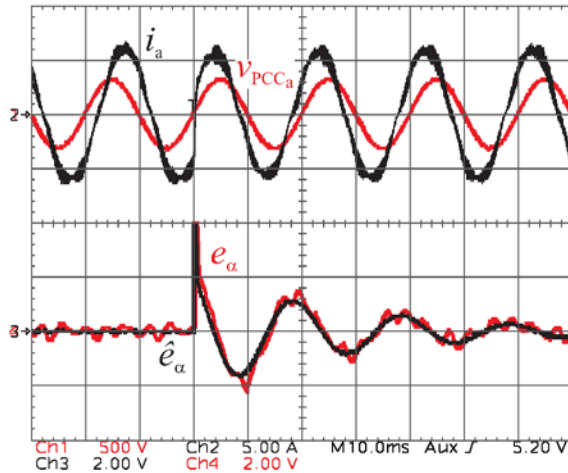
- VSC working as a rectifier.
- Control implemented in dSpace DS1104.
- The Pacific 360-AMX 3-ph linear power source is used to supply the ac voltages and to program the voltage sags.
- $i_q^*$  is set manually to perform transients in the current reference.
- $i_d^*$  is set through an outer loop which controls  $v_{dc}$ .



# A. PR Controller Tuned at $f_1$ . High $f_s$ (10 kHz)

$K_{I1} = 2000$

$K_{I1} = 17645$



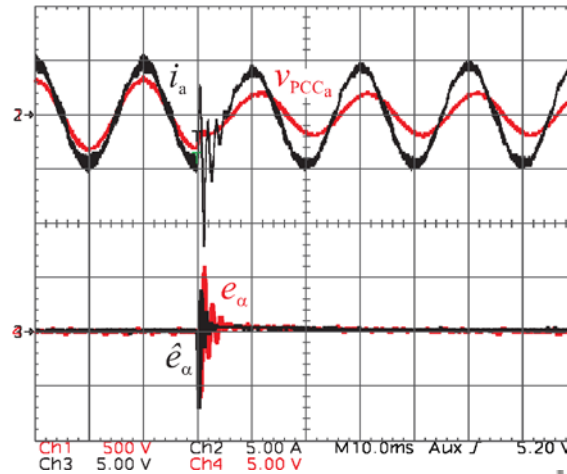
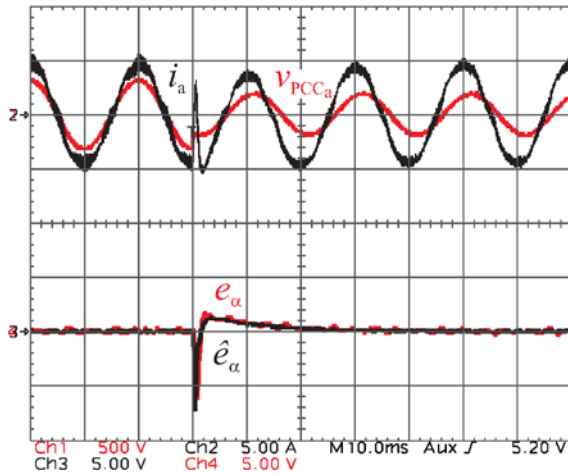
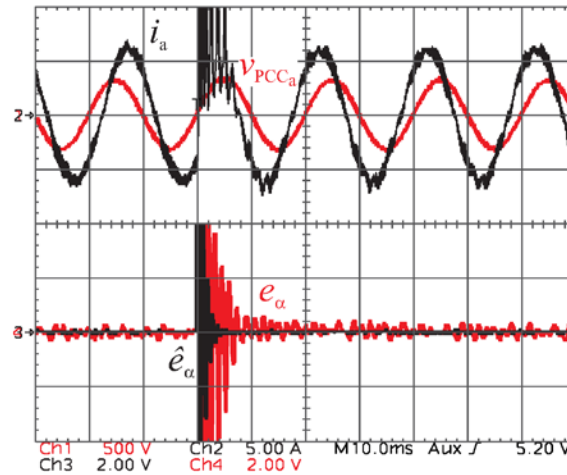
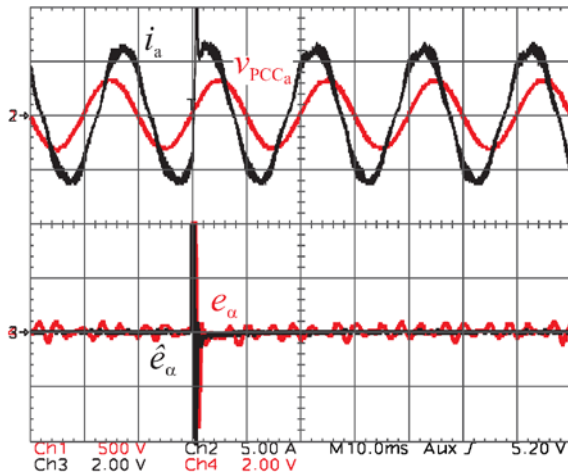
$$E_{\Delta i^*}(z)$$

$$E_{\Delta v_{PCC}}(z)$$

## A. PR Controller Tuned at $f_1$ . High $f_s$ (10 kHz)

$K_{I1} = 34000$

$K_{I1} = 100000$



$$E_{\Delta i^*}(z)$$

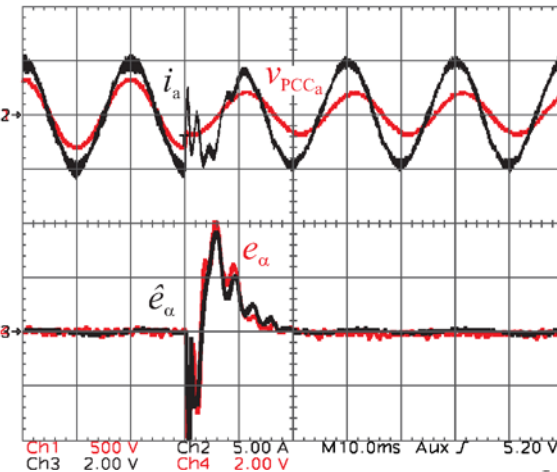
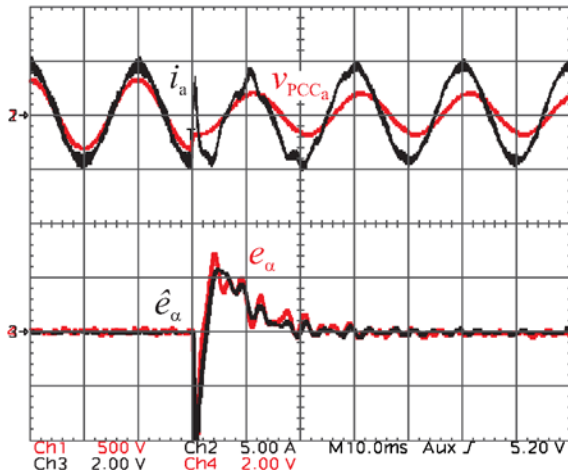
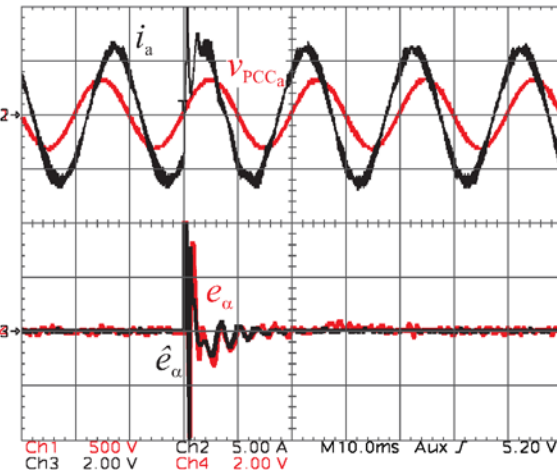
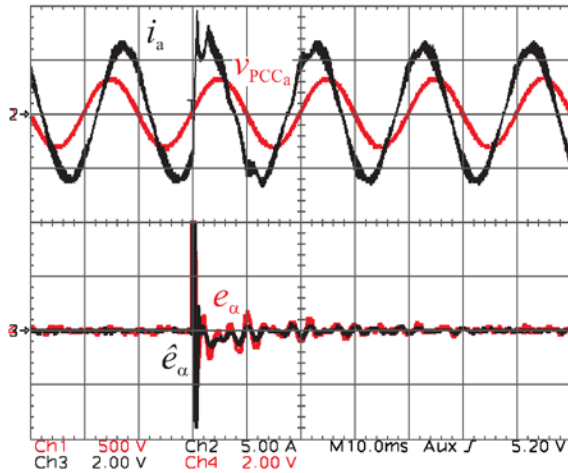
$$E_{\Delta v_{PCC}}(z)$$

Pag.  
101-104

## B. PR Controller Tuned at $f_1, f_5$ and $f_7$ . High $f_s$ (10 kHz)

$$K_{I5} = K_{I7} = 2000$$

$$K_{I5} = K_{I7} = 17645$$



$$E_{\Delta i^*}(z)$$

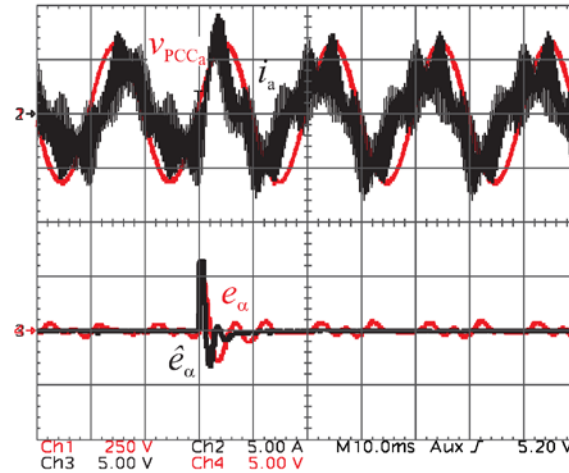
$$E_{\Delta v_{PCC}}(z)$$



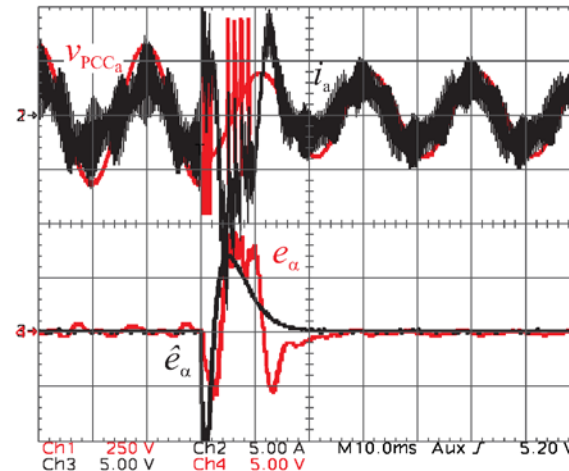
## C. PR Controller Tuned at $f_1$ . Low $f_s$ (2.5 kHz)

$$K_{I1} = 5262$$

$$E_{\Delta i^*}(z)$$



$$E_{\Delta v_{PCC}}(z)$$



## Conclusions of Chapter 4

- A **methodology to assess and optimize** the transient response of **PR controllers** has been developed. It is **based on** the **accurate modeling** (including the delay effects) **and study** of the **error signal roots caused** either by
  - **Transients** in the **current reference**
  - **Changes** in the **disturbance** (voltage sags at the PCC).
- **Different** significant situations considering very **demanding scenarios** have been **analyzed and tested**.
- **Optimal gains** result from a **tradeoff** between the **two types of transients**, in **favor** of the most critical one, which is the **disturbance** one.
- It is concluded that **precisely tuned PR controllers** are a **suitable** option to **fulfill** the **GC** requirements in terms of **transient response**.

# Outline

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1. Introduction
2. Equivalent Loss Resistance Estimation of Grid-Tied Converters for Current Control Analysis and Design
3. A Method for Identification of the Equivalent Inductance and Resistance in the Plant Model of Current-Controlled Grid-Tied Converters
4. Assessment and Optimization of the Transient Response of Proportional-Resonant Current Controllers for Distributed Power Generation Systems
5. **Transient Response Evaluation of Stationary-Frame Resonant Current Controllers for Grid-Connected Applications**
  - Introduction
  - Design Study
  - Experimental Results
  - Conclusion
6. Conclusions and Future Research


## Framework

---

- **VPI controllers** are **alternative resonant regulators** to PR ones.
- Some works prove **they could provide higher stability margins** than PR ones and hence, **more damped responses**.
- **Studies** about the utilization of **VPI controllers** for **current control** in **renewable energy applications** are **lacking**. There is **not a methodology** for VPI controller **tuning oriented** to the **transient response optimization** of command tracking and disturbance rejection.

## Framework

- **VPI controllers** are **alternative resonant regulators** to PR ones.
- Some works prove **they could provide higher stability margins** than PR ones and hence, **more damped responses**.
- **Studies** about the utilization of **VPI controllers** for **current control** in **renewable energy applications** are **lacking**. There is **not a methodology** for VPI controller **tuning oriented** to the **transient response optimization** of command tracking and disturbance rejection.

- 
- **Application to VPI controllers** of the **methodology** described in **Chapter 4**.
  - **Comparison between PR and VPI controllers**.

## Methodology & Tests

1st step:

**Discrete-time expression of the global error.**

2nd step:

**Graphical representation of the error signal roots as a function of the controller gain → Root loci.**

3rd step:

**Accurate prediction of the error waveform.**

4th step:

**Gain tuning.**

Four control situations:

- A. Resonant filters tuned at  $f_1$ . High sampling frequency ( $f_s = 10$  kHz).
- B. Resonant filters tuned at  $f_1, f_5$  and  $f_7$ . High sampling frequency ( $f_s = 10$  kHz).
- C. Resonant filters tuned at  $f_1$ . Low sampling frequency ( $f_s = 2.5$  kHz).
- D. Effect of a feed-forward path.

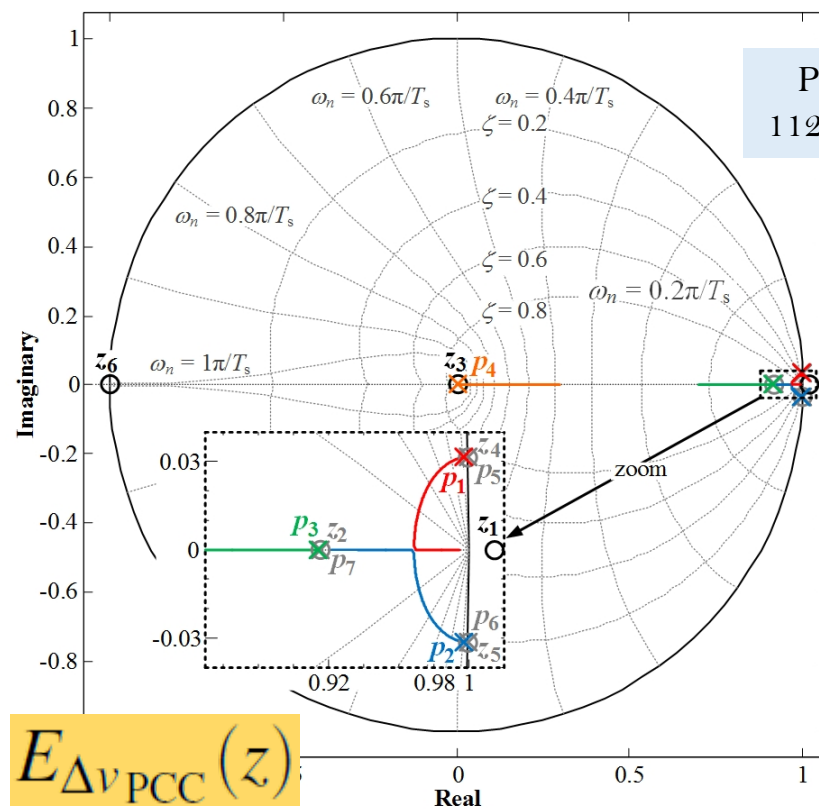
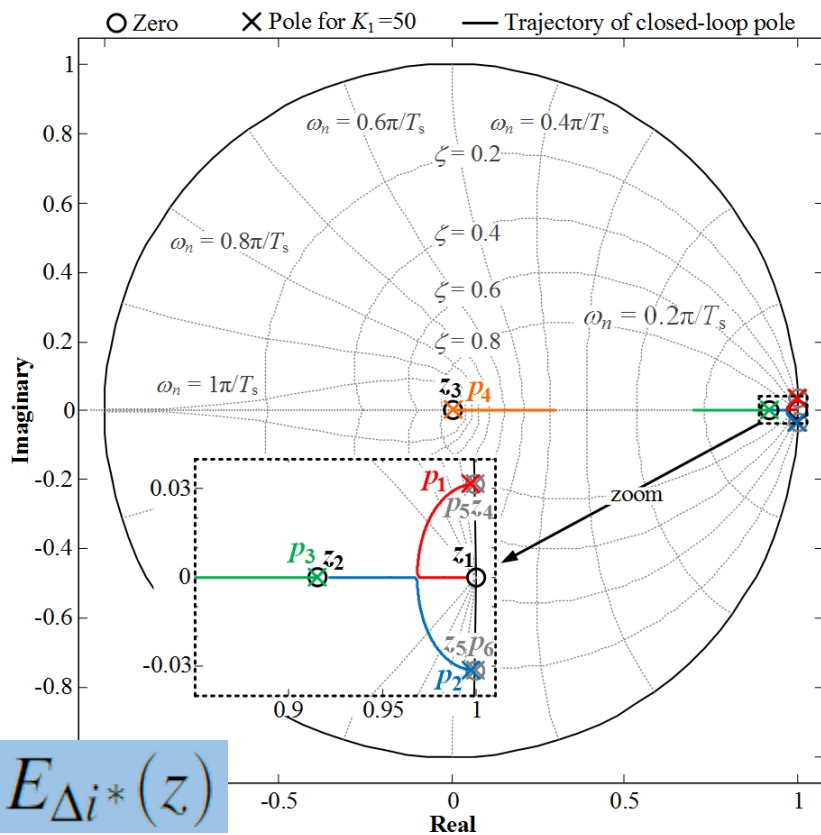
Two transients:

- I. Transients in the current reference: a phase change of  $90^\circ$  in  $i^*$ .  $\Delta i^*(z)$
- II. Transients in the disturbance: a type 'C' sag in  $v_{PCC}$ .  $\Delta v_{PCC}(z)$

# A. VPI Controller Tuned at $f_1$ . High $f_s$ (10 kHz)

**2nd step:**

Graphical representation of the error signal roots as a function of the controller gain  $\rightarrow$  Root loci.



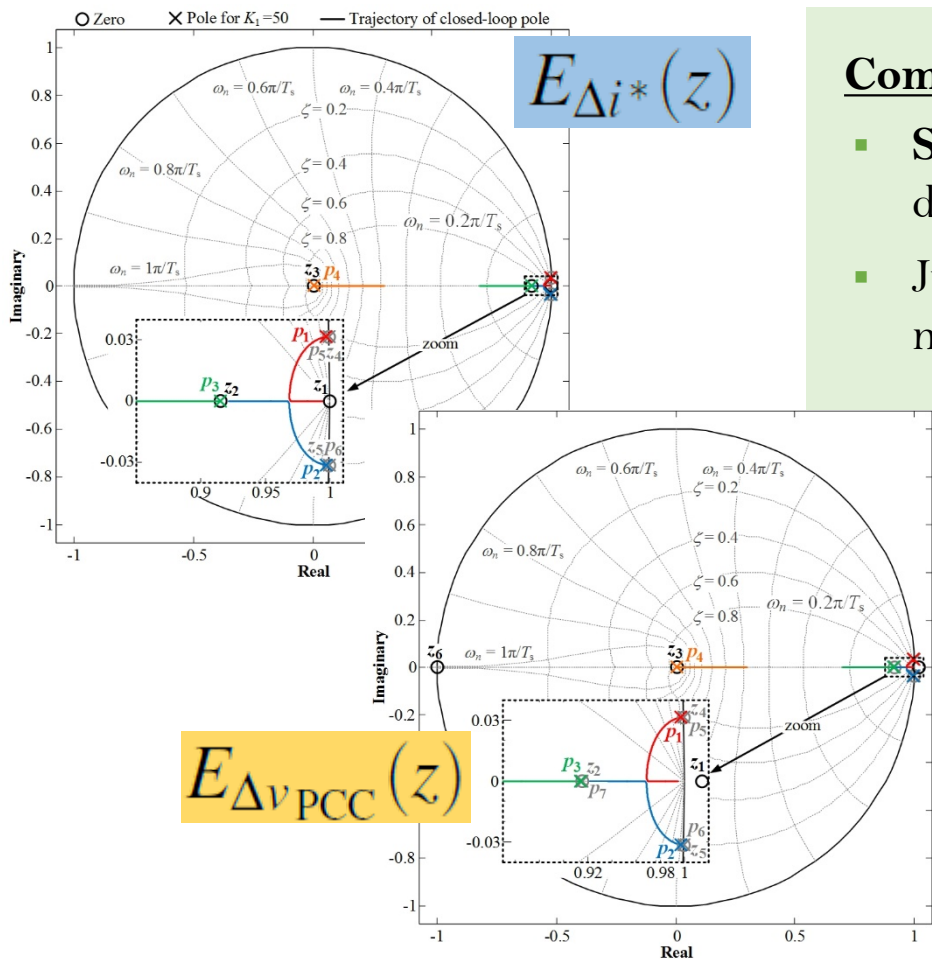
Pag. 112-115



# A. VPI Controller Tuned at $f_1$ . High $f_s$ (10 kHz)

**3rd step:**

**Analysis of the effects of the root position on the transient response.**



## Comparing with the analysis of the PR controller:

- Same number of roots (numerators and denominators of the same order).
- Just the roots that depend on the controller numerator are different  $\rightarrow p_1, p_2, p_3$  &  $p_4$
- $p_1$  &  $p_2$  (dominant poles): behave similarly with an increasing gain.
- $p_3$  &  $p_4$ : behave differently.
  - PR controller  $\rightarrow$  Complex
  - VPI controller  $\rightarrow$  Real; plant dynamics cancellation

Pag. 112-115

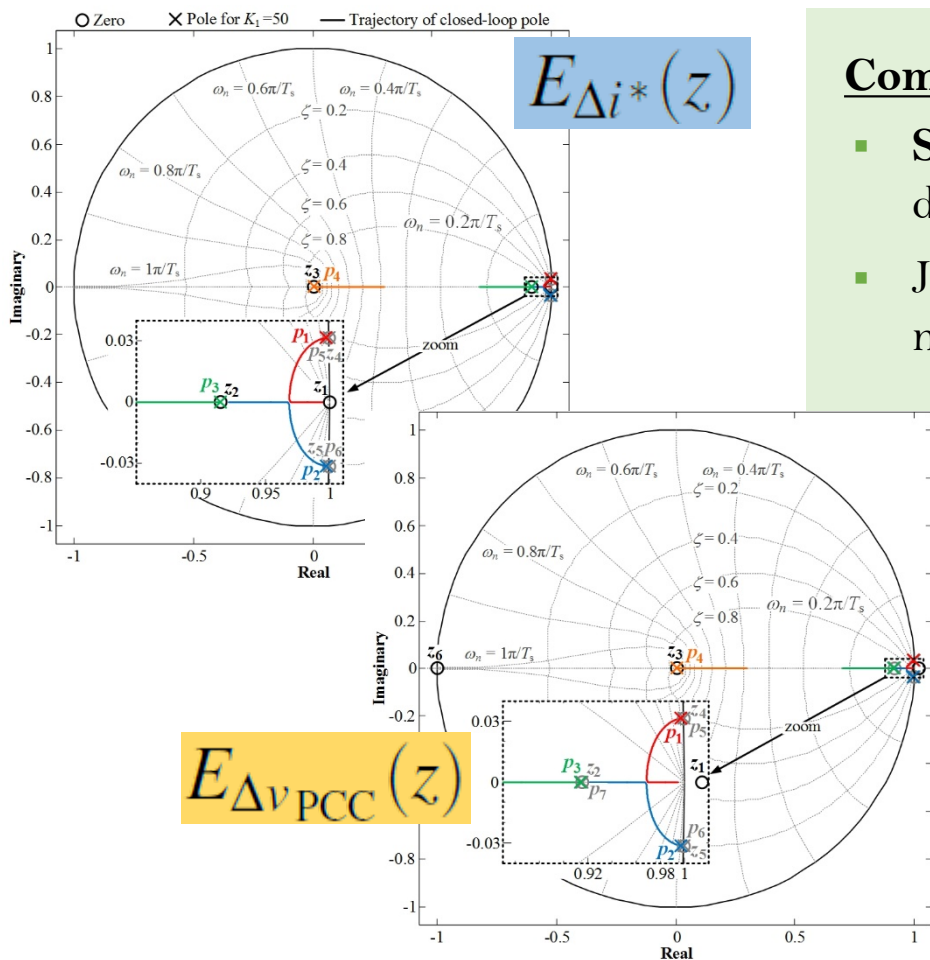
$p_3 \leftarrow z_2$   
 $p_4 \leftarrow z_3$



# A. VPI Controller Tuned at $f_1$ . High $f_s$ (10 kHz)

## 3rd step:

Analysis of the effects of the root position on the transient response.



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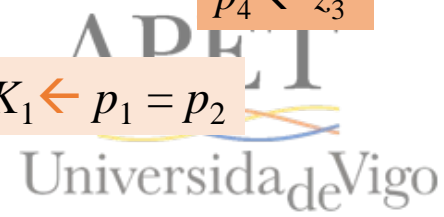
Pag. 112-115

$p_3 \leftarrow z_2$   
 $p_4 \leftarrow z_3$

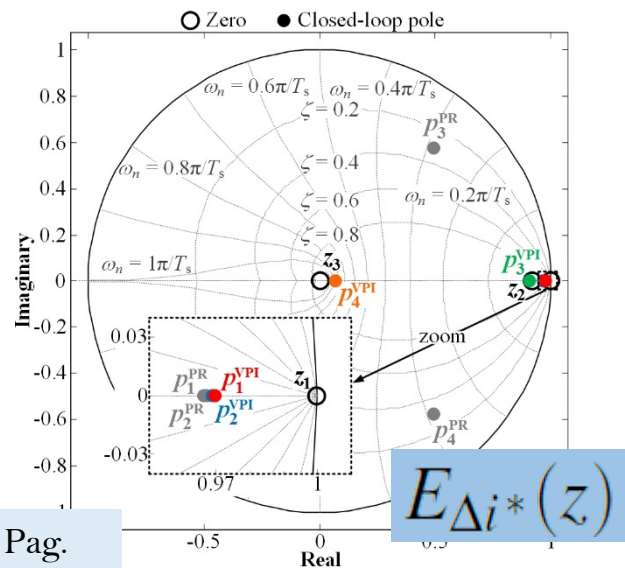
## 4th step:

Gain tuning.

$K_1 \leftarrow p_1 = p_2$

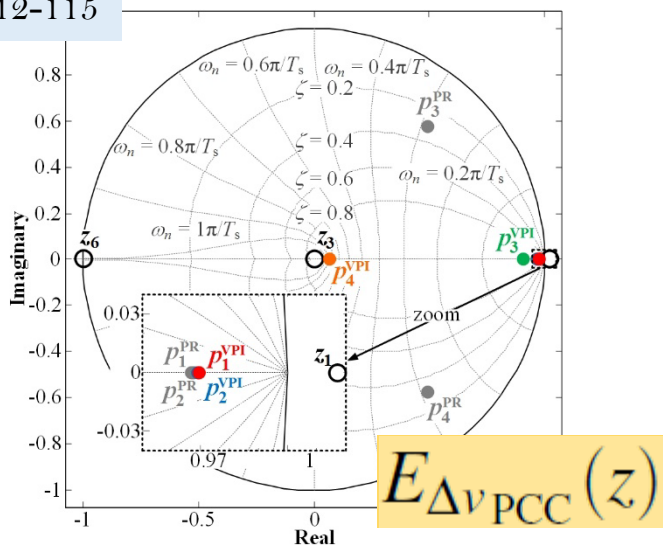


# A. Resonant Controllers Tuned at $f_1$ . High $f_s$ (10 kHz)



Pag.

112-115



## Pole position (decay rate)

- $p_1$  &  $p_2$  (dominant poles)  $\rightarrow$  slower with the VPI controller
- $p_3$  &  $p_4 \rightarrow p_3$  slower and  $p_4$  faster with the VPI controller

## Residues in the reference change (damping)

- $p_1$  &  $p_2$  (dominant poles)  $\rightarrow$  bigger residues with the VPI controller
- $p_3$  &  $p_4 \rightarrow$  smaller residues with the VPI controller

## Residues in the disturbance change (damping)

- $p_1, p_2$  &  $p_3 \rightarrow$  larger residues with the VPI controller
- $p_4 \rightarrow$  smaller residues with the VPI controller

## B. Resonant Controllers Tuned at $f_1, f_5$ & $f_7$ . High $f_s$ (10 kHz)

- **Adding** more **resonant filters** with high gains **affects the position** of the dominant **poles**  $p_1$  &  $p_2$ , as well as those of  $p_3$  &  $p_4$  with both controllers → **Smaller values** of  $K_{I1}$  and  $K_1$  **are needed** to achieve  $p_1 = p_2$ .
- For  $p_1, p_2, p_3$  &  $p_4$ , the conclusions are the same as in the previous case.
- For **the additional poles**, the **differences** are **marginal**.

Pag.  
115, 116

## C. Resonant Controllers Tuned at $f_1$ . Low $f_s$ (2.5 kHz)

- As  $f_s$  decreases, the **delay effects** caused by the **discrete-time implementation** become **more noticeable**. The **discretization method** applied to the resonant controllers **affects the system dynamics**. → **The best option is assessed**.
- **More similarities** in the root loci of **both controllers** at this  $f_s$ .
  - The **dominant poles**  $p_1$  &  $p_2$  are **slightly faster with the PR controller** → slightly faster reference tracking and disturbance rejection responses.
  - **Smaller residues** of the dominant poles with the PR controller → **smaller overshoot**.
  - Initial high-frequency oscillations in the **reference change** with the PR controller (due to larger residues of  $p_3$  &  $p_4$ ) → it will increase the overshoot.

Pag.  
116-118

## B. Resonant Controllers Tuned at $f_1, f_5$ & $f_7$ . High $f_s$ (10 kHz)

- **Adding** more **resonant filters** with high gains **affects the position** of the dominant **poles**  $p_1$  &  $p_2$ , as well as those of  $p_3$  &  $p_4$  with both controllers → **Smaller values** of  $K_{I1}$  and  $K_1$  **are needed** to achieve  $p_1 = p_2$ .
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Pag.  
115, 116

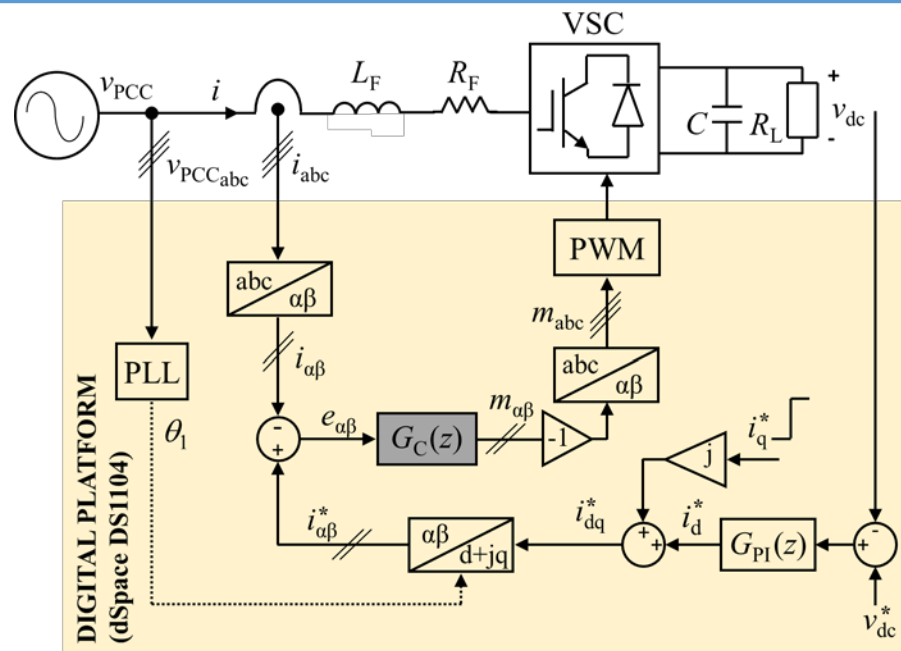
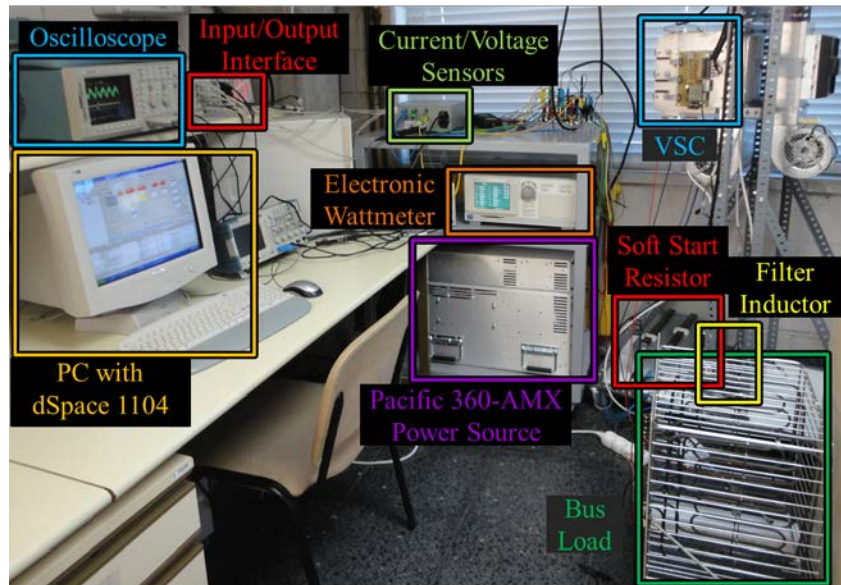
## C. Resonant Controllers Tuned at $f_1$ . Low $f_s$ (2.5 kHz)

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  - Initial high-frequency oscillations in the **reference change** with the PR controller (due to **larger residues of  $p_3$  &  $p_4$** ) → it will **increase the overshoot**.

Pag.  
116-118



# Experimental Setup

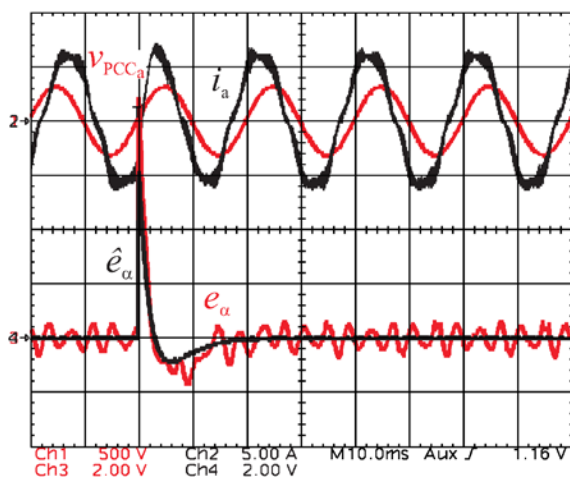


- VSC working as a rectifier.
- Control implemented in dSpace DS1104.
- The Pacific 360-AMX 3-ph linear power source is used to supply the ac voltages and to program the voltage sags.
- $i_q^*$  is set manually to perform transients in the current reference.
- $i_d^*$  is set through an outer loop which controls  $v_{dc}$ .

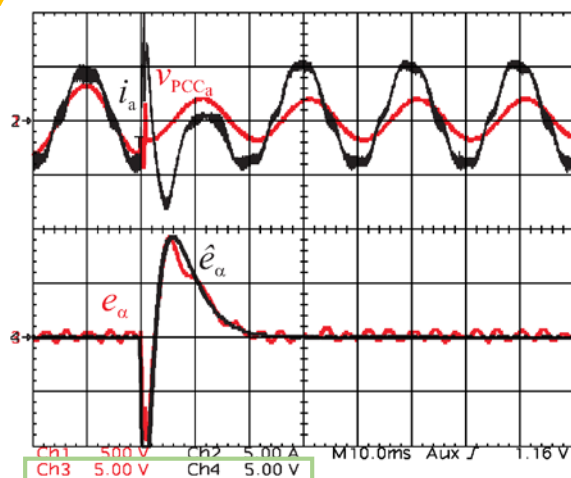
# A. Resonant Controllers Tuned at $f_1$ . High $f_s$ (10 kHz)

VPI

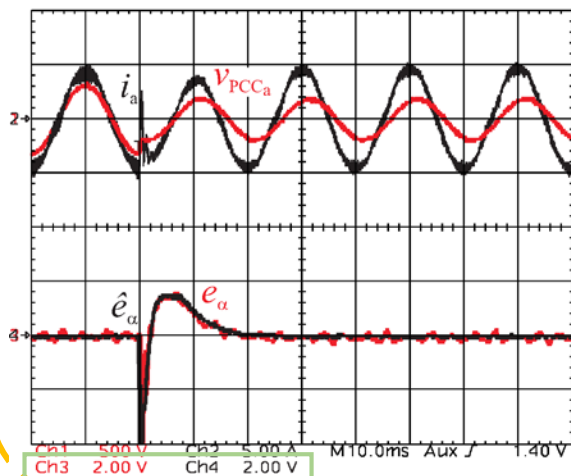
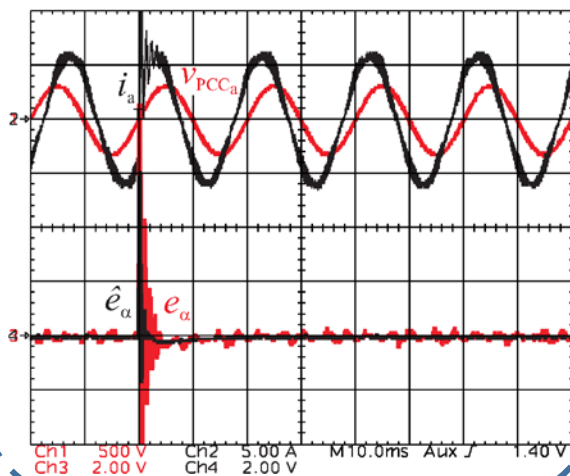
$$E_{\Delta i^*}(z)$$



$$E_{\Delta v_{PCC}}(z)$$



PR

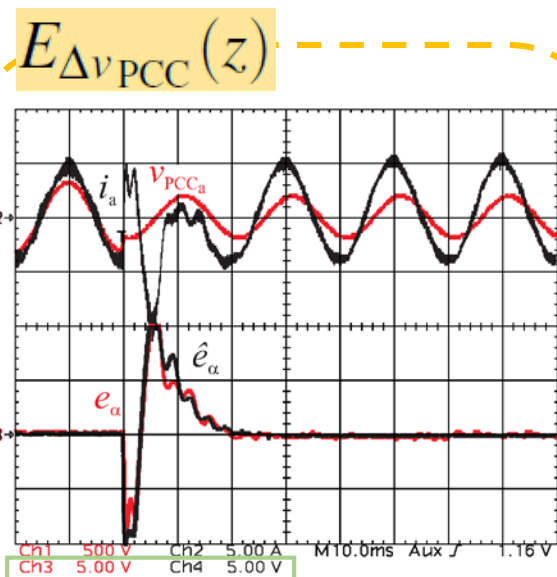
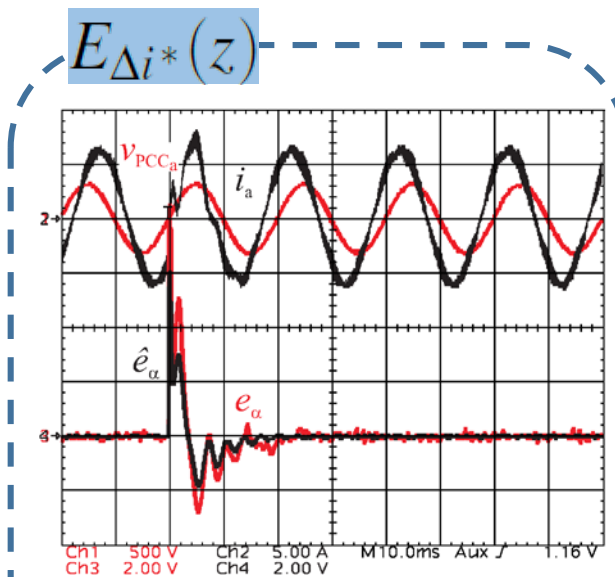


Pag.  
121-125

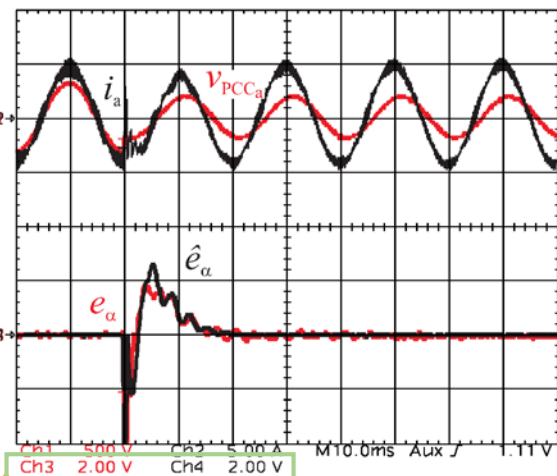
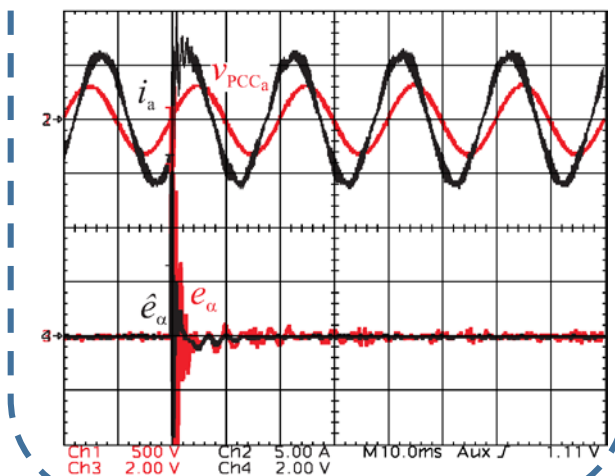


B. Resonant Controllers Tuned at  $f_1$ ,  $f_5$  and  $f_7$ . High  $f_s$  (10 kHz)

VPI



PR

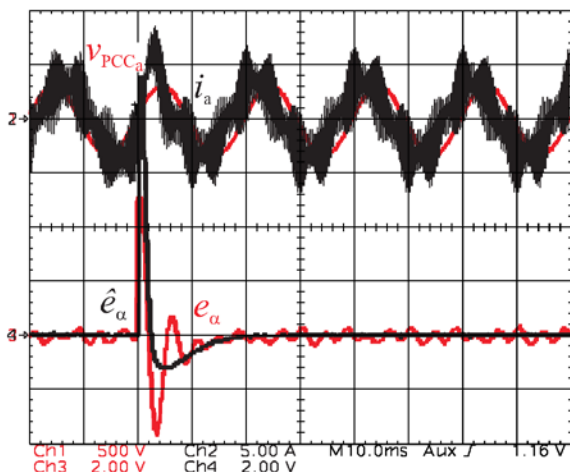


Pag.  
121-125

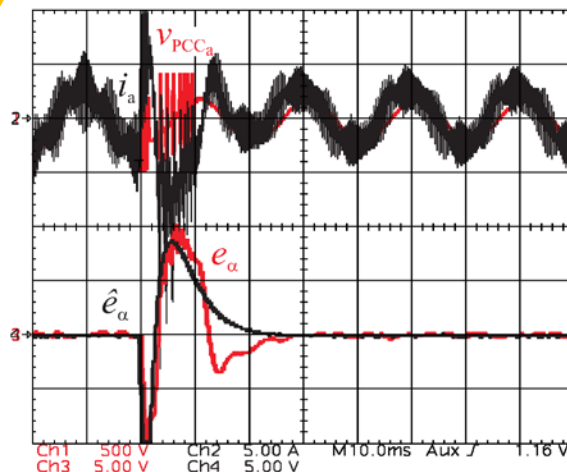
## C. Resonant Controllers Tuned at $f_1$ . Low $f_s$ (2.5 kHz)

VPI

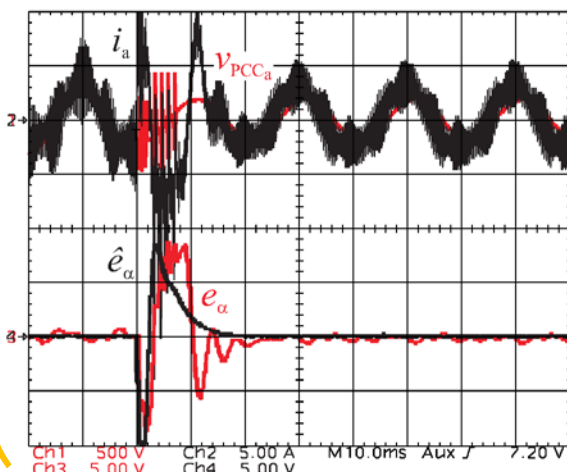
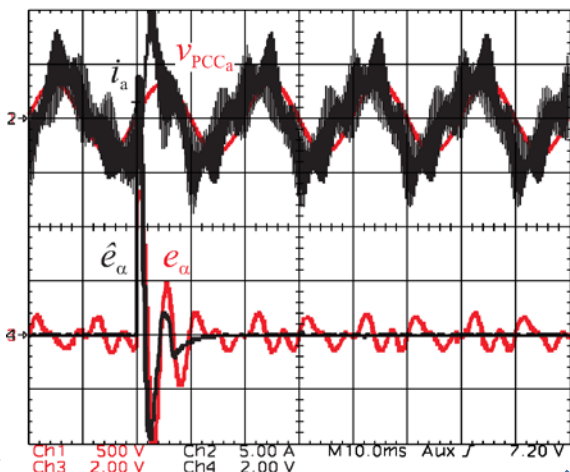
$$E_{\Delta i^*}(z)$$



$$E_{\Delta v_{PCC}}(z)$$



PR

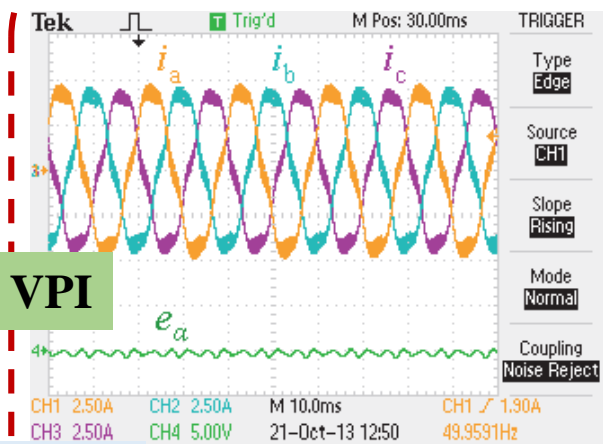


Pag.  
121-125



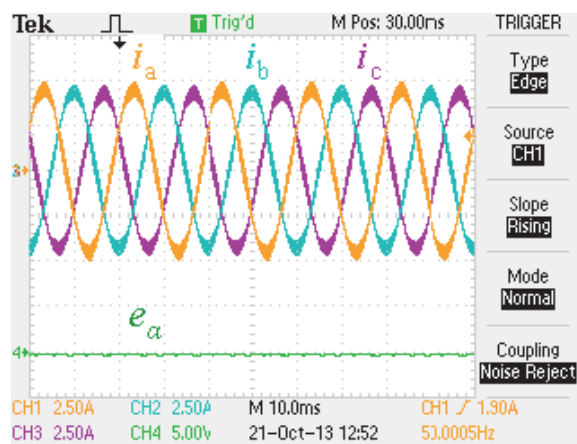
## D. THD Analysis

A.  $f_s=10$  kHz; without harmonic compensation



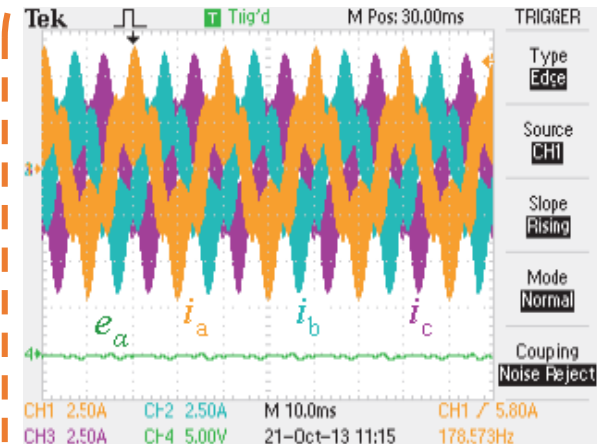
THD = 8.29 %

B.  $f_s=10$  kHz; with harmonic compensation

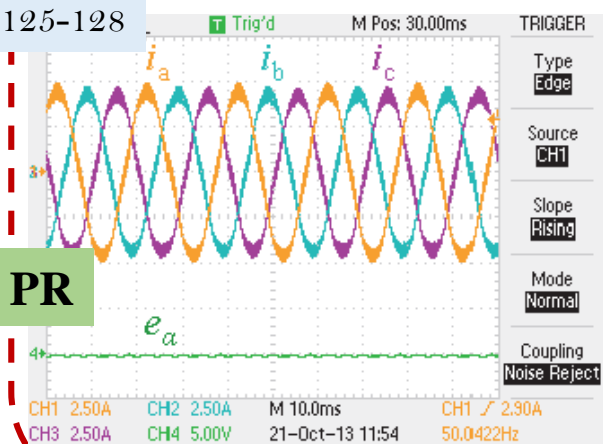


THD = 1.10 %

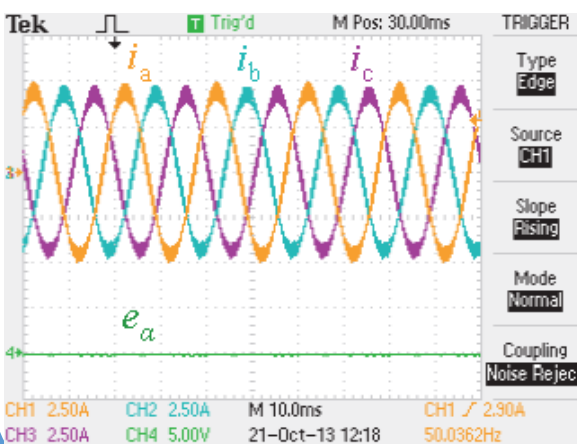
C.  $f_s=2.5$  kHz; without harmonic compensation



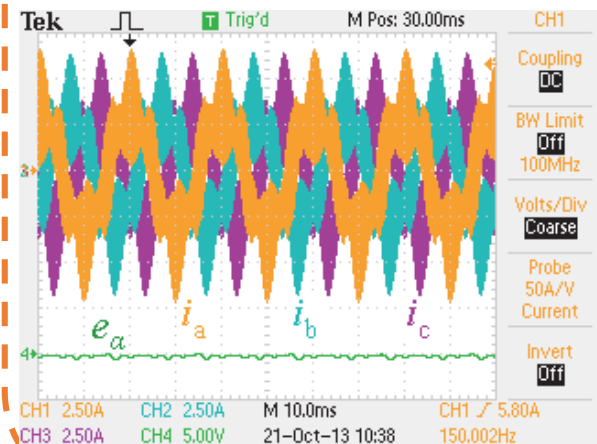
THD = 4.75 %



THD = 2.65 %



THD = 0.92 %



THD = 4.63 %

Controller	$f_s$	$h$	THD	Reference change		Disturbance change	
				Overshoot	Set. time	Overshoot	Set. time
VPI	10 kHz	1	8.29 %	14 %	17 ms	8.6 A	27 ms
PR	10 kHz	1	2.65 %	28 %	9 ms	4.4 A	20 ms
VPI	10 kHz	1, 5, 7	1.10 %	49 %	16 ms	8.8 A	26 ms
PR	10 kHz	1, 5, 7	0.92 %	57 %	12 ms	4.4 A	19 ms
VPI	2.5 kHz	1	4.75 %	13 %	16 ms	12.1 A	28 ms
PR	2.5 kHz	1	4.63 %	40 %	10 ms	10.9 A	22 ms

Controller	$f_s$	$h$	THD	Reference change		Disturbance change	
				Overshoot	Set. time	Overshoot	Set. time
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PR	10 kHz	1, 5, 7	0.92 %	57 %	12 ms	4.4 A	19 ms
VPI	2.5 kHz	1	4.75 %	13 %	16 ms	12.1 A	28 ms
PR	2.5 kHz	1	4.63 %	40 %	10 ms	10.9 A	22 ms

Controller	$f_s$	$h$	THD	Reference change		Disturbance change	
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### Effect of a Feed Forward on the Disturbance Rejection Response

- At high  $f_s$  (10 kHz) → **significant** improvement in overshoot & settling time.
- At low  $f_s$  (2.5 kHz) → improvement in overshoot & **insignificant** improvement in settling time.

### Effect of the PLL on the Disturbance Rejection Response

- In principle, it might have a certain impact: transient in  $v_{dc}$  error in the outer loop & transitory increase in the error.
- Evaluation → **scarce** influence.

## Conclusions of Chapter 5

- This chapter **studies the convenience of VPI controllers** use when **fast transient responses** are demanded:
  - For **new reference tracking**
  - For **disturbance rejection**
- The **transient response** of the current loop is **assessed** by means of the **error signal roots** following the **methodology** proposed in the **previous chapter**.
- Different significant situations considering very **demanding scenarios** have been **analyzed and tested for the VPI controller** and **compared with those obtained with the PR one**.
  - At **high  $f_s$** , **VPI controllers** lead to **longer settling times** than PR ones, for **both reference and disturbance changes** and also to a **higher THD**.
  - At  **$f_s = 2.5$  kHz**, the root loci of both controllers, and accordingly, their transient responses, present **more similarities**, although the **PR regulator is faster**. The **THD is similar**.
- However, **as the sampling frequency decreases**, the **VPI controller** becomes an **interesting alternative** to the PR one: its transient response **can be optimized** at lower sampling frequencies **without risking the stability**.

# Outline

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1. Introduction
2. Equivalent Loss Resistance Estimation of Grid-Tied Converters for Current Control Analysis and Design
3. A Method for Identification of the Equivalent Inductance and Resistance in the Plant Model of Current-Controlled Grid-Tied Converters
4. Assessment and Optimization of the Transient Response of Proportional-Resonant Current Controllers for Distributed Power Generation Systems
5. Transient Response Evaluation of Stationary-Frame Resonant Current Controllers for Grid-Connected Applications
6. Conclusions and Future Research
  - Conclusions
  - Future Research



## Conclusions

- It is demonstrated that **a precise knowledge of  $L$  and  $R$**  (which includes the converter losses) **is essential to guarantee the performance of the current loop** (particularly when specifications are established in terms of transient response). **Closed-loop identification methods**, able to work either **offline or online**, are developed. These methods are also **valid** when **LCL filters** are employed.
- A **methodology to assess and optimize the transient response of PR controllers** is proposed, oriented to **fulfilling the LVRT (disturbance rejection) and grid-support (command tracking) requirements from GCs**. A **criterion for gain tuning** is developed according to the observations.
- A **comparison between the transient response of PR and VPI controllers** is presented, aimed at evaluating the suitability of the latter in grid-tied applications. Their **THD** is also assessed, as well as the **effects of the feedforward and of the PLL on the disturbance rejection response**.

## Future Research

- Study of **the VSC equivalent loss resistance at different frequencies**, from the control point of view. Analysis from the control viewpoint of the **correlation between the VSC equivalent loss resistance and the voltage drops** caused by dead times, the voltage drops in the transistors, etc.
- Development of a **tuning method to optimize the transient response of the current loop at very low ratios between the sampling and fundamental frequencies**. The **complete** transfer function of the **plant admittance** in case of **LCL** filters would be employed.
- Analysis of the different **effects** (positive and negative) of **adding an “active resistance”** in order to **improve the disturbance rejection capability**.
- Study of the **interactions between the outer control of the PCC voltage and the inner current one**.

# Transient Response Analysis and Design of Current-Controlled Grid-Tied Converters

Author: *Ana Vidal González*

Supervisors: *Jesús Doval Gando y & Francisco D. Freijedo Fernández*

Applied Power Electronics Research Group,  
University of Vigo

15th May 2015

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Dissertation submitted for the degree of Doctor of  
Philosophy at the University of Vigo  
“International Doctor Mention”



Universidade de Vigo